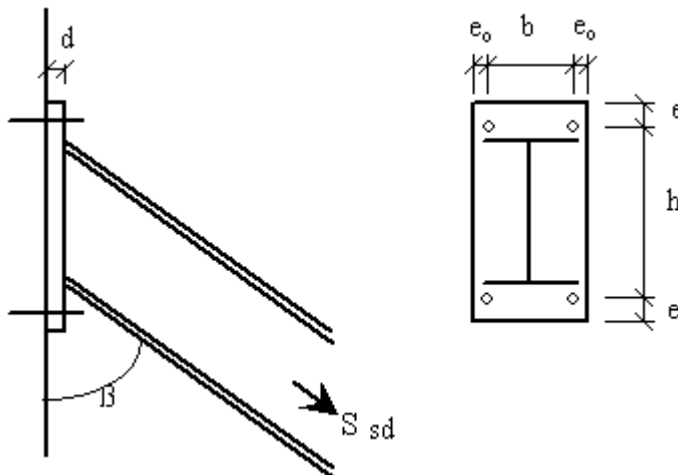


Euro-Code 3

Bolted connections

Bolted angular connection:



Dimensions of connection:

Plate thickness $d =$	15,00 mm
Bolt spacing $e =$	35,00 mm
Spacing of bolts $e_o =$	30,00 mm
Spacing of bolts $b =$	70,00 mm
Spacing of bolts $h =$	220,00 mm
Angle of tension force $\beta =$	45,00 °

Bolts:

Bolt =	SEL("steel/bolt"; BS;)	=	M 20
SC =	SEL("steel/bolt"; SC;)	=	8.8
$f_{u,b} =$	TAB("steel/bolt"; fubk; SC=SC)	=	800,00 N/mm ²
Hole diameter $d_1 =$	TAB("steel/bolt"; d; BS=Bolt)	=	20,00 mm
Shaft diameter $d_{II} =$	$d_1 + 2$	=	22,00 mm
Cross-section areas $A_s =$	TAB("steel/bolt"; Asp; BS=Bolt)	=	2,45 cm ²

Plate:

steel =	SEL("steel/EC"; Name;)	=	Fe 510
$f_y =$	TAB("steel/EC"; fy; Name=steel)	=	355,00 N/mm ²
$f_u =$	TAB("steel/EC"; fu; Name=steel)	=	510,00 N/mm ²
$\gamma_{M0} =$	1,10		
$\gamma_{Mb} =$	1,25		

Loads:

$S_{sd} =$	424,26 kN		
$N_{sd} =$	$\text{COS}(\beta) * S_{sd}$	=	300,00 kN
$V_{sd} =$	$\text{SIN}(\beta) * S_{sd}$	=	300,00 kN

Force per bolt:

$F_{t,sd} =$	$N_{sd} / 4$	=	75,00 kN
$F_{v,sd} =$	$V_{sd} / 4$	=	75,00 kN

Limit tension force of bolts:

$$F_{t,Rd} = 0,9 * f_{u,b} * A_s / \gamma_{Mb} / 10 = 141,12 \text{ kN}$$

$$F_{t,sd} / F_{t,Rd} = \underline{0,53 < 1}$$

Check limit shear force for bolts:

$$F_{v,Rd} = 0,6 * f_{u,b} * \pi * d_l^2 / 4000 / \gamma_{Mb} = 120,64 \text{ kN}$$

$$F_{v,sd} / F_{v,Rd} = \underline{0,62 < 1}$$

Check combined:

$$F_{t,sd} / (1,4 * F_{t,Rd}) + F_{v,sd} / F_{v,Rd} = \underline{1,00 \leq 1}$$

Analysis of bearing strength:

$$\begin{aligned} \text{as in 6.5.1.3:} & \quad e_o / d_{ll} & = & \quad 1,36 > 1 \\ \text{as in 6.5.1.3:} & \quad e_o / d_{ll} & = & \quad 1,36 < 1,5 \\ \text{as in 6.5.1.2(1):} & \quad e / d_{ll} & = & \quad 1,59 > 1,2 \\ \text{as in 6.5.1.2(3):} & \quad b / d_{ll} & = & \quad 3,18 > 3 \end{aligned}$$

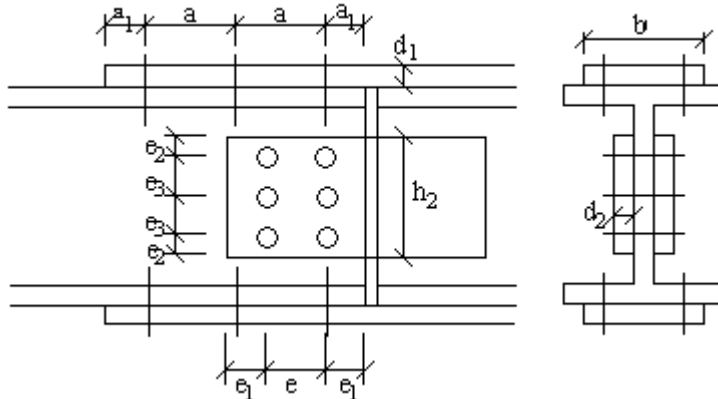
$$\alpha = \text{MIN}(e / (3 * d_{ll}); b / (3 * d_{ll}) - 0,25; f_{u,b} / f_u; 1) = 0,53$$

$$\text{Tab.6.5.3 } F_{b1,Rd} = 2,5 * \alpha * f_u * d_l * d / \gamma_{Mb} / 10^3 = 162,18 \text{ kN}$$

$$6.5.5.(10) F_{b2,Rd} = 2/3 * F_{b1,Rd} = 108,12 \text{ kN}$$

$$F_{b,Rd} = F_{b2,Rd} + (F_{b1,Rd} - F_{b2,Rd}) * (e_o / d_l - 1,2) / 0,3 = 162,18 \text{ kN}$$

$$F_{v,sd} / F_{b,Rd} = \underline{0,46 < 1}$$

Bolted connection subject to bending**Dimensions of connection:**

$a =$	80,00 mm	
$a_1 =$	45,00 mm	
$e =$	80,00 mm	
$e_1 =$	45,00 mm	
$e_2 =$	50,00 mm	
$e_3 =$	90,00 mm	
$d_1 =$	20,00 mm	
$d_2 =$	8,00 mm	
$b_1 =$	160,00 mm	
$h_2 =$	$2 * (e_2 + e_3)$	$= 280,00 \text{ mm}$

Flansch-Bolts:

Bolt _f =	SEL("steel/bolt"; BS;)	=	M 20
SC1 =	SEL("steel/bolt"; SC;)	=	4.6
$f_{u,bo} =$	TAB("steel/bolt"; fubk; SC=SC1)	=	400,00 N/mm ²
Hole diameter $d_{lo} =$	TAB("steel/bolt"; d; BS=Bolt _f)	=	20,00 mm
Shaft diameter $d_{l1o} =$	$d_{lo} + 2$	=	22,00 mm
Number of rows $n_o =$		=	3

Steg-Bolts:

Bolt _s =	SEL("steel/bolt"; BS;)	=	M 16
SC2 =	SEL("steel/bolt"; SC;)	=	4.6
$f_{u,bs} =$	TAB("steel/bolt"; fubk; SC=SC2)	=	400,00 N/mm ²
Hole diameter $d_{ls} =$	TAB("steel/bolt"; d; BS=Bolt _s)	=	16,00 mm
Shaft diameter $d_{l1s} =$	$d_{ls} + 2$	=	18,00 mm
Number of rows $n_s =$		=	3
Number of columns $m_s =$		=	2

Profil:

Profil Typ =	SEL("steel/Profils"; Name;)	=	IPE
Selected Profil =	SEL("steel/"Typ; Name;)	=	IPE 240
Column height $h =$	TAB("steel/"Typ; h; Name=Profil)	=	240,00 mm
Web thickness $s =$	TAB("steel/"Typ; s; Name=Profil)	=	6,20 mm
Flange thickness $t =$	TAB("steel/"Typ; t; Name=Profil)	=	9,80 mm
Cross-sectional area $A =$	TAB("steel/"Typ; A; Name=Profil)	=	39,10 cm ²
Moment of resistance $W_y =$	TAB("steel/"Typ; W _y ; Name=Profil)	=	324,00 cm ³
Moment of resistance $W_{pl} =$	$1,14 * W_y$	=	369,36 cm ³

Material and Partial safety factors:

$$\begin{aligned}
 \text{steel} &= \text{SEL}(\text{"steel/EC"; Name; }) &= & \text{Fe 360} \\
 f_y &= \text{TAB}(\text{"steel/EC"; } f_y; \text{ Name=steel}) &= & 235,00 \text{ N/mm}^2 \\
 f_u &= \text{TAB}(\text{"steel/EC"; } f_u; \text{ Name=steel}) &= & 360,00 \text{ N/mm}^2 \\
 \gamma_{M0} &= & & 1,10 \\
 \gamma_{M2} &= & & 1,25
 \end{aligned}$$

Loads:

$$\begin{aligned}
 M_{sd} &= 157,95 \text{ kNm} \\
 V_{sd} &= 60,75 \text{ kN}
 \end{aligned}$$

Check beam-web strength without holes:

$$\begin{aligned}
 M_{c,Rd} &= W_{pl} * f_y / \gamma_{M0} / 10^3 &= & 78,91 \text{ kNm} \\
 M_{sd} / M_{c,Rd} &= & & \underline{2,00 < 1} \\
 A_v &= 1,04 * h * s / 100 &= & 15,48 \text{ cm}^2 \\
 V_{pl,Rd} &= A_v * f_y / 10 / \sqrt{3} / \gamma_{M0} &= & 190,93 \text{ kN} \\
 V_{sd} / V_{pl,Rd} &= & & \underline{0,32 < 1}
 \end{aligned}$$

Check beam-web strength with holes:

$$\begin{aligned}
 A_z &= 0,5 * A &= & 19,55 \text{ cm}^2 \\
 A_{z,net} &= A_z - (2 * d_{10} * t + ((n_s - 1) / 2) * d_{1s} * s) / 100 &= & 14,12 \text{ cm}^2 \\
 (f_y / f_u * \gamma_{M2} / \gamma_{M0}) / (0,9 * A_{z,net} / A_z) &= & & 1,14 \leq 1 \\
 W_{pl,net} &= W_{pl} - 2 * d_{10} * t * (h - t) / 2000 &= & 319,73 \text{ cm}^3 \\
 M_{c,Rd,C} &= W_{pl,net} * f_y / (\gamma_{M0} * 10^3) &= & 68,31 \text{ kNm} \\
 M_{sd} / M_{c,Rd,C} &= & & \underline{2,31 < 1} \\
 A_{v,net} &= A_v - n_s * d_{1s} * s / 100 &= & 12,13 \text{ cm}^2 \\
 f_y / f_u * A_v / A_{v,net} &= & & \underline{0,83 < 1} \\
 &\Rightarrow \text{Area of holes will be neglected.}
 \end{aligned}$$

Analysis of bolts in flange:

$$\begin{aligned}
 I_w &= 2 / 12 * d_2 * h_2^3 / 10^4 &= & 2926,93 \text{ cm}^4 \\
 I_f &= 2 * b_1 * d_1 * ((h + d_1) / 2)^2 / 10^4 &= & 10816,00 \text{ cm}^4 \\
 M_w &= M_{sd} * I_w / (I_w + I_f) &= & 33,64 \text{ kNm} \\
 M_f &= M_{sd} * I_f / (I_w + I_f) &= & 124,31 \text{ kNm}
 \end{aligned}$$

Effective tension force in flange:

$$\begin{aligned}
 N_{sd} &= M_f / (h + d_1) * 10^3 &= & 478,12 \text{ kN} \\
 \text{Limit shear force} & & & \\
 F_{v,Rd} &= n_o * 2 * 0,6 * f_{u,bo} * \pi/4 * d_{lo}^2 / \gamma_{M2} / 10^3 &= & 361,91 \text{ kN} \\
 \text{Limit bearing force:} & & & \\
 \alpha &= \text{MIN}(a_1 / (3 * d_{10}); a / (3 * d_{10}) - 0,25; f_{u,bo} / f_u; 1) &= & 0,682 \\
 F_{b,Rd} &= 2 * n_o * 2,5 * \alpha * f_u * d_{lo} * t / \gamma_{M2} / 10^3 &= & 577,46 \text{ kN} \\
 N_{sd} / \text{MIN}(F_{v,Rd}; F_{b,Rd}) &= & & \underline{1,32 < 1}
 \end{aligned}$$

Analysis of bolts in web:

$$\begin{aligned}
 n_{s1} &= (n_s - 1) / 2 + 0,49 & = & 1 \\
 n_{s2} &= n_{s1} * 2 & = & 2 \\
 m_{s1} &= (m_s - 1) / 2 + 0,49 & = & 1 \\
 m_{s2} &= m_{s1} * 2 & = & 2 \\
 I_p &= (n_s * m_{s2} * ((m_s - 1) / 2 * e)^2 + n_{s2} * m_s * ((n_s - 1) / 2 * e_3)^2) / 10^2 & = & 420,00 \text{ cm}^2 \\
 M_{sw} &= M_w + V_{sd} * e_3 / 10^3 & = & 39,11 \text{ kNm} \\
 R_{sd} &= \sqrt{((10 * M_{sw} * e_3 / I_p)^2 + ((V_{sd} / (m_s * n_s)) + 10 * M_{sw} * (m_s - 1) / 2 * e / I_p)^2)} & = & 96,27 \text{ kN} \\
 F_{v,Rd} &= m_s * 0,6 * f_{u,bs} * \pi / 4 * d_{ls}^2 / 10^3 / \gamma_{M2} & = & 77,21 \text{ kN} \\
 \alpha &= \text{MIN}(e_1 / (3 * d_{l1s}); e / (3 * d_{l1s}) - 0,25; f_{u,bo} / f_u; 1) & = & 0,833 \\
 F_{b,Rd} &= 2,5 * \alpha * f_u * d_{ls} * s / \gamma_{M2} / 10^3 & = & 59,50 \text{ kN}
 \end{aligned}$$

$$R_{sd} / \text{MIN}(F_{v,Rd}; F_{b,Rd}) = \underline{\underline{1,62 < 1}}$$

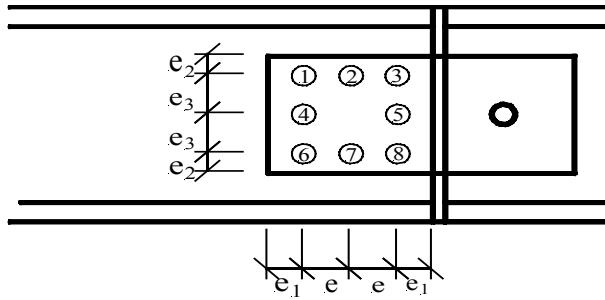
Analysis of cover plates:

$$\begin{aligned}
 A &= d_1 * b_1 / 100 & = & 32,00 \text{ cm}^2 \\
 A_{net} &= A - (2 * d_{l10} * d_1) / 100 & = & 23,20 \text{ cm}^2
 \end{aligned}$$

Limit tension force:

$$N_{t,Rd} = \text{MIN}(A * f_y / \gamma_{M0}; 0,9 * A_{net} * f_u / \gamma_{M2}) / 10 = 601,34 \text{ kN}$$

$$N_{sd} / N_{t,Rd} = \underline{\underline{0,80 < 1}}$$

Connection subject to moment load:**Dimensions of connection:**

Bolt spacing e =	50,00 mm
Edge distance e1 =	35,00 mm
Bolt spacing e3 =	70,00 mm
Plate thickness t =	6,00 mm
Number of bolts n =	8

Bolts:

Bolt1 =	SEL("steel/bolt"; BS;)	=	M 30
SC1 =	SEL("steel/bolt"; SC;)	=	5.6
$f_{u,b1}$ =	TAB("steel/bolt"; fubk; SC=SC1)	=	500,00 N/mm ²
Hole diameter d_{11} =	TAB("steel/bolt"; d; BS=Bolt1)	=	30,00 mm

Bolt2 =	SEL("steel/bolt"; BS;)	=	M 12
SC2 =	SEL("steel/bolt"; SC;)	=	5.6
$f_{u,b2}$ =	TAB("steel/bolt"; fubk; SC=SC2)	=	500,00 N/mm ²
Hole diameter d_{s2} =	TAB("steel/bolt"; d; BS=Bolt2)	=	12,00 mm
Shaft diameter d_{12} =	$d_{s2}+1$	=	13,00 mm

IPE330 aus

steel =	SEL("steel/EC"; Name;)	=	Fe 360
f_{u2} =	TAB("steel/EC"; fu; Name=steel)	=	360,00 N/mm ²
γ_{Mb} =	1,25		
γ_{Mo} =	1,25		

Loads:

V_{sd} =	58,70 kN
M_{sd} =	910,00 kNcm

Analysis of the right bolt:

Check limit shear force

$$F_{v,Rd} = 0,6 * \pi / 4 * (d_{11} / 10)^2 * f_{u,b1} / \gamma_{Mo} / 10 = 169,65 \text{ kN}$$

$$V_{sd} / F_{v,Rd} = \underline{\underline{0,35 < 1}}$$

Limit bearing strength

$$F_{b,Rd} = 1,5 * d_{11} * t * f_{u2} / \gamma_{Mb} / 10^3 = 77,76 \text{ kN}$$

$$V_{sd} / F_{b,Rd} = \underline{\underline{0,75 < 1}}$$

Check bolts on left:

$$I_p = (6 * e^2 + 6 * e_3^2) / 100 = 444,00 \text{ cm}^2$$

Maximum horizontal force in bolt due to moment:

$$F_h = M_{sd} * e_3 / 10 / I_p = 14,35 \text{ kN}$$

Maximum vertical force:

$$F_v = M_{sd} * e / 10 / I_p + V_{sd} / n = 17,59 \text{ kN}$$

Resulting force

$$R_r = \sqrt{(F_h^2 + F_v^2)} = 22,70 \text{ kN}$$

$$F_{v,Rd} = 0,6 * f_{u,b2} * d_{l2}^2 * \pi / 4 / \gamma_{Mb} / 10^3 = 31,86 \text{ kN}$$

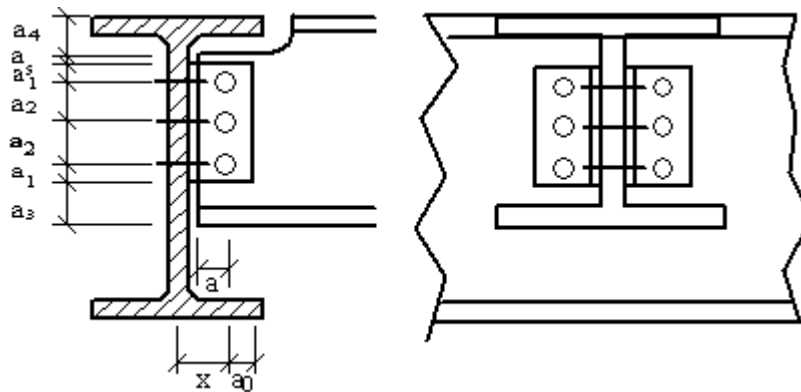
$$R_r / F_{v,Rd} = \underline{0,71 < 1}$$

Analysis of bearing strength

$$\alpha = \text{MIN}(e_1 / (3 * d_{l2}); 2 * e / (3 * d_{l2}) - 0,25; f_{u,b2} / f_{u2}; 1) = 0,90$$

$$F_{b,Rd} = 2,5 * \alpha * f_{u2} * d_{l2} * t / \gamma_{Mb} / 10^3 = 50,54 \text{ kN}$$

$$F_h / F_{b,Rd} = \underline{0,28 < 1}$$

Bolted shear joint:**Dimensions of connection:**

Spacing of bolts a =	45,00 mm
Spacing of bolts a_0 =	35,00 mm
Spacing of bolts a_1 =	30,00 mm
Spacing of bolts a_2 =	50,00 mm
Spacing of bolts a_3 =	90,00 mm
Depth of cope a_4 =	30,00 mm
Plate projection a_5 =	20,00 mm
Lever-arm x =	45,00 mm
Number of bolts n =	3

Bolts:

M16 4.6

Bolt =	SEL("steel/bolt"; BS;)	=	M 16
SC =	SEL("steel/bolt"; SC;)	=	4.6
$f_{u,b}$ =	TAB("steel/bolt"; fubk; SC=SC)	=	400,00 N/mm ²
Hole diameter d_f =	TAB("steel/bolt"; d; BS=Bolt)	=	16,00 mm
Shaft diameter d_0 =	$d_f + 2$	=	18,00 mm

Angle section P =	SEL("steel/WG"; Name;)	=	L 80x8
Angle thickness t =	TAB("steel/WG"; s; Name=P)	=	8,00 mm

Factor for group bolts as in 6.5.2..2(3):

k =	0,5 for 1 group bolts; =2,5 for 2 rows
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steel =	SEL("steel/EC"; Name;)	=	Fe 360
f_y =	TAB("steel/EC"; f_y ; Name=steel)	=	235,00 N/mm ²
f_u =	TAB("steel/EC"; f_u ; Name=steel)	=	360,00 N/mm ²

Profil Typ =	SEL("steel/Profils"; Name;)	=	IPE
Selected Profil =	SEL("steel/"Typ; Name;)	=	IPE 270
Column height h =	TAB("steel/"Typ; h ; Name=Profil)	=	270,00 mm
Web thickness s =	TAB("steel/"Typ; s ; Name=Profil)	=	6,60 mm

γ_{Mb} =	1,25
γ_{M2} =	1,25
γ_{M0} =	1,10

Loads:

V_{sd} =	60,00 kN
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Check bolt spacing as in 6.5.1:

$$\begin{aligned}
 1,2 * d_0 / a_1 &= 0,72 < 1 \\
 a_1 / \text{MAX}(12 * t; 150) &= 0,20 < 1 \\
 1,5 * d_0 / a_0 &= 0,77 < 1 \\
 a_0 / \text{MAX}(12 * t; 150) &= 0,23 < 1 \\
 2,2 * d_0 / a_2 &= 0,79 < 1 \\
 a_2 / \text{MIN}(12 * s; 200) &= 0,63 < 1
 \end{aligned}$$

Check bolts strength:

$$\begin{aligned}
 \text{Bolts in web of main beam } F_{v,sd} &= V_{sd} / (2 * n) &= 10,00 \text{ kN} \\
 \text{Bolts in web of connecting beam } M_{sd} &= x / 10 * V_{sd} &= 270,00 \text{ kNm} \\
 \text{Horizontal force due to } M_{sd} F_{h,sd} &= M_{sd} / ((n - 1) * a_2 / 10) &= 27,00 \text{ kN} \\
 \text{Distributed shearing force on bolts } F_{v,sd} &= V_{sd} / n &= 20,00 \text{ kN} \\
 \text{Maximum bolt strength } F_{sd} &= \sqrt{F_{h,sd}^2 + F_{v,sd}^2} &= 33,60 \text{ kN}
 \end{aligned}$$

Limit strength and analysis of bolts:**Bolts in web of main beam:**

$$\text{Plain ...in the shear plane } F_{v,Rd} = 0,6 * f_{u,b} * \pi * d_l^2 / 4 / \gamma_{Mb} / 10^3 = 38,60 \text{ kN}$$

Limit bearing strength

$$\begin{aligned}
 \alpha &= \text{MIN}(a_1 / (3 * d_0); a_2 / (3 * d_0) - 0,25; f_{u,b} / f_u; 1) &= 0,556 \\
 F_{b,Rd} &= 2,5 * \alpha * f_u * d_l * t / \gamma_{Mb} / 10^3 &= 51,24 \text{ kN}
 \end{aligned}$$

Analysis:

$$F_{sd} / F_{b,Rd} = \underline{0,66 < 1}$$

Bolts in web of connecting beam:

$$F_{v,Rd} = 2 * 0,6 * f_{u,b} * \pi * d_l^2 / 4 / \gamma_{Mb} / 10^3 = 77,21 \text{ kN}$$

Limit bearing strength

$$\begin{aligned}
 \alpha &= \text{MIN}(a_1 / (3 * d_0); a_2 / (3 * d_0) - 0,25; f_{u,b} / f_u; 1) &= 0,556 \\
 F_{b,Rd} &= 2,5 * \alpha * f_u * d_l * s / \gamma_{Mb} / 10^3 &= 42,27 \text{ kN}
 \end{aligned}$$

Analysis:

$$F_{sd} / F_{b,Rd} = \underline{0,79 < 1}$$

Check angle section strength

Design loads:

$$\begin{aligned}
 V_{sdw} &= V_{sd} / 2 &= 30,00 \text{ kN} \\
 M_{sdw} &= M_{sd} / 2 &= 135,00 \text{ kNm}
 \end{aligned}$$

$$A = (2 * a_2 + 2 * a_1) * t / 200 = 6,40 \text{ cm}^2$$

$$A_{net} = (2 * a_2 + 2 * a_1 - n * d_0) * t / 200 = 4,24 \text{ cm}^2$$

$$(f_y / f_u * \gamma_{M2} / \gamma_{M0}) / (0,9 * A_{net} / A) = 1,24 > 1$$

⇒ Subtract bottom bolt holes.

$$A = A * 2 = 12,80 \text{ cm}^2$$

$$A_{net} = A_{net} * 2 = 8,48 \text{ cm}^2$$

$$f_y / f_u * A / A_{net} = 0,99 < 1$$

⇒ Bolt holes should not be subtracted

$$W_{pl} = (t * (2 * a_2 + 2 * a_1)^2 / 4 - d_0 * t * a_2) / 1000 = 44,00 \text{ cm}^3$$

$$M_{pl,Rd} = W_{pl} * f_y / 10 / \gamma_{M0} = 940,00 \text{ kNm}$$

$$M_{sd} / M_{pl,Rd} = \underline{0,29 < 1}$$

$$V_{pl,Rd} = A * f_y / 10 / (\sqrt{3} * \gamma_{M0}) = 157,88 \text{ kN}$$

$$V_{sd} / V_{pl,Rd} = \underline{0,38 < 1}$$

Also:

$$V_{sd} / (V_{pl,Rd} / 2) = \underline{0,76 < 1}$$

⇒ No interaction.

Check shear failure:

$$L_v = (n - 1) * a_2 = 100,00 \text{ mm}$$

$$L_1 = a_2 = 50,00 \text{ mm}$$

$$L_1 / (5 * d_0) = 0,56 < 1$$

$$L_2 = (a - k * d_0) * f_u / f_y = 55,15 \text{ mm}$$

$$L_3 = L_v + a_2 + a_3 = 240,00 \text{ mm}$$

$$L_{v,eff} = L_v + L_1 + L_2 = 205,15 \text{ mm}$$

$$L_{v,eff} / L_3 = 0,85 < 1$$

$$L_3 / ((L_v + a_2 + a_3 - n * d_0) * f_u / f_y) = 0,84 < 1$$

Effective shear area:

$$A_{v,eff} = L_{v,eff} * t / 100 = 16,41 \text{ cm}^2$$

$$V_{eff,Rd} = A_{v,eff} * f_y / 10 / \sqrt{3} / \gamma_{M0} = 202,41 \text{ kN}$$

$$V_{sd} / V_{eff,Rd} = \underline{\underline{0,30 < 1}}$$

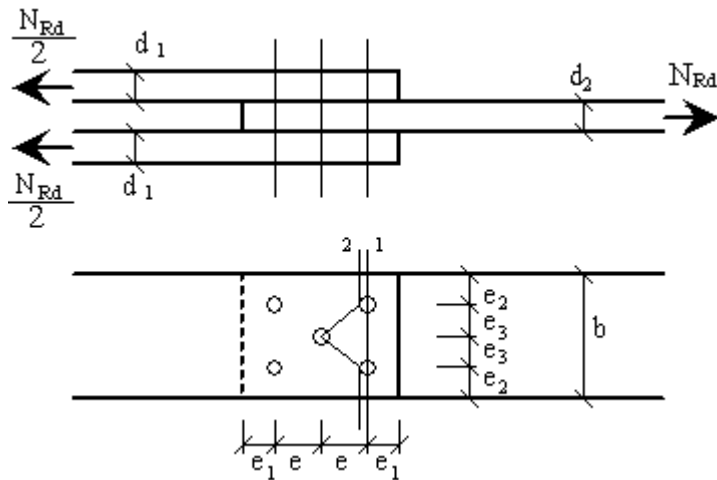
Double shear joint with bolts:**Dimensions of connection:**

Plate thickness $d_1 =$	6,00 mm
Number of plates $n_1 =$	2
Plate thickness $d_2 =$	7,10 mm
Number of plates $n_2 =$	1
Plate width $b =$	210,00 mm
Bolt spacing $e =$	40,00 mm
Edge distance $e_1 =$	60,00 mm
Edge distance $e_2 =$	40,00 mm
Bolt spacing $e_3 =$	65,00 mm

Bolts:

Bolt =	SEL("steel/bolt"; BS;)	=	M 20
SC =	SEL("steel/bolt"; SC;)	=	10.9
$f_{u,b} =$	TAB("steel/bolt"; fubk; SC=SC)	=	1000,00 N/mm ²
Hole diameter $d_f =$	TAB("steel/bolt"; d; BS=Bolt)	=	20,00 mm
Cross-section areas $A_s =$	TAB("steel/bolt"; Asp; BS=Bolt)	=	2,45 cm ²
Number of bolts $n =$			5

Plate :

steel =	SEL("steel/EC"; Name;)	=	Fe 360
$f_y =$	TAB("steel/EC"; fy; Name=steel)	=	235,00 N/mm ²
$f_u =$	TAB("steel/EC"; fu; Name=steel)	=	360,00 N/mm ²
$\gamma_{M0} =$			1,10
$\gamma_{M2} =$			1,25

Loads:

$N_{sd} =$	100,00 kN
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Joint with tension and shear:**Limit tension force of plate links**

$A =$	$b * d_1 * n_1 / 100$	=	25,20 cm ²
$d =$	$d_1 + 2$	=	22,00 mm
Cross-section area 1:			
$A_{net,1} =$	$A - 2 * d * d_1 * n_1 / 100$	=	19,92 cm ²

Cross-section area 2:

$$A_{\text{net},2} = A - 3 * d * d_1 * n_1 / 10^2 + 2 * e^2 / (4 * e_3) * d_1 * n_1 / 10^2 = 18,76 \text{ cm}^2$$

$$A_{\text{net}} = \text{MIN}(A_{\text{net},1}; A_{\text{net},2}) = 18,76 \text{ cm}^2$$

$$N_{t,Rd1} = \text{MIN}(A * f_y / \gamma_{M0}; 0,9 * A_{\text{net}} * f_u / \gamma_{M2}) / 10 = 486,26 \text{ kN}$$

Limit tension force of plate rechte

$$A = b * d_2 * n_2 / 100 = 14,91 \text{ cm}^2$$

$$d = d_1 + 2 = 22,00 \text{ mm}$$

$$A_{\text{net},1} = A - 2 * d * d_2 * n_2 / 100 = 11,79 \text{ cm}^2$$

$$A_{\text{net},2} = A - 3 * d * d_2 * n_2 / 10^2 + 2 * e^2 / (4 * e_3) * d_2 * n_2 / 10^2 = 11,10 \text{ cm}^2$$

$$A_{\text{net}} = \text{MIN}(A_{\text{net},1}; A_{\text{net},2}) = 11,10 \text{ cm}^2$$

$$N_{t,Rd2} = \text{MIN}(A * f_y / \gamma_{M0}; 0,9 * A_{\text{net}} * f_u / \gamma_{M2}) / 10 = 287,71 \text{ kN}$$

$$N_{t,Rd} = \text{MIN}(N_{t,Rd2}; N_{t,Rd1}) = \underline{\underline{287,71 \text{ kN}}}$$

Limit tension force of boltsn:

$$A_s = \pi * (d_i / 10)^2 / 4 = 3,14 \text{ cm}^2$$

Thread in the shearing plane:

$$F_{v,Rd} = 0,6 * n * (n_1 + n_2 - 1) * f_{u,b} / 10 * A_s / \gamma_{M2} = 1507,20 \text{ kN}$$

Limit bearing strength

$$\alpha = \text{MIN}(e_1 / (3 * d); 2 * e / (3 * d) - 0,25; f_{u,b} / f_u; 1) = 0,91$$

$$F_{b,Rd1} = n_1 * n * 2,5 * \alpha * f_u * d_i * d_1 / \gamma_{M2} / 10^3 = 786,24 \text{ kN}$$

$$\alpha = \text{MIN}(e_1 / (3 * d); 2 * e / (3 * d) - 0,25; f_{u,b} / f_u; 1) = 0,91$$

$$F_{b,Rd2} = n_2 * n * 2,5 * \alpha * f_u * d_i * d_2 / \gamma_{M2} / 10^3 = 465,19 \text{ kN}$$

$$F_{b,Rd} = \text{MIN}(F_{b,Rd1}; F_{b,Rd2}) = \underline{\underline{465,19 \text{ kN}}}$$

Maximum allowed force:

$$N_{l,Rd} = \text{MIN}(N_{t,Rd}; F_{v,Rd}; F_{b,Rd}) = \underline{\underline{287,71 \text{ kN}}}$$

Analysis:

$$N_{sd} / N_{l,Rd} = \underline{\underline{0,35 < 1}}$$

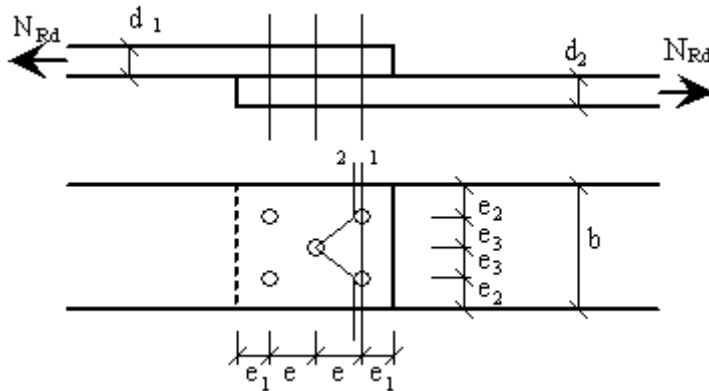
High strength friction-grip bolt connection:**Dimensions of connection:**

Plate thickness 1 d_1 =	10,00 mm
Plate thickness 2 d_2 =	8,00 mm
Bolt spacing e =	65,00 mm
Edge distance e_1 =	55,00 mm
Edge distance e_2 =	50,00 mm
Bolt spacing e_3 =	70,00 mm
Plate width b =	240,00 mm

Bolts:

Bolt =	SEL("steel/bolt"; BS;)	=	M 22
SC =	SEL("steel/bolt"; SC;)	=	10.9
$f_{u,b}$ =	TAB("steel/bolt"; fubk; SC=SC)	=	1000,00 N/mm ²
Hole diameter d_f =	TAB("steel/bolt"; d; BS=Bolt)	=	22,00 mm
Cross-section areas A_s =	TAB("steel/bolt"; Asp; BS=Bolt)	=	3,03 cm ²
Number of bolts n =			5

Löcher mit normalem Lochspiel as in 6.5.8.1 (2) K_s =	1,00
Anzahl der Gleitfugen as in 6.5.8.1 (1) η =	1,00
Reibungszahl as in 6.5.8.3 μ =	0,40
as in 6.5.8.1 (3) γ_{Ms} =	1,25

Plate:

steel =	SEL("steel/EC"; Name;)	=	Fe 360
f_y =	TAB("steel/EC"; fy; Name=steel)	=	235,00 N/mm ²
f_u =	TAB("steel/EC"; fu; Name=steel)	=	360,00 N/mm ²
γ_{M0} =	1,10		
γ_{M2} =	1,25		

Loads:

Tension force N_{sd} =	100,00 kN
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Limit tension force of plate:

A =	$b \cdot \text{MIN}(d_1; d_2) / 100$	=	19,20 cm ²
as in 7.5.2 $d = d_1 + 2$		=	24,00 mm
Cross-section area 1:			
$A_{net,1}$ =	$A - 2 \cdot d \cdot \text{MIN}(d_1; d_2) / 10^2$	=	15,36 cm ²
Cross-section area 2:			
$A_{net,2}$ =	$A - 3 \cdot d \cdot \text{MIN}(d_1; d_2) / 10^2 + 2 \cdot e^2 / (4 \cdot e_3) \cdot \text{MIN}(d_1; d_2) / 10^2$	=	15,85 cm ²
A_{net} =	$\text{MIN}(A_{net,1}; A_{net,2})$	=	15,36 cm ²

Friction-grip connection:

Plate

$$N_{net,Rd} = A_{net} * f_y / 10 / \gamma_{M0} = 328,15 \text{ kN}$$

Limit tension force of bolts

$$\text{Limit shank tension } F_{p,cd} = 0,7 * f_{u,b} / 10 * A_s = 212,10 \text{ kN}$$

$$\text{Limit slip resistance force } F_{s,Rd} = n * K_s * \eta * \mu * F_{p,cd} / \gamma_{Ms} = 339,36 \text{ kN}$$

Limit bearing force:

$$\alpha = \text{MIN}(e_1 / (3 * d); 2 * e / (3 * d) - 0,25; f_{u,b} / f_u; 1) = 0,76$$

$$F_{b,Rd} = n * 2,5 * \alpha * f_u / 10 * d_l * \text{MIN}(d_1; d_2) / \gamma_{M2} / 100 = 481,54 \text{ kN}$$

Maximum allowed force:

$$N_{g,Rd} = \text{MIN}(N_{net,Rd}; F_{b,Rd}; F_{s,Rd}) = \underline{\underline{328,15 \text{ kN}}}$$

Analysis:

$$N_{sd} / N_{g,Rd} = \underline{\underline{0,30 < 1}}$$

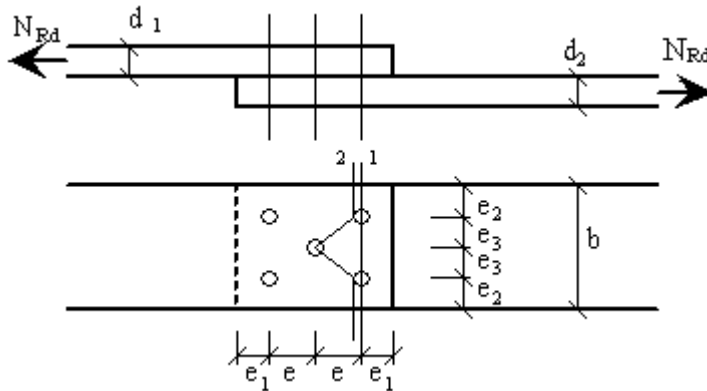
Joint with tension and shear:**Dimensions of connection:**

Plate thickness $d_1 =$	10,00 mm
Plate thickness $d_2 =$	8,00 mm
Bolt spacing $e =$	65,00 mm
Edge distance $e_1 =$	55,00 mm
Edge distance $e_2 =$	50,00 mm
Bolt spacing $e_3 =$	70,00 mm
Plate width $b =$	240,00 mm

Bolts:

Bolt =	SEL("steel/bolt"; BS;)	=	M 22
SC =	SEL("steel/bolt"; SC;)	=	4.6
$f_{u,b} =$	TAB("steel/bolt"; fubk; SC=SC)	=	400,00 N/mm ²
Hole diameter $d_1 =$	TAB("steel/bolt"; d; BS=Bolt)	=	22,00 mm
Cross-section areas $A_s =$	TAB("steel/bolt"; Asp; BS=Bolt)	=	3,03 cm ²
Number of bolts $n =$			5

Plate:

steel =	SEL("steel/EC"; Name;)	=	Fe 360
$f_y =$	TAB("steel/EC"; fy; Name=steel)	=	235,00 N/mm ²
$f_u =$	TAB("steel/EC"; fu; Name=steel)	=	360,00 N/mm ²
$\gamma_{M0} =$	1,10		
$\gamma_{M2} =$	1,25		

Loads:

$N_{sd} =$	100,00 kN
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Joint with tension and shear:**Limit tension force of plate:**

$A =$	$b * \text{MIN}(d_1; d_2) / 100$	=	19,20 cm ²
$d =$	$d_1 + 2$	=	24,00 mm
Cross-section area 1:			
$A_{net,1} =$	$A - 2 * d * \text{MIN}(d_1; d_2) / 100$	=	15,36 cm ²
Cross-section area 2:			
$A_{net,2} =$	$A - 3 * d * \text{MIN}(d_1; d_2) / 10^2 + 2 * e^2 / (4 * e_3) * \text{MIN}(d_1; d_2) / 10^2$	=	15,85 cm ²
$A_{net} =$	$\text{MIN}(A_{net,1}; A_{net,2})$	=	15,36 cm ²
$N_{t,Rd} =$	$\text{MIN}(A * f_y / \gamma_{M0}; 0,9 * A_{net} * f_u / \gamma_{M2}) / 10$	=	398,13 kN

Limit tension force of bolts:

$$A_s = \pi * (d / 10)^2 / 4 = 4,52 \text{ cm}^2$$

Thread in the shearing plane:

$$F_{v,Rd} = 0,6 * n * f_{u,b} / 10 * A_s / \gamma_{M2} = 433,92 \text{ kN/cm}^2$$

Limit bearing strength

$$\alpha = \text{MIN}(e_1 / (3 * d); 2 * e / (3 * d) - 0,25; f_{u,b} / f_u; 1) = 0,76$$

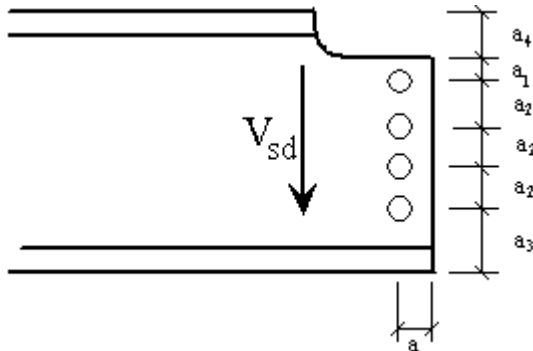
$$F_{b,Rd} = n * 2,5 * \alpha * f_u * d * \text{MIN}(d_1; d_2) / \gamma_{M2} / 10^3 = 525,31 \text{ kN}$$

Maximum allowed force:

$$N_{I,Rd} = \text{MIN}(N_{t,Rd}; F_{v,Rd}; F_{b,Rd}) = \underline{\underline{398,13 \text{ kN}}}$$

Analysis:

$$N_{sd} / N_{I,Rd} = \underline{\underline{0,25 < 1}}$$

Check shear failure:**Dimensions of connection:**

Spacing of bolts a =	50,00 mm
Spacing of bolts a_1 =	43,00 mm
Spacing of bolts a_2 =	70,00 mm
Spacing of bolts a_3 =	75,00 mm
Number of bolts n =	4

Bolts:

Bolt =	SEL("steel/bolt"; BS;)	=	M 20
SC =	SEL("steel/bolt"; SC;)	=	5.6
$f_{u,b}$ =	TAB("steel/bolt"; fubk; SC=SC)	=	500,00 N/mm ²
Hole diameter d_1 =	TAB("steel/bolt"; d; BS=Bolt)	=	20,00 mm
Shaft diameter d_2 =	$d_1 + 2$	=	22,00 mm
k =	0,5 for 1 group bolts; =2,5 for 2 rows		
steel =	SEL("steel/EC"; Name;)	=	Fe 360
f_y =	TAB("steel/EC"; f_y ; Name=steel)	=	235,00 N/mm ²
f_u =	TAB("steel/EC"; f_u ; Name=steel)	=	360,00 N/mm ²
Profil Typ =	SEL("steel/Profils"; Name;)	=	IPE
Selected Profil =	SEL("steel/"Typ; Name;)	=	IPE 360
Column height h =	TAB("steel/"Typ; h; Name=Profil)	=	360,00 mm
Web thickness s =	TAB("steel/"Typ; s; Name=Profil)	=	8,00 mm
γ_{Mb} =	1,25		
γ_{M0} =	1,10		

Loads:

$$V_{sd} = 58,70 \text{ kN}$$

Limit shear force of section:

A_v =	$1,04 \cdot h \cdot s / 100$	=	29,95 cm ²
$V_{pl,Rdp}$ =	$A_v \cdot f_y / 10 / \sqrt{3} / \gamma_{M0}$	=	369,41 kN
$A_{v,net}$ =	$A_v - (n \cdot s \cdot d_2) / 100$	=	22,91

$$f_y / f_u \cdot A_v / A_{v,net} = 0,85 < 1$$

⇒ Holes can be neglected.

Joint with shear failure as in Bild 6.5.5:

$$\begin{aligned}
 L_v &= (n - 1) * a_2 &= & 210,00 \text{ mm} \\
 L_1 &= a_1 &= & 43,00 \text{ mm} \\
 L_1 / (5 * d_{l2}) & &= & 0,39 < 1 \\
 L_2 &= (a - k * d_{l2}) * f_u / f_y &= & 59,74 \text{ mm} \\
 L_3 &= L_v + a_1 + a_3 &= & 328,00 \text{ mm} \\
 L_{v,eff} &= L_v + L_1 + L_2 &= & 312,74 \text{ mm} \\
 L_{v,eff} / L_3 & &= & 0,95 < 1 \\
 L_3 / (L_v + a_1 + a_3 - n + d_{l2}) & &= & 0,95 < 1
 \end{aligned}$$

Effective shear area:

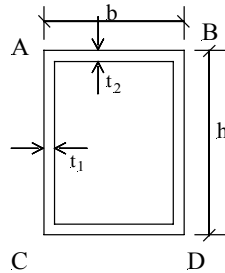
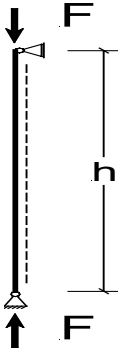
$$\begin{aligned}
 A_{v,eff} &= L_{v,eff} * s / 100 &= & 25,02 \text{ cm}^2 \\
 V_{pl,Rd} &= A_{v,eff} * f_y / 10 / \sqrt{3} / \gamma_{M0} &= & 308,60 \text{ kN}
 \end{aligned}$$

Maximum design force for shear:

$$V_{Rd} = \text{MIN}(V_{pl,Rdp}, V_{pl,Rd}) = \underline{\underline{308,60 \text{ kN}}}$$

Columns

Column of section class 4:



Load diagram:

Column height H =	6,50 m
Beam width b =	50,00 cm
Column height h =	100,00 cm
Web thickness t_1 =	1,00 cm
Flange thickness t_2 =	1,00 cm

Loads:

N_d =	3500,00 kN
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Materials and stresses:

steel =	SEL("steel/EC"; Name;)	=	Fe 360
f_y =	TAB("steel/EC"; f_y ; Name=steel)	=	235,00 N/mm ²
E =	TAB("steel/EC"; E; Name=steel)	=	210000,00 N/mm ²
ϵ =	$\sqrt{(235 / f_y)}$	=	1,00

Partial safety factors:

γ_M =	1,10
γ_g =	1,35

Section classification:

As in Table 5.3.1			
b' =	$b - 2 * t_1$	=	48,00 cm
$b' / t_2 / (42 * \epsilon)$		=	1,14 > 1
Section class 4			
h' =	$h - 2 * t_2$	=	98,00 cm
$h' / t_1 / (42 * \epsilon)$		=	2,33 > 1
Section class 4			

Effective web area:

Part A-B; C-D As in Table 5.3.2:

$$\begin{aligned} \psi &= 1,00 \\ k_{\sigma} &= 4,00 \\ \text{as in 5.3.5(3)} \\ \lambda_{\text{trans,p}} &= b' / t_2 / (28,4 * \epsilon * \sqrt{k_{\sigma}}) = 0,85 > 0,673 \\ \rho &= (\lambda_{\text{trans,p}} - 0,22) / \lambda_{\text{trans,p}}^2 = 0,872 \\ b_{\text{eff}} &= \rho * b' = 41,86 \text{ cm} \end{aligned}$$

Part A-C; B-D As in Table 5.3.2:

$$\begin{aligned} \psi &= 1,00 \text{ cm} \\ k_{\sigma} &= 4,00 \\ \text{as in 5.3.5(3)} \\ \lambda_{\text{trans,p}} &= h' / t_1 / (28,4 * \epsilon * \sqrt{k_{\sigma}}) = 1,73 > 0,673 \\ \rho &= (\lambda_{\text{trans,p}} - 0,22) / \lambda_{\text{trans,p}}^2 = 0,505 \\ h_{\text{eff}} &= \rho * h' = 49,49 \text{ cm} \end{aligned}$$

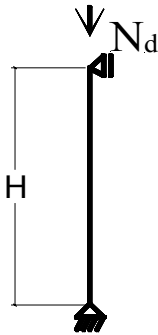
Check buckling:

$$\begin{aligned} A_{\text{eff}} &= 2 * (h_{\text{eff}} * t_1 + b_{\text{eff}} * t_2) + 4 * t_1 * t_2 = 186,70 \text{ cm}^2 \\ A &= b * h - (b - 2 * t_1) * (h - 2 * t_2) = 296,00 \text{ cm}^2 \\ \beta_A &= A_{\text{eff}} / A = 0,631 \\ I_b &= (b * h^3 - (b - 2 * t_1) * (h - 2 * t_2)^3) / 12 = 401898,67 \text{ cm}^4 \\ I_h &= (b^3 * h - (b - 2 * t_1)^3 * (h - 2 * t_2)) / 12 = 138498,67 \text{ cm}^4 \\ I &= \text{MIN}(I_b; I_h) = 138498,67 \text{ cm}^4 \\ N_{\text{cr}} &= \pi^2 * E / 10 * I / (H * 100)^2 = 67941,82 \text{ kN} \\ \lambda_{\text{trans}} &= \sqrt{\beta_A * A * f_y / 10 / N_{\text{cr}}} = 0,25 \end{aligned}$$

Apply strut curve b

$$\begin{aligned} \alpha &= 0,34 \\ \varphi &= 0,5 * (1 + \alpha * (\lambda_{\text{trans}} - 0,2) + \lambda_{\text{trans}}^2) = 0,540 \\ \chi &= 1 / (\varphi + (\varphi^2 - \lambda_{\text{trans}}^2)^{0,5}) = 0,9817 \\ N_{b,Rd} &= \chi * \beta_A * A * f_y / 10 / \gamma_M = 3917,19 \text{ kN} \end{aligned}$$

$$N_d / N_{b,Rd} = \underline{\underline{0,893 < 1}}$$

Column subject to compression force:

Column height $H =$				7,50 m
$l_y =$	$H/2 =$			3,75 m
$l_z =$	$H/3 =$			2,50 m

Materials and stresses:

steel =	SEL("steel/EC"; Name;)	=	Fe 430
$f_y =$	TAB("steel/EC"; f_y ; Name=steel)	=	275,00 N/mm ²
$E =$	TAB("steel/EC"; E ; Name=steel)	=	210000,00 N/mm ²
$\epsilon =$	$\sqrt{(235 / f_y)}$	=	0,92

Profil:

Profil Typ =	SEL("steel/Profils"; Name;)	=	IPE
Selected Profil =	SEL("steel/"Typ; Name;)	=	IPE 300
Cross-sectional area $A =$	TAB("steel/"Typ; A ; Name=Profil)	=	53,80 cm ²
Column height $h =$	TAB("steel/"Typ; h ; Name=Profil)	=	300,00 mm
Depth of web $h_1 =$	TAB("steel/"Typ; h_1 ; Name=Profil)	=	248,00 mm
Web thickness $s =$	TAB("steel/"Typ; s ; Name=Profil)	=	7,10 mm
Flange width $b =$	TAB("steel/"Typ; b ; Name=Profil)	=	150,00 mm
Flange thickness $t =$	TAB("steel/"Typ; t ; Name=Profil)	=	10,70 mm
Radius of gyration $i_y =$	TAB("steel/"Typ; i_y ; Name=Profil)	=	12,50 cm
Radius of gyration $i_z =$	TAB("steel/"Typ; i_z ; Name=Profil)	=	3,35 cm

Section classification As in Table 5.3.1:**Web:**

$$(h_1 / s) / (33 * \epsilon) = 1,15 < 1$$

$$(h_1 / s) / (38 * \epsilon) = 1,00 < 1$$

Section class 2.

Flange:

$$(b / 2 / t) / (10 * \epsilon) = 0,76 < 1$$

Section class 1.

Section will be classified as class 2.

Analysis:

nach 5.5.1.1 (1) $\beta_A =$ 1,00 Cross-section class 2

nach 5.1.1 (2) $\gamma_{M1} =$ 1,10 Cross-section class 2

Check buckling In Y-Y Axis:

$h / b = 2,00 > 1,2$

$t / 10 = 1,07 \text{ cm} < 4 \text{ cm}$

as in Tab 5.5.3 :

$\lambda_y = i_y * 100 / i_y = 30,00$

$\lambda_1 = 93,9 * \epsilon = 86,39$

$\lambda_{trans,y} = \lambda_y / \lambda_1 * \sqrt{\beta_A} = 0,347$

Apply strut curve a

As in Table 5.5.1 $\alpha = 0,21$

$\varphi = 0,5 * (1 + \alpha * (\lambda_{trans,y} - 0,2) + \lambda_{trans,y}^2) = 0,576$

$\chi = 1 / (\varphi + (\varphi^2 - \lambda_{trans,y}^2)^{0,5}) = 0,9655$

$N_{b,y,Rd} = \chi * \beta_A * A * f_y / 10 / \gamma_{M1} = 1298,60 \text{ kN}$

Check buckling In Z-Z Axis:

$h / b = 2,00 > 1,2$

$t / 10 = 1,07 \text{ cm} < 4 \text{ cm}$

as in Tab 5.5.3 :

$\lambda_z = i_z * 100 / i_z = 74,63$

$\lambda_{trans,z} = \lambda_z / \lambda_1 * \sqrt{\beta_A} = 0,864$

Apply strut curve b

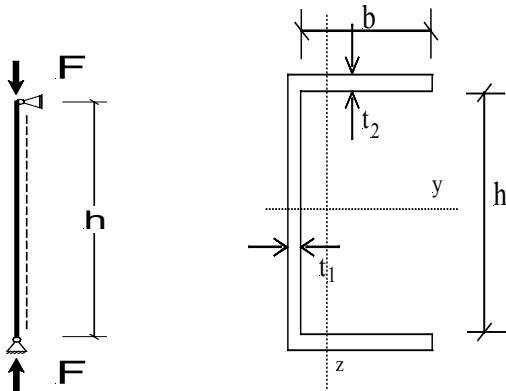
As in Table 5.5.1 $\alpha = 0,34$

$\varphi = 0,5 * (1 + \alpha * (\lambda_{trans,z} - 0,2) + \lambda_{trans,z}^2) = 0,986$

$\chi = 1 / (\varphi + (\varphi^2 - \lambda_{trans,z}^2)^{0,5}) = 0,6844$

$N_{b,z,Rd} = \chi * \beta_A * A * f_y / 10 / \gamma_{M1} = 920,52 \text{ kN}$

$\max_N_d = \text{MIN}(N_{b,y,Rd}; N_{b,z,Rd}) = \underline{\underline{920,52 \text{ kN}}}$

Column of section class 4:**Load diagram:**

Column height $H =$	4,00 kN
Flange width $b =$	20,00 cm
Depth of web $h =$	30,00 cm
Web thickness $t_1 =$	1,20 cm
Flange thickness $t_2 =$	1,20 cm

Loads:

$N_d =$	700,00 kN
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Materials and stresses:

steel =	SEL("steel/EC"; Name;)	=	Fe 360
$f_y =$	TAB("steel/EC"; f_y ; Name=steel)	=	235,00 N/mm ²
$E =$	TAB("steel/EC"; E ; Name=steel)	=	210000,00 N/mm ²
$\epsilon =$	$\sqrt{(235 / f_y)}$	=	1,00
$\lambda_1 =$	$93,90 * \epsilon$	=	93,90
Partial safety factors:			
$\gamma_M =$			1,10

Section classification As in Table 5.3.1:

$b / t_2 / (14 * \epsilon)$	=	1,19 > 1
Section class 4		
$h / t_1 / (33 * \epsilon)$	=	0,76 > 1
Section class 1		

Effective web area:**Flange:**

As in Table 5.3.3:

$$\psi = 1,00$$

$$k_{\sigma} = 0,43$$

as in 5.3.5(3)

$$\lambda_{trans,p} = b / t_2 / (28,4 * \epsilon * \sqrt{k_{\sigma}}) = 0,89 > 0,673$$

$$\rho = (\lambda_{trans,p} - 0,22) / \lambda_{trans,p}^2 = 0,846$$

$$b_{eff} = \rho * b = 16,92 \text{ cm}$$

$$A_{eff} = 2 * (b_{eff} * t_2) + (h + 2 * t_2) * t_1 = 79,49 \text{ cm}^2$$

Location of shear centre:

$$y_{s,eff} = (b_{eff} * (2 * t_2) * (b_{eff} + t_2) / 2) / A_{eff} = 4,628 \text{ cm}$$

$$b_{eff}^3 / 12 * (2 * t_2) + b_{eff} * (2 * t_2) * ((b_{eff} + t_1) / 2 - y_{s,eff})^2 = 1766,44 \text{ cm}^4$$

$$(h + 2 * t_2) * t_1^3 / 12 + (h + 2 * t_2) * t_1 * y_{s,eff}^2 = 837,41 \text{ cm}^4$$

$$I_{z,eff} = 2603,85 \text{ cm}^4$$

$$W_{z,eff} = I_{z,eff} / ((b_{eff} + t_1) - y_{s,eff} - (t_1 / 2)) = 201,97 \text{ cm}^3$$

Gross area:

$$A = b * 2 * t_2 + (h + 2 * t_2) * t_1 = 86,88 \text{ cm}^2$$

Location of center of gravity:

$$y_s = (b * 2 * t_2 * (b + t_1) / 2) / A = 5,856 \text{ cm}$$

$$I_z = b^3 / 12 * 2 * t_2 + b * 2 * t_2 * ((b + t_1) / 2 - y_s)^2 + (h + 2 * t_2) * t_1^3 / 12 + (h + 2 * t_2) * t_1 * y_s^2 = 4018,23 \text{ cm}^4$$

$$e_{Nz} = y_s - y_{s,eff} = 1,228 \text{ cm}$$

Check buckling:

$$N_{cr} = \pi^2 * E / 10 * I_z / (H * 100)^2 = 5205,15 \text{ kN}$$

$$\beta_A = A_{eff} / A = 0,915$$

$$\lambda_{trans,z} = \sqrt{(\beta_A * A * f_y / 10 / N_{cr})} = 0,60$$

Apply strut curve c As in Table 5.5.3

$$\alpha = 0,49$$

$$\varphi = 0,5 * (1 + \alpha * (\lambda_{trans,z} - 0,2) + \lambda_{trans,z}^2) = 0,778$$

$$\chi = 1 / (\varphi + (\varphi^2 - \lambda_{trans,z}^2)^{0,5}) = 0,7854$$

$$M_z = N_d * e_{Nz} / 100 = 8,60 \text{ kNm}$$

$$\psi = 1,00$$

$$\beta_{M\psi} = 1,8 - 0,7 * \psi = 1,10$$

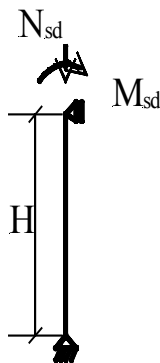
$$\mu_z = \lambda_{trans,z} * (2 * \beta_{M\psi} - 4) = -1,080 < 0,9$$

$$k_{z1} = 1 - (\mu_z * N_d) / (\chi * A_{eff} * f_y / 10) = 1,515 \sim 1,5$$

$$k_{z2} = 1,500$$

$$k_z = \text{MIN}(k_{z1}; k_{z2}) = 1,500$$

$$N_d / (\chi * A_{eff} * f_y / 10 / \gamma_M) + 100 * k_z * M_z / (W_{z,eff} * f_y / 10 / \gamma_M) = \underline{\underline{0,824 < 1}}$$

Column with compression and moment:**Load diagram:**

Column height $H = 5,00$ m

Loads:

$N_{sd} = 200,00$ kN
 $M_{y, sd} = 10,00$ kN

Materials and stresses:

steel = SEL("steel/EC"; Name;) = Fe 360
 $f_y =$ TAB("steel/EC"; f_y ; Name=steel) = 235,00 N/mm²
 $E =$ TAB("steel/EC"; E; Name=steel) = 210000,00 N/mm²
 $G =$ TAB("steel/EC"; G; Name=steel) = 81000,00 N/mm²
 $\epsilon =$ $\sqrt{(235 / f_y)}$ = 1,00

Partial safety factors:

$\gamma_M = 1,10$
 $\gamma_g = 1,35$
 platischer Formbeiwert $\alpha_{ply} = 1,14$
 platischer Formbeiwert $\alpha_{plz} = 1,25$

Profil:

Profil Typ = SEL("steel/Profils"; Name;) = HEA
 Selected Profil = SEL("steel/"Typ; Name;) = HEA 160
 Cross-sectional area $A =$ TAB("steel/"Typ; A; Name=Profil) = 38,80 cm²
 Column height $h =$ TAB("steel/"Typ; h; Name=Profil) = 152,00 mm
 Depth of web $h_1 =$ TAB("steel/"Typ; h1; Name=Profil) = 104,00 mm
 Web thickness $s =$ TAB("steel/"Typ; s; Name=Profil) = 6,00 mm
 Flange width $b =$ TAB("steel/"Typ; b; Name=Profil) = 160,00 mm
 Flange thickness $t =$ TAB("steel/"Typ; t; Name=Profil) = 9,00 mm
 Radius of gyration $i_y =$ TAB("steel/"Typ; iy; Name=Profil) = 6,57 cm
 Radius of gyration $i_z =$ TAB("steel/"Typ; iz; Name=Profil) = 3,98 cm
 $W_{ely} =$ TAB("steel/"Typ; Wy; Name=Profil) = 220,00 cm³
 $W_{ply} =$ $\alpha_{ply} * W_{ely}$ = 250,80 cm³
 $W_{elz} =$ TAB("steel/"Typ; Wz; Name=Profil) = 76,90 cm³
 $W_{plz} =$ $\alpha_{plz} * W_{elz}$ = 96,13 cm³

Section classification As in Table5.3.1:

Web will be assumed as pressed in

$$(h_1 / s) / (33 * \epsilon) = 0,53 < 1$$

Section class 1.

Flange:

$$(b / 2 / t) / (10 * \epsilon) = 0,89 < 1$$

Section class 1.

Check bending and buckling:

$$\text{as in 5.5.1.1 (1) } \beta_A = 1,00 \text{ Cross-section class 1}$$

$$\text{as in 5.1.1 (2) } \gamma_{M1} = 1,10 \text{ Cross-section class 1}$$

$$\lambda_y = H * 100 / i_y = 76,10$$

$$\lambda_1 = 93,9 * \epsilon = 93,90$$

$$\lambda_{trans,y} = \lambda_y / \lambda_1 * \sqrt{\beta_A} = 0,810$$

$$\lambda_z = 100 * H / i_z = 125,63$$

$$\lambda_{trans,z} = \lambda_z / (\pi * \sqrt{E / f_y}) = 1,34$$

As in Table 5.5.3

$$h / b = 0,95 < 1,2$$

$$t / 10 = 0,90 \text{ cm} < 10 \text{ cm}$$

As in Table:5.5.1

Strut curve b for Y-Y axis

$$\alpha = 0,34$$

$$\varphi = 0,5 * (1 + \alpha * (\lambda_{trans,y} - 0,2) + \lambda_{trans,y}^2) = 0,932$$

$$\chi_y = 1 / (\varphi + (\varphi^2 - \lambda_{trans,y}^2)^{0,5}) = 0,7179$$

Apply strut curve c for z-Achse

$$\alpha = 0,49$$

$$\varphi = 0,5 * (1 + \alpha * (\lambda_{trans,z} - 0,2) + \lambda_{trans,z}^2) = 1,677$$

$$\chi_z = 1 / (\varphi + (\varphi^2 - \lambda_{trans,z}^2)^{0,5}) = 0,3724$$

$$\psi = 0,00$$

$$\beta_{My} = 1,8 - 0,7 * \psi = 1,80$$

$$\mu_y = \lambda_{trans,y} * (2 * \beta_{My} - 4) + (W_{ply} - W_{ely}) / W_{ely} = -0,184 < 0,9$$

$$k_y = 1 - (\mu_y * N_{sd}) / (\chi_y * A * f_y) = 1,006 < 1,5$$

$$\chi = \text{MIN}(\chi_y; \chi_z) = 0,372$$

$$N_{sd} / (\chi * A * f_y / 10 / \gamma_M) + 100 * k_y * M_{y,sd} / (W_{ply} * f_y / 10 / \gamma_M) = \underline{0,836 < 1}$$

Check torsional-flexural buckling:

$$\beta_w = 1,00 \text{ Cross-section class 1}$$

As in Table: F.1.1

$$\psi = 0,00$$

$$k = 1,00$$

$$C_1 = 1,879$$

$$\lambda_{LT} = 90 * H / i_z / ((C_1)^{0,5} * (1 + 1 / 20 * ((100 * H / i_z) / (h / t))^2)^{0,25}) = 59,208$$

$$\lambda_{trans,LT} = \lambda_{LT} / \lambda_1 * \sqrt{\beta_w} = 0,631$$

For rolled sections strut curve a

$$\alpha = 0,21$$

$$\varphi = 0,5 * (1 + \alpha * (\lambda_{trans,LT} - 0,2) + \lambda_{trans,LT}^2) = 0,74$$

$$\chi_{LT} = 1 / (\varphi + (\varphi^2 - \lambda_{trans,LT}^2)^{0,5}) = 0,89$$

$$\beta_{M,LT} = 1,8 - 0,7 * \psi = 1,80$$

$$\lambda_{trans,z} = \lambda_z / \lambda_1 * \sqrt{\beta_A} = 1,338$$

$$\mu_{LT} = 0,15 * \lambda_{trans,z} * \beta_{M,LT} - 0,15 = 0,211 < 0,9$$

$$h / b = 0,95 < 1,2$$

$$t / 10 = 0,90 \text{ cm} < 10 \text{ cm}$$

Z-Z axis Strut curve c

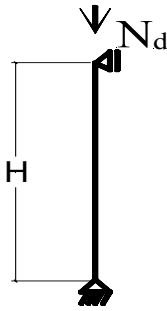
$$\alpha = 0,49$$

$$\varphi = 0,5 * (1 + \alpha * (\lambda_{trans,z} - 0,2) + \lambda_{trans,z}^2) = 1,674$$

$$\chi_z = 1 / (\varphi + (\varphi^2 - \lambda_{trans,z}^2)^{0,5}) = 0,3731$$

$$k_{LT} = 1 - (\mu_{LT} * N_{sd}) / (\chi_z * A * f_y) = 0,988 < 1,0$$

$$N_{sd} / (\chi_z * A * f_y / 10 / \gamma_M) + 100 * k_{LT} * M_{y,sd} / (\chi_{LT} * W_{ply} * f_y / 10 / \gamma_M) = \underline{0,854 < 1}$$

Column subject to compression force:

Column base is pinned.

For buckling, column head is pinned about the Y-Y axis, and fixed about the Z-Z axis .

Load diagram:

Column height $H = 8,00 \text{ m}$

Loads:

$N_d = 2000,00 \text{ kN}$

Materials and stresses:

steel =	SEL("steel/EC"; Name;)	=	Fe 360
$f_y =$	TAB("steel/EC"; f_y ; Name=steel)	=	235,00 N/mm ²
$E =$	TAB("steel/EC"; E; Name=steel)	=	210000,00 N/mm ²
$\epsilon =$	$\sqrt{(235 / f_y)}$	=	1,00

Effective length factor:

$k_y =$	1,00	For simply supported ends
$k_z =$	0,70	fixed ends

Profil:

Profil Typ =	SEL("steel/Profils"; Name;)	=	HEB
Selected Profil =	SEL("steel/"Typ; Name;)	=	HEB 300
Cross-sectional area $A =$	TAB("steel/"Typ; A; Name=Profil)	=	149,00 cm ²
Column height $h =$	TAB("steel/"Typ; h; Name=Profil)	=	300,00 mm
Depth of web $h_1 =$	TAB("steel/"Typ; h1; Name=Profil)	=	208,00 mm
Web thickness $s =$	TAB("steel/"Typ; s; Name=Profil)	=	11,00 mm
Flange width $b =$	TAB("steel/"Typ; b; Name=Profil)	=	300,00 mm
Flange thickness $t =$	TAB("steel/"Typ; t; Name=Profil)	=	19,00 mm
Moment of inertia $I =$	TAB("steel/"Typ; Iy; Name=Profil)	=	25170,00 cm ⁴
Radius of gyration $i_y =$	TAB("steel/"Typ; iy; Name=Profil)	=	13,00 cm
Radius of gyration $i_z =$	TAB("steel/"Typ; iz; Name=Profil)	=	7,58 cm

Section classification:**Web:**

$(h_1 / s) / (33 * \epsilon) = 0,57 < 1$

Flange:

$(b / 2 / t) / (10 * \epsilon) = 0,79 < 1$

Section class 1.

Analysis:

$$\beta_A = 1,00 \text{ Cross-section class 1}$$

$$\gamma_{M1} = 1,10 \text{ Cross-section class 1}$$

Check buckling In Y-Y Axis:

$$h / b = 1,00 < 1,2$$

$$t / 10 = 1,90 \text{ cm} < 10 \text{ cm}$$

$$\lambda_y = k_y * H * 100 / i_y = 61,54$$

$$\lambda_1 = 93,9 * \epsilon = 93,90$$

$$\lambda_{\text{trans,y}} = \lambda_y / \lambda_1 * \sqrt{\beta_A} = 0,655$$

Apply strut curve b

$$\text{As in Table 5.5.1 } \alpha = 0,34$$

$$\varphi = 0,5 * (1 + \alpha * (\lambda_{\text{trans,y}} - 0,2) + \lambda_{\text{trans,y}}^2) = 0,792$$

$$\chi = 1 / (\varphi + (\varphi^2 - \lambda_{\text{trans,y}}^2)^{0,5}) = 0,8083$$

$$N_{b,Rd} = \chi * \beta_A * A * f_y / 10 / \gamma_{M1} = 2572,97 \text{ kN}$$

$$N_d / N_{b,Rd} = \underline{\underline{0,78 < 1}}$$

Check buckling In Z-Z Axis:

$$h / b = 1,00 < 1,2$$

$$t / 10 = 1,90 \text{ cm} < 10 \text{ cm}$$

$$\lambda_z = k_z * H * 100 / i_z = 73,88 \text{ m}$$

$$\lambda_{\text{trans,z}} = \lambda_z / \lambda_1 * \sqrt{\beta_A} = 0,787$$

Apply strut curve c

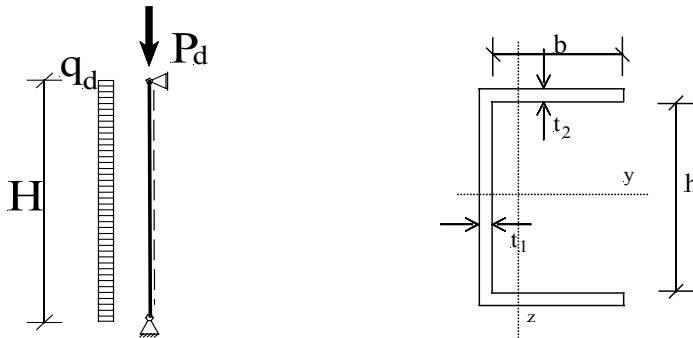
$$\text{As in Table 5.5.1 } \alpha = 0,49$$

$$\varphi = 0,5 * (1 + \alpha * (\lambda_{\text{trans,z}} - 0,2) + \lambda_{\text{trans,z}}^2) = 0,953$$

$$\chi = 1 / (\varphi + (\varphi^2 - \lambda_{\text{trans,z}}^2)^{0,5}) = 0,6709$$

$$N_{b,Rd} = \chi * \beta_A * A * f_y / 10 / \gamma_{M1} = 2135,60 \text{ kN}$$

$$N_d / N_{b,Rd} = \underline{\underline{0,94 < 1}}$$

Column of channel section with compression and transverse loads:**Load diagram:**

Column height H =	4,00 m
Beam width b =	9,50 cm
Depth of web h =	29,40 cm
Web thickness t_1 =	1,00 cm
Flange width t_2 =	0,60 cm

Loads:

q_d =	15,00 kN/m
N_d =	90,00 kN

Materials and stresses:

steel =	SEL("steel/EC"; Name;)	=	Fe 360
f_y =	TAB("steel/EC"; f_y ; Name=steel)	=	235,00 N/mm ²
E =	TAB("steel/EC"; E; Name=steel)	=	210000,00 N/mm ²
ϵ =	$\sqrt{(235 / f_y)}$	=	1,00
λ_1 =	$93,90 * \epsilon$	=	93,90
Partial safety factors:			
γ_M =		=	1,10

Section classification:

As in Table 5.3.1			
$b / t_2 / (14 * \epsilon)$	=	1,13 > 1	
Section class 4			
As in Table 5.3.2			
$h / t_1 / (33 * \epsilon)$	=	0,89 > 1	
Section class 1			
A =	$b * 2 * t_2 + (h + 2 * t_2) * t_1$	=	42,00 cm ²
Location of center of gravity:			
y_s =	$(b * 2 * t_2 * (b + t_1) / 2) / A$	=	1,425 cm
	$b^3 / 12 * 2 * t_2 + b * 2 * t_2 * ((b + t_1) / 2 - y_s)^2$	=	252,53 cm ⁴
	$(h + 2 * t_2) * t_1^3 / 12 + (h + 2 * t_2) * t_1 * y_s^2$	=	64,69 cm ⁴
		Iz =	317,22 cm ⁴
I_y =	$h^3 / 12 * t_1 + 2 * (b * t_2^3 / 12 + b * t_2 * ((h + t_2) / 2)^2)$	=	4683,02 cm ⁴
$W_{el,z}$ =	$I_z / (b + t_1 / 2 - y_s)$	=	36,99 cm ³
$W_{el,y}$ =	$I_y / ((h + t_1) / 2)$	=	308,09 cm ³

Effective web area:**Flangee:**

As in Table 5.3.3:

$$\psi = 1,00$$

$$k_{\sigma} = 0,43$$

as in 5.3.5(3)

$$\lambda_{\text{trans,p}} = b / t_2 / (28,4 * \epsilon * \sqrt{k_{\sigma}}) = 0,85 > 0,673$$

$$\rho = (\lambda_{\text{trans,p}} - 0,22) / \lambda_{\text{trans,p}}^2 = 0,872$$

$$b_{\text{eff}} = \rho * b = 8,28 \text{ cm}$$

$$A_{\text{eff}} = 2 * (b_{\text{eff}} * t_2) + (h + 2 * t_2) * t_1 = 40,54 \text{ cm}^2$$

Location of shear centre:

$$y_{s,\text{eff}} = (b_{\text{eff}} * (2 * t_2) * (b_{\text{eff}} + t_2) / 2) / A_{\text{eff}} = 1,088 \text{ cm}$$

$$e_{\text{Nz}} = y_s - y_{s,\text{eff}} = 0,337 \text{ cm}$$

$$\beta_A = A_{\text{eff}} / A = 0,965$$

Slenderness and reductions:**In Z-Z Axis:**

$$N_{\text{cr,z}} = \pi^2 * E * I_z / (H * 100)^2 = 4109,22 \text{ kN}$$

$$\lambda_{\text{trans,z}} = \sqrt{(\beta_A * A * f_y / N_{\text{cr,z}})} = 1,52$$

Apply strut curve c

$$\alpha = 0,49$$

$$\phi = 0,5 * (1 + \alpha * (\lambda_{\text{trans,z}} - 0,2) + \lambda_{\text{trans,z}}^2) = 1,979$$

$$\chi_z = 1 / (\phi + (\phi^2 - \lambda_{\text{trans,z}}^2)^{0,5}) = 0,3080$$

In Y-Y Axis:

$$N_{\text{cr,y}} = \pi^2 * E * I_y / (H * 100)^2 = 60663,06 \text{ kN}$$

$$\lambda_{\text{trans,y}} = \sqrt{(\beta_A * A * f_y / N_{\text{cr,y}})} = 0,40$$

Apply strut curve c

$$\alpha = 0,49$$

$$\phi = 0,5 * (1 + \alpha * (\lambda_{\text{trans,y}} - 0,2) + \lambda_{\text{trans,y}}^2) = 0,629$$

$$\chi_y = 1 / (\phi + (\phi^2 - \lambda_{\text{trans,y}}^2)^{0,5}) = 0,8973$$

$$\chi = \text{MIN}(\chi_z; \chi_y) = 0,3080$$

$$N_{\text{b,Rd}} = \chi * A_{\text{eff}} * f_y / \gamma_M = 2667,53 \text{ kN}$$

Limit bending moment about the Y-Y axis:

Cross-section class 4

$$z'_s = \frac{(-b_{\text{eff}} * t_2 * (h + t_2) / 2 + (b + (t_1 / 2)) * t_2 * (h + t_2) / 2)}{A_{\text{eff}}} = 0,382 \text{ cm}$$

$$(h + t_2)^3 / 12 * t_1 + (h + t_2) * t_1 * z'_s = 2261,46 \text{ cm}^4$$

$$b_{\text{eff}} * t_2 * ((h + t_2) / 2 + z'_s)^2 + (b + (t_1 / 2)) * t_2 * ((h + t_2) / 2 - z'_s)^2 = 2457,57 \text{ cm}^4$$

$$I_{\text{eff},y} = 4719,03 \text{ cm}^4$$

$$W_{\text{eff},y} = I_{\text{eff},y} / ((h + t_2) / 2 + z'_s) = 306,79 \text{ cm}^3$$

$$M_{c,Rd,y} = W_{\text{eff},y} * f_y / \gamma_M = 65541,50 \text{ kNm}$$

Limit bending moment about the Z-Z axis:

Cross-section class 4 Tab 5.3.3

$$\psi = -y_s / (b + (t_1 / 2) - y_s) = -0,17$$

$$k_{\sigma} = 0,57 - 0,21 * \psi + 0,07 * \psi^2 = 0,61$$

$$(b + (t_1 / 2)) / t_2 / (21 * \epsilon * \sqrt{k_{\sigma}}) = 1,02 > 1$$

As in Table:5.3.5 (3)

$$\lambda_{\text{trans},p} = (b + (t_1 / 2)) / t_2 / (28,4 * \epsilon * \sqrt{k_{\sigma}}) = 0,75 > 0,673$$

$$\rho = (\lambda_{\text{trans},p} - 0,22) / \lambda_{\text{trans},p}^2 = 0,942$$

$$b_{\text{eff}} = \rho * (b + (t_1 / 2)) / (1 - \psi) = 8,05 \text{ cm}$$

$$b_t = -(b + (t_1 / 2)) * \psi / (1 - \psi) = 1,45 \text{ cm}$$

$$c_{\text{eff}} = b_{\text{eff}} + b_t = 9,50 \text{ cm}$$

$$A_{\text{eff}} = (h + t_2) * t_1 + 2 * c_{\text{eff}} * t_2 = 41,40 \text{ cm}^2$$

$$y' = 2 * c_{\text{eff}}^2 * t_2 / 2 / A_{\text{eff}} = 1,31 \text{ cm}$$

$$I_{\text{eff},z} = (h + t_2) * t_1 * y'^2 + 2 * c_{\text{eff}}^3 / 12 * t_2 + 2 * c_{\text{eff}} * t_2 * (c_{\text{eff}} / 2 - y')^2 = 272,12 \text{ cm}^4$$

$$W_{\text{eff},z} = I_{\text{eff},z} / (c_{\text{eff}} / 2 - y') = 79,10 \text{ cm}^3$$

$$M_{c,Rd,z} = W_{\text{eff},z} * f_y / \gamma_M = 16898,64 \text{ kNm}$$

Check buckling:

$$N_{sd} = N_d = 90,00 \text{ kN}$$

$$M_{y,sd} = q_d * H^2 / 8 = 30,00 \text{ kNm}$$

$$M_{z,sd} = N_d * e_{Nz} / 100 = 0,30 \text{ kNm}$$

Hilfsbeiwerte:

$$\beta_{My} = 1,30$$

$$\mu_y = \lambda_{\text{trans},y} * (2 * \beta_{My} - 4) = -0,560 < 0,9$$

$$k_y = 1 - (\mu_y * N_{sd}) / (\chi_y * A_{\text{eff}} * f_y) = 1,006 < 1,5$$

$$\psi = 1,000$$

$$\beta_{M\psi} = 1,8 - 0,7 * \psi = 1,10 < 1,5$$

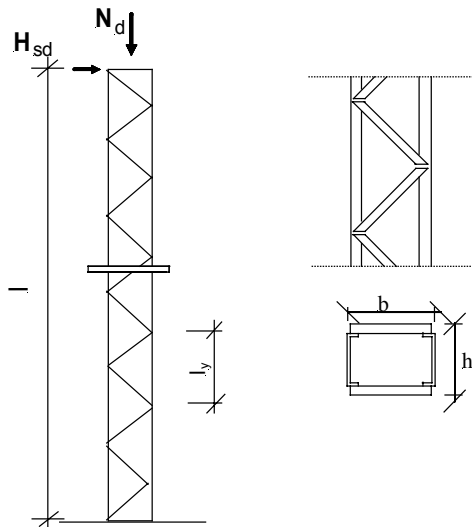
$$\mu_z = \lambda_{\text{trans},z} * (2 * \beta_{M\psi} - 4) = -2,736 < 0,9$$

$$k_{z1} = 1 - (\mu_z * N_{sd}) / (\chi * A_{\text{eff}} * f_y) = 1,082$$

$$k_{z2} = 1,500$$

$$k_z = \text{MIN}(k_{z1}; k_{z2}) = 1,082$$

$$N_{sd} / (\chi * A_{\text{eff}} * f_y / \gamma_M) + k_y * 100 * M_{y,sd} / (W_{\text{eff},y} * f_y / \gamma_M) + k_z * 100 * M_{z,sd} / (W_{\text{eff},z} * f_y / \gamma_M) = \underline{\underline{0,081 < 1}}$$

Laced column made up of channel and angle sections:**Loads:**

$N_{sd} =$	300,00 kN
$H_{sd} =$	45,00 kN

Plan and elevation values:

Span length $l_y =$	69,20 cm
Column height $l =$	$10 \cdot l_y / 100 = 6,92$ m
Width $b =$	40,00 cm
Winkel $\phi_1 =$	45,00 °

U-Profil U =	SEL("steel/U"; Name;)	=	U 300
$A_f =$	TAB("steel/U"; A; Name=U)	=	58,80 cm ²
$e_z =$	TAB("steel/U"; ez; Name=U)	=	2,70 cm
$i_z =$	TAB("steel/U"; iz; Name=U)	=	2,90 cm

Winkel W =	SEL("steel/WG"; Name;)	=	L 50x5
Angle thickness $A_D =$	TAB("steel/WG"; A; Name=W)	=	4,80 cm ²
Angle thickness $i_\zeta =$	TAB("steel/WG"; i ζ ; Name=W)	=	0,98 cm

steel =	SEL("steel/EC"; Name;)	=	Fe 360
$f_y =$	TAB("steel/EC"; fy; Name=steel)	=	235,00 N/mm ²
$E =$	TAB("steel/EC"; E; Name=steel)	=	210000,00 N/mm ²

$\epsilon =$	$\sqrt{(235 / f_y)}$	=	1,00
$\lambda_1 =$	$93,90 \cdot \epsilon$	=	93,90

Partial safety factors:

$\gamma_M =$	1,10
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Maximal tension force in chord:

$$\begin{aligned} \text{Effective length ratio } k &= 2,00 \\ \text{Imperfection:} \\ w_o &= 2 * l / 5 = 2,77 \text{ cm} \\ \text{Effective moment of inertia:} \\ h_o &= b - 2 * e_z = 34,60 \text{ cm} \\ I_{\text{eff}} &= 0,5 * h_o^2 * A_f = 35196,50 \text{ cm}^4 \\ \text{Shear strength:} \\ S_v &= 2 * E / 10 * A_D * I_y * h_o^2 / (2 * \sqrt{(2 * h_o^2)^3}) = 71276,36 \text{ kN} \\ N_{\text{cr}} &= 1 / ((4 * (100 * l)^2 / (\pi^2 * E / 10 * I_{\text{eff}})) + (1 / S_v)) = 3615,26 \text{ kN} \\ \text{max_M}_s &= H_{\text{sd}} * l + N_{\text{sd}} / (1 - N_{\text{sd}} / N_{\text{cr}}) * w_o / 100 = 320,46 \text{ kNm} \\ N_{\text{f,sd}} &= 0,5 * N_{\text{sd}} + 100 * \text{max_M}_s / h_o = 1076,18 \text{ kN} \end{aligned}$$

Analysis of channels:

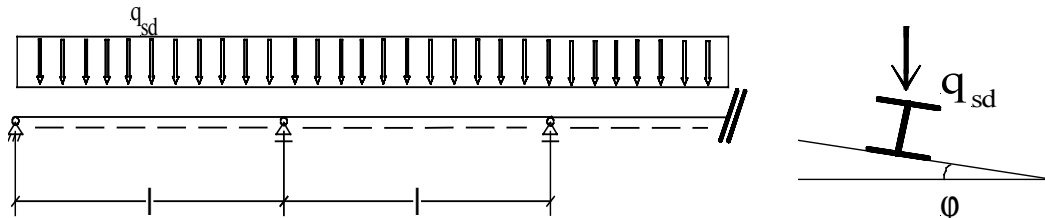
$$\begin{aligned} \lambda &= l_y / i_z = 23,86 \\ \lambda_{\text{trans}} &= \lambda / (\lambda_1 * \epsilon) = 0,254 \\ \text{Apply strut curve c} \\ \alpha &= 0,49 \\ \phi &= 0,5 * (1 + \alpha * (\lambda_{\text{trans}} - 0,2) + \lambda_{\text{trans}}^2) = 0,545 \\ \chi &= 1 / (\phi + (\phi^2 - \lambda_{\text{trans}}^2)^{0,5}) = 0,9735 \\ N_{\text{b,Rd}} &= \chi * A_f * f_y / 10 / \gamma_M = 1222,89 \text{ kN} \\ N_{\text{f,sd}} / N_{\text{b,Rd}} &= \underline{\underline{0,88 < 1}} \end{aligned}$$

Analysis of lacing angles:

$$\begin{aligned} \text{max_V}_s &= H_{\text{sd}} + N_{\text{sd}} / (1 - N_{\text{sd}} / N_{\text{cr}}) * w_o * \pi / (200 * l) = 47,06 \text{ kN} \\ \text{Design force for a diagonal:} \\ N_{\text{dS}} &= \text{max_V}_s / (2 * \text{COS}(\phi_1)) = 33,28 \text{ kN} \\ \lambda &= \sqrt{(2 * h_o^2) / i_\zeta} = 49,93 \\ \lambda_{\text{trans}} &= \lambda / (\lambda_1 * \epsilon) = 0,532 \\ \text{Apply strut curve c} \\ \alpha &= 0,49 \\ \phi &= 0,5 * (1 + \alpha * (\lambda_{\text{trans}} - 0,2) + \lambda_{\text{trans}}^2) = 0,723 \\ \chi &= 1 / (\phi + (\phi^2 - \lambda_{\text{trans}}^2)^{0,5}) = 0,8247 \\ N_{\text{b,Rd}} &= \chi * A_D * f_y / 10 / \gamma_M = 84,57 \text{ kN} \\ N_{\text{dS}} / N_{\text{b,Rd}} &= \underline{\underline{0,39 < 1}} \end{aligned}$$

Continuous Beam

Purlin / Strut with biaxial bending and torsional-flexural buckling:



Plan and elevation values:

Span length l=	720,00 cm
Angle of slope ϕ =	10,00 °
Spacing of purlin l'=	4,00 m
platischer Formbeiwert α_{ply} =	1,14
platischer Formbeiwert α_{plz} =	1,25

Loads:

From dead load g=	0,20 kN/m ²
From snow load s=	0,40 kN/m ²

Section classification for: IPE 200

Profil Typ =	SEL("steel/Profils"; Name;)	=	IPE
Selected Profil =	SEL("steel/"Typ; Name;)	=	IPE 200
Column height h =	TAB("steel/"Typ; h; Name=Profil)	=	200,00 mm
Flange width b _f =	TAB("steel/"Typ; b; Name=Profil)	=	100,00 mm
Flange thickness t _f =	TAB("steel/"Typ; t; Name=Profil)	=	8,50 mm
Flange thickness t _w =	TAB("steel/"Typ; s; Name=Profil)	=	5,60 mm
Moment of inertia I _y =	TAB("steel/"Typ; Iy; Name=Profil)	=	1940,00 cm ⁴
Moment of inertia I _z =	TAB("steel/"Typ; Iz; Name=Profil)	=	142,00 cm ⁴
Moment of inertia I _y =	TAB("steel/"Typ; IT; Name=Profil)	=	6,98 cm ⁴
I _ω =	t _f * b _f ³ * (h - t _f) ² / (24*10 ⁶)	=	12988,09 cm ⁶
i _z =	TAB("steel/"Typ; iz; Name=Profil)	=	2,24 cm
W _{ely} =	TAB("steel/"Typ; Wy; Name=Profil)	=	194,00 cm ³
W _{ply} =	$\alpha_{ply} * W_{ely}$	=	221,16 cm ³
W _{elz} =	TAB("steel/"Typ; Wz; Name=Profil)	=	28,50 cm ³

Materials and stresses:

steel =	SEL("steel/EC"; Name;)	=	Fe 360
E _s =	TAB("steel/EC"; E; Name=steel)	=	210000,00 N/mm ²
G =	TAB("steel/EC"; G; Name=steel)	=	81000,00 N/mm ²
f _y =	TAB("steel/EC"; fy; Name=steel)	=	235,00 N/mm ²

$$\varepsilon = \sqrt{(235/f_y)} = 1,00$$

Partial safety factors:

γ_M =	1,10
γ_g =	1,35
γ_p =	1,50

Design calculations:

$$\begin{aligned} \text{Factored load } p_d &= \gamma_g * g + \gamma_p * s &= & 0,87 \text{ kN/m}^2 \\ \text{Effective load } q_d &= p_d * 4 &= & 3,48 \text{ kN/m} \\ \text{Vertical load component } q_{zd} &= q_d * \text{COS}(\varphi) &= & 3,43 \text{ kN/m} \\ \text{Horizontal load component } q_{yd} &= q_d * \text{SIN}(\varphi) &= & 0,60 \text{ kN/m} \end{aligned}$$

Forces at 2nd support:

$$\begin{aligned} M_{bysd} &= 0,105 * q_{zd} * (l / 100)^2 &= & 18,67 \text{ kNm} \\ M_{bzsd} &= 0,105 * q_{yd} * (l / 100)^2 &= & 3,27 \text{ kNm} \\ V_{bzsd} &= 0,606 * q_{zd} * l / 100 &= & 14,97 \text{ kN} \\ V_{bysd} &= 0,606 * q_{yd} * l / 100 &= & 2,62 \text{ kN} \end{aligned}$$

Check biaxial bending strength:**About Y-Y axis**

$$\begin{aligned} A_v &= 1,04 * h * t_w / 10^2 &= & 11,65 \text{ cm}^2 \\ V_{pl,z,Rd} &= A_v * f_y / (\gamma_M * \sqrt{(3) * 10}) &= & 143,69 \text{ kN} \\ V_{bzsd} / V_{pl,z,Rd} & &= & \underline{0,10 < 1} \\ V_{bysd} / V_{pl,z,Rd} & &= & \underline{0,10 < 0,5} \\ \Rightarrow & \text{No reduction in moment strength necessary due to shear.} \\ M_{pl,y,Rd} &= W_{ply} * f_y / \gamma_M / 10 &= & 4724,78 \text{ kNcm} \end{aligned}$$

About Z-Z axis

$$\begin{aligned} A_v &= 2 * b_f * t_f / 10^2 &= & 17,00 \text{ cm}^2 \\ V_{pl,y,Rd} &= A_v * f_y / (\gamma_M * \sqrt{(3) * 10}) &= & 209,68 \text{ kN} \\ V_{bysd} / V_{pl,y,Rd} & &= & \underline{0,01 < 1} \\ V_{bzsd} / V_{pl,y,Rd} & &= & \underline{0,01 < 0,5} \\ \Rightarrow & \text{No reduction in moment strength necessary due to shear} \\ M_{pl,z,Rd} &= 1,5 * W_{elz} * f_y / \gamma_M / 10 &= & 913,30 \text{ kNcm} \end{aligned}$$

Analysis:

as in 5.35: for I- and H- sections:

$$\alpha = 2,00$$

$$\beta = 1,00$$

Or else: 5.4.8.1 (11)

$$\text{ABS}((M_{bysd} / (M_{pl,y,Rd} / 10^2))^\alpha + (M_{bzsd} / (M_{pl,z,Rd} / 10^2))^\beta) = \underline{0,514 < 1}$$

Check flexural-torsional buckling strength:

$$i_{LT} = (I_z * I_\omega / W_{ply}^2)^{0,25} = 2,48 \text{ cm}$$

Load is applied in top flange.

$$z_a = 10,00 \text{ cm}$$

$$z_s = 0,00 \text{ cm}$$

$$z_g = z_a - z_s = 10,00 \text{ cm}$$

As in Table F.1.2, Werte interpoliert.

$$C_1 = 1,00$$

$$C_2 = 0,80$$

$$C_3 = 0,70$$

$$\text{For simply supported ends – fixed ends } k = 0,70$$

$$\text{No measures taken toward bending } k_w = 1,00$$

$$\begin{aligned}
 h_s &= (h - t_f) / 10 &= & 19,15 \text{ cm} \\
 5.5.2; \text{ Section class } 1+2 \beta_w &= &= & 1,00 \\
 \lambda_1 &= \pi \cdot \sqrt{(E_s / f_y)} &= & 93,91 \\
 \text{Auxilliary value } v &= ((k / k_w)^2 + 1/20 \cdot (k \cdot i_{LT} / (h/t_f))^2 + (2 \cdot C_2 \cdot z_g / h_s)^2) &= & 4,92 \\
 \lambda_{LT} &= k \cdot i_{LT} / ((C_1)^{0,5} \cdot (v^{0,5} - 2 \cdot C_2 \cdot z_g / h_s)^{0,5}) &= & 172,83 \\
 \lambda_{trans,LT} &= \lambda_{LT} / \lambda_1 \cdot \sqrt{\beta_w} &= & 1,840 \\
 \text{Apply strut curve a:} & & & \\
 \text{As in Table 5.5.1 } \alpha &= &= & 0,21 \\
 \varphi &= 0,5 \cdot (1 + \alpha \cdot (\lambda_{trans,LT}^{-0,2} + \lambda_{trans,LT}^2)) &= & 2,37 \\
 \chi_{LT} &= 1 / (\varphi + (\varphi^2 - \lambda_{trans,LT}^2)^{0,5}) &= & 0,26 \\
 \text{No longitudinal forces } k_z &= &= & 1,00 \\
 \text{No longitudinal forces } k_{LT} &= &= & 1,00
 \end{aligned}$$

$$k_{LT} \cdot M_{bysd} / (\chi_{LT} \cdot M_{pl,y,Rd} / 10^2) + k_z \cdot M_{bzs d} / (M_{pl,z,Rd} / 10^2) = \underline{1,88 < 1}$$

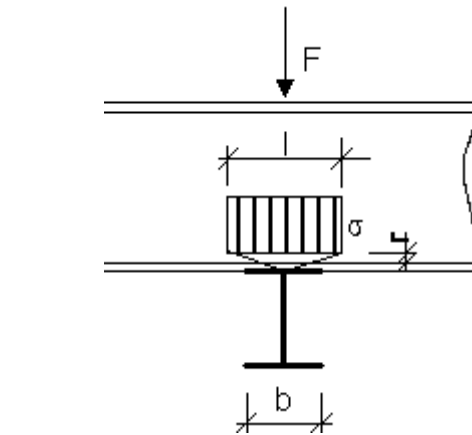
Section is not adequate: Restrain section in quarterly points:

$$\begin{aligned}
 l &= l / 4 &= & 180,00 \text{ cm} \\
 \text{Auxilliary value } v &= ((k/k_w)^2 + 1/20 \cdot (k \cdot i_{LT} / (h/t_f))^2 + (2 \cdot C_2 \cdot z_g / h_s)^2) &= & 1,42 \\
 \lambda_{LT} &= k \cdot i_{LT} / ((C_1)^{0,5} \cdot (v^{0,5} - 2 \cdot C_2 \cdot z_g / h_s)^{0,5}) &= & 85,14 \\
 \lambda_{trans,LT} &= \lambda_{LT} / \lambda_1 \cdot \sqrt{\beta_w} &= & 0,907 \\
 \text{Apply strut curve a:} & & & \\
 \varphi &= 0,5 \cdot (1 + \alpha \cdot (\lambda_{trans,LT}^{-0,2} + \lambda_{trans,LT}^2)) &= & 0,99 \\
 \chi_{LT} &= 1 / (\varphi + (\varphi^2 - \lambda_{trans,LT}^2)^{0,5}) &= & 0,72
 \end{aligned}$$

$$k_{LT} \cdot M_{bysd} / (\chi_{LT} \cdot M_{pl,y,Rd} / 10^2) + k_z \cdot M_{bzs d} / (M_{pl,z,Rd} / 10^2) = \underline{0,91 < 1}$$

foot and support

Concentrated point load of a beam in another beam:



Design loads and properties

$P_{sd} =$	68,00 kN
$M_{sd1} =$	70,00 kNm
$M_{sd2} =$	-22,00 kNm

Top beam (IPE180)

Profil TypO =	SEL("steel/Profils"; Name;)	=	IPE
Selected ProfilO =	SEL("steel/"TypO; Name;)	=	IPE 180
Web thickness $s_o =$	TAB("steel/"TypO; s; Name=ProfilO)	=	5,30 mm
Flange thickness $t_o =$	TAB("steel/"TypO; t; Name=ProfilO)	=	8,00 mm
Radius $r_o =$	TAB("steel/"TypO; r; Name=ProfilO)	=	9,00 mm
Flange width $b_o =$	TAB("steel/"TypO; b; Name=ProfilO)	=	91,00 mm
Web depth $h_o =$	TAB("steel/"TypO; h; Name=ProfilO)	=	180,00 mm
Web depth $h_{1o} =$	TAB("steel/"TypO; h1; Name=ProfilO)	=	146,00 mm
$W_{elo} =$	TAB("steel/"TypO; W_y ; Name=ProfilO)	=	146,00 cm ³
$W_{plo} =$	1,14 * W_{elo}	=	166,44 cm ³
$I_{yo} =$	TAB("steel/"TypO; I_y ; Name=ProfilO)	=	1320,00 cm ⁴

Bottom beam (HEA200)

Profil TypO =	SEL("steel/Profils"; Name;)	=	HEA
Selected ProfilO =	SEL("steel/"TypO; Name;)	=	HEA 200
Web thickness of beam $s_u =$	TAB("steel/"TypO; s; Name=ProfilO)	=	6,50 mm
Flange thickness $t_u =$	TAB("steel/"TypO; t; Name=ProfilO)	=	10,00 mm
Radius $r_u =$	TAB("steel/"TypO; r; Name=ProfilO)	=	18,00 mm
Flange width $b_u =$	TAB("steel/"TypO; b; Name=ProfilO)	=	200,00 mm
Web depth $h_u =$	TAB("steel/"TypO; h; Name=ProfilO)	=	190,00 mm
Web depth $h_{1u} =$	TAB("steel/"TypO; h1; Name=ProfilO)	=	134,00 mm
$W_{elu} =$	TAB("steel/"TypO; W_y ; Name=ProfilO)	=	389,00 cm ³
$W_{plu} =$	1,14 * W_{elu}	=	443,46 cm ³
$I_{yu} =$	TAB("steel/"TypO; I_y ; Name=ProfilO)	=	3690,00 cm ⁴

Materials and stresses:

steel =	SEL("steel/EC"; Name;)	=	Fe 360
E_s =	TAB("steel/EC"; E; Name=steel)	=	210000,00 N/mm ²
G =	TAB("steel/EC"; G; Name=steel)	=	81000,00 N/mm ²
f_y =	TAB("steel/EC"; fy; Name=steel)	=	235,00 N/mm ²
ϵ =	$\sqrt{(235 / f_y)}$	=	1,00
γ_M =		=	1,10
λ_1 =	$93,90 * \epsilon$	=	93,90
f_{yd} =	f_y / γ_M	=	213,64 kN/cm ²

Limit plastic bearing:**Stiff bearing length of top, bottom beam:**

s_{s1} =	$s_o + 2 * t_o + 4 * r_o * (1 - \sqrt{(2) / 2})$	=	31,84 mm
$\sigma_{f,Ed1}$ =	$100 * M_{sd1} / W_{el1}$	=	17,99 kN/cm ²
b_{f1} =	$t_u * 25$	=	250,00 mm
b_{f1} =	MIN(b_{f1} ; b_u)	=	200,00 mm
s_{y1} =	$2 * t_u * (b_u / s_u)^{0,5} * (1 - (\gamma_M * \sigma_{f,Ed1} / f_y * 10)^2)^{0,5}$	=	59,83 mm
$R_{y,Rd1}$ =	$(s_{s1} + s_{y1}) * s_u * f_y / \gamma_M / 10^3$	=	127,30 kN

$$P_{sd} / R_{y,Rd1} = \underline{\underline{0,53 < 1}}$$

Stiff bearing length of bottom beam:

s_{s2} =	$s_u + 2 * t_u + 4 * r_u * (1 - \sqrt{(2) / 2})$	=	47,59 mm
$\sigma_{f,Ed2}$ =	$100 * M_{sd2} / W_{el2}$	=	-15,07 kN/cm ²
b_f =	$t_o * 25$	=	200,00 mm
b_{f2} =	MIN(b_f ; b_o)	=	91,00 mm
s_{y2} =	$2 * t_o * (b_o / s_o)^{0,5} * (1 - (\gamma_M * \sigma_{f,Ed2} / f_y * 10)^2)^{0,5}$	=	46,99 mm
$R_{y,Rd2}$ =	$(s_{s2} + s_{y2}) * s_o * f_y / \gamma_M / 10^3$	=	107,09 kN

$$P_{sd} / R_{y,Rd2} = \underline{\underline{0,63 < 1}}$$

Check web crushing:**Bottom beam:**

m_1 =	s_{s1} / h_{1u}	=	0,238
m_2 =		=	0,200
m_u =	MIN(m_1 ; m_2)	=	0,200
$R_{a,Rd1}$ =	$0,5 * s_u^2 * (E_s * f_y)^{0,5} * ((t_u / s_u)^{0,5} + 3 * (s_u / t_u) * m_u) / \gamma_M / 10^3$	=	219,95 kN
$P_{sd} / R_{a,Rd1}$		=	<u><u>0,31 < 1</u></u>

$$M_{c,Rd1} = W_{plu} * f_y / \gamma_M / 10^3 = 94,74 \text{ kNm}$$

$$M_{sd1} / M_{c,Rd1} = \underline{\underline{0,74 < 1}}$$

Top beam:

m_1 =	s_{s2} / h_{1o}	=	0,326
m_2 =		=	0,200
m_o =	MIN(m_1 ; m_2)	=	0,200
$R_{a,Rd2}$ =	$0,5 * s_o^2 * (E_s * f_y)^{0,5} * ((t_o / s_o)^{0,5} + 3 * (s_o / t_o) * m_o) / \gamma_M / 10^3$	=	145,85 kN
$P_{sd} / R_{a,Rd2}$		=	<u><u>0,47 < 1</u></u>

$$M_{c,Rd2} = W_{plo} * f_y / \gamma_M / 10^3 = 35,56 \text{ kNm}$$

$$ABS(M_{sd2}) / M_{c,Rd2} = \underline{\underline{0,62 < 1}}$$

Check web buckling for whole web:**Bottom beam:**

$$\text{Effective web width } b_{\text{eff}2} = (h_u^2 + s_{s1}^2)^{0,5} = 192,65 \text{ mm}$$

$$\text{Effective web area } A_2 = b_{\text{eff}2} * s_u / 100 = 12,52 \text{ cm}^2$$

$$\text{Moment of inertia } I_2 = b_{\text{eff}2} / 10 * (s_u / 10)^3 / 12 = 0,441 \text{ cm}^4$$

$$\text{Radius of gyration } i_2 = (I_2 / A_2)^{0,5} = 0,188 \text{ cm}$$

$$\text{Effective slenderness } \lambda_{\text{trans}2} = h_u / (i_2 * \lambda_1 * 10) = 1,076$$

Apply strut curve c:

$$\alpha = 0,49$$

$$\phi = 0,5 * (1 + \alpha * (\lambda_{\text{trans}2} - 0,2) + \lambda_{\text{trans}2}^2) = 1,294$$

$$\chi_2 = 1 / (\phi + (\phi^2 - \lambda_{\text{trans}2}^2)^{0,5}) = 0,4968$$

$$R_{b,Rd2} = \chi_2 * A_2 * f_y / 10 / \gamma_M = 132,88 \text{ kN}$$

$$P_{sd} / R_{b,Rd2} = \underline{\underline{0,51 < 1}}$$

Top beam:

$$\text{Effective web width } b_{\text{eff}1} = (h_o^2 + s_{s1}^2)^{0,5} = 182,79 \text{ mm}$$

$$\text{Effective web area } A_1 = b_{\text{eff}1} * s_o / 100 = 9,69 \text{ cm}^2$$

$$\text{Moment of inertia } I_1 = b_{\text{eff}1} / 10 * (s_o / 10)^3 / 12 = 0,227 \text{ cm}^4$$

$$\text{Radius of gyration } i_1 = (I_1 / A_1)^{0,5} = 0,153 \text{ cm}$$

$$\text{Effective slenderness } \lambda_{\text{trans}1} = h_o / (i_1 * \lambda_1 * 10) = 1,253$$

Apply strut curve c:

$$\alpha = 0,49$$

$$\phi = 0,5 * (1 + \alpha * (\lambda_{\text{trans}1} - 0,2) + \lambda_{\text{trans}1}^2) = 1,543$$

$$\chi_1 = 1 / (\phi + (\phi^2 - \lambda_{\text{trans}1}^2)^{0,5}) = 0,4093$$

$$R_{b,Rd1} = \chi_1 * A_1 * f_y / 10 / \gamma_M = 84,73 \text{ kN}$$

$$P_{sd} / R_{b,Rd1} = \underline{\underline{0,80 < 1}}$$

Check web yield at load points:**Bottom beam:**

$$\sigma_{x,Ed2} = M_{sd1} * 10^2 * (h_u / 2 - t_u) / I_{yu} = 161,25 \text{ kN/cm}^2$$

$$\sigma_{z,Ed2} = 10^3 * P_{sd} / ((s_{s1} + 2 * t_u) * s_u) = 201,80 \text{ kN/cm}^2$$

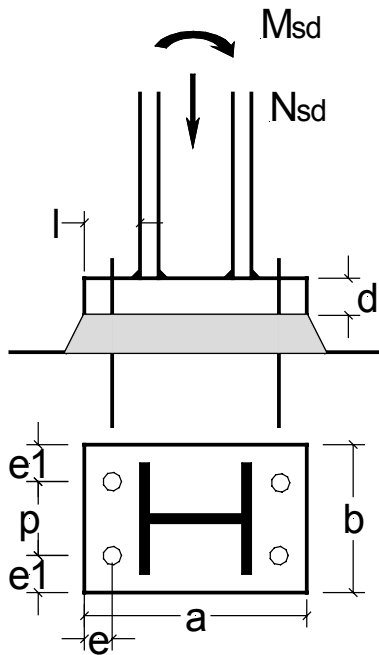
$$(\sigma_{x,Ed2} / f_{yd})^2 + (\sigma_{z,Ed2} / f_{yd})^2 - (\sigma_{x,Ed2} / f_{yd}) * (\sigma_{z,Ed2} / f_{yd}) = \underline{\underline{0,75 < 1}}$$

Top beam:

$$\sigma_{x,Ed1} = -M_{sd2} * 10^2 * (h_o / 2 - t_o) / I_{yo} = 136,67 \text{ kN/cm}^2$$

$$\sigma_{z,Ed1} = 10^3 * P_{sd} / ((s_{s2} + 2 * t_o) * s_o) = 201,76 \text{ kN/cm}^2$$

$$(\sigma_{x,Ed1} / f_{yd})^2 + (\sigma_{z,Ed1} / f_{yd})^2 - (\sigma_{x,Ed1} / f_{yd}) * (\sigma_{z,Ed1} / f_{yd}) = \underline{\underline{0,70 < 1}}$$

Column base subject to compression und bending:**Plan and elevation values:**

Distance to edge of baseplate $e =$	45,00 mm
Distance to edge of baseplate $e_1 =$	100,00 mm
Spacing of bolts $p =$	300,00 mm
Width of baseplate $b =$	500,00 mm
Length of baseplate $a =$	500,00 mm
Plate thickness $d =$	30,00 mm
Projection of plate $l =$	100,00 mm
Weld thickness $a_w =$	10,00 mm
Projection of pad footing $a_r =$	1000,00 mm
Depth of pad footing $h =$	1400,00 mm
as in L.3 (idR) Bearing plane factor $\beta_j = 2/3 =$	0,67

Profil Typ =	SEL("steel/Profils"; Name;)	=	HEB
Selected Profil =	SEL("steel/"Typ; Name;)	=	HEB 300
Moment of inertia $I_{y1} =$	TAB("steel/"Typ; ly; Name=Profil)	=	25170,00 cm ⁴
Flange width $b_f =$	TAB("steel/"Typ; b; Name=Profil)	=	300,00 mm
Flange thickness $t_f =$	TAB("steel/"Typ; t; Name=Profil)	=	19,00 mm
Column height $h_t =$	TAB("steel/"Typ; h; Name=Profil)	=	300,00 mm
$M_{pl,y,Rd} =$	TAB("steel/"Typ; Mplyd; Name=Profil)	=	418,00 kNm
$N_{pl,Rd} =$	TAB("steel/"Typ; Npld; Name=Profil)	=	3250,00 kN

Loads:

$N_{sd} =$	1000,00 kN
$M_{sd} =$	221,75 kNm

Materials and stresses:

steel =	SEL("steel/EC"; Name;)	=	Fe 430
E_s =	TAB("steel/EC"; E; Name=steel)	=	210000,00 N/mm ²
f_y =	TAB("steel/EC"; f_y ; Name=steel)	=	275,00 N/mm ²
Concrete =	SEL("Concrete/EC"; Name;)	=	C30/37
f_{ck} =	TAB("Concrete/EC"; f_{ck} ; Name=Concrete)	=	30,00 N/mm ²
SC =	SEL("steel/bolt"; SC;)	=	4.6
Bolt =	SEL("steel/bolt"; BS;)	=	M 24
f_u =	TAB("steel/bolt"; f_{ub} ; SC=SC)	=	400,00 N/mm ²
A_s =	TAB("steel/bolt"; A_s ; BS=Bolt)	=	3,53 cm ²
γ_{Mb} =			1,25
γ_c =			1,50
γ_{M0} =			1,10

Design:

m =	$l - e - 0,8 * a_w * \sqrt{2}$	=	43,69 mm
l_{eff1a} =	$\text{MIN}(4 * m + 1,25 * e; 2 * m + 0,625 * e + e_1)$	=	215,51 mm
l_{eff1b} =	$\text{MIN}(2 * m + 0,625 * e + 0,5 * p; e_1 + 0,5 * p; b / 2)$	=	250,00 mm
l_{eff1} =	$\text{MIN}(l_{eff1a}; l_{eff1b})$	=	215,51 mm
l_{eff2a} =	$\text{MIN}(\pi * 2 * m; \pi * m + 2 * e_1)$	=	274,51 mm
l_{eff2b} =	$\text{MIN}(\pi * m + p; p + 2 * e_1)$	=	437,26 mm
l_{eff} =	$\text{MIN}(l_{eff2a}; l_{eff2b}; l_{eff1})$	=	215,51 mm

Maximum stress of base plate at the centre of tension bolt:

$M_{pl,1,Rd}$ =	$0,25 * l_{eff} * (d / 10)^2 * f_y / 10 / \gamma_{M0}$	=	$12,12 * 10^3$ kNm
n =	e	=	45,00 mm
$n / (1,25 * m)$		=	0,82 < 1
$B_{t,Rd}$ =	$0,9 * f_u * A_s / 10 / \gamma_{Mb}$	=	101,66 kN

Full flange yield:

$$F_{T,Rd1} = 4 * M_{pl,1,Rd} / m = 1109,64 \text{ kN}$$

Bolt failure with flange yielding:

$$F_{T,Rd2} = (2 * M_{pl,1,Rd} + n * 2 * B_{t,Rd}) / (m + n) = 376,47 \text{ kN}$$

Bolt failure without flange yielding:

$$F_{T,Rd3} = 2 * B_{t,Rd} = 203,32 \text{ kN}$$

$$F_{T,Rd} = \text{MIN}(F_{T,Rd1}; F_{T,Rd2}; F_{T,Rd3}) = \mathbf{203,32 \text{ kN}}$$

Effective compression area:

Limit pressure in the base plate:

$$a_1 = \text{MIN}(a + 2 * a_r; 5 * a; a + h) = 1900,00 \text{ mm}$$

$$k_j = (a_1^2 / (a * b))^{0,5} = 3,80$$

$$f_j = \beta_j * k_j * f_{ck} / \gamma_c = 50,92 \text{ N/mm}^2$$

$$A_{eff} = 10 * (N_{sd} + F_{T,Rd}) / f_j = 236,32 \text{ cm}^2$$

$$c = d * (f_y * 10 / (3 * f_j * \gamma_{M0}))^{0,5} = 121,36 \text{ mm}$$

$$x_0 = 100 * A_{eff} / (2 * c + b_f) = 43,54 \text{ mm}$$

$$x_0 / (t_f + 2 * c) = \mathbf{0,17 < 1}$$

Limit moment at column base:

$$r_c = h_t / 2 + c - x_0 / 2 = 249,59 \text{ mm}$$

$$M_{Rd} = (F_{T,Rd} * 10^3 * (h_t/2 + 100 - e) + A_{eff} * 100 * f_j * r_c) / 10^6 = 342,02 \text{ kNm}$$

Check permissible strength of column to bending and compression.:

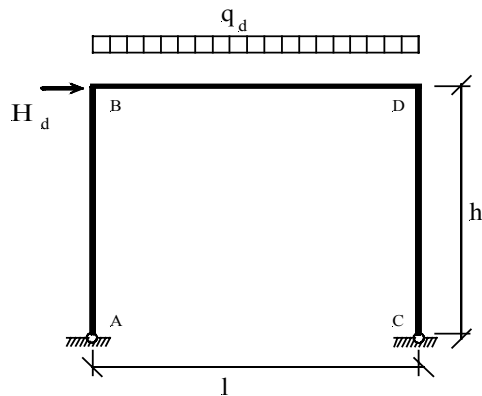
$$M_{Ny,Rd} = 1,1 * M_{pl,y,Rd} * (1 - N_{sd} / N_{pl,Rd}) = 318,32 \text{ kNm}$$

Analysis:

$$M_{sd} / \text{MIN}(M_{Ny,Rd}; M_{Rd}) = \underline{\underline{0,70 < 1}}$$

Frames

Sway frame with bracing out of plane of frame, plastic theory:



Plan and elevation values:

Frame width $l =$	8,00 m
Frame depth $h =$	6,00 m
Number of column $n_c =$	2
Number of storeys $n_s =$	1

Beam:

Profil Typ1 =	SEL("steel/Profils"; Name;)	=	IPE
Selected Profil1=	SEL("steel/"Typ1; Name;)	=	IPE 240
Column height $h_1 =$	TAB("steel/"Typ1; h; Name=Profil1)	=	240,00 mm
Web thickness $s_1 =$	TAB("steel/"Typ1; s; Name=Profil1)	=	6,20 mm
Moment of inertia $I_{y1} =$	TAB("steel/"Typ1; Iy; Name=Profil1)	=	3890,00 cm ⁴
Cross-sectional area $A_1 =$	TAB("steel/"Typ1; A; Name=Profil1)	=	39,10 cm ²
Moment of resistance $W_{y1} =$	TAB("steel/"Typ1; Wy; Name=Profil1)	=	324,00 cm ³
Moment of resistance $W_{pl,y1} =$	1,14 * W_{y1}	=	369,36 cm ³

Column section:

Profil Typ2 =	SEL("steel/Profils"; Name;)	=	HEB
Selected Profil2 =	SEL("steel/"Typ2; Name;)	=	HEB 240
Flange width $b_2 =$	TAB("steel/"Typ2; b; Name=Profil2)	=	240,00 mm
Column height $h_2 =$	TAB("steel/"Typ2; h; Name=Profil2)	=	240,00 mm
Web thickness $s_2 =$	TAB("steel/"Typ2; s; Name=Profil2)	=	10,00 mm
Moment of inertia $I_{y2} =$	TAB("steel/"Typ2; Iy; Name=Profil2)	=	11260,00 cm ⁴
Moment of inertia $I_{z2} =$	TAB("steel/"Typ2; Iz; Name=Profil2)	=	3920,00 cm ⁴
Moment of inertia $I_{t2} =$	TAB("steel/"Typ2; IT; Name=Profil2)	=	103,00 cm ⁴
Moment of inertia $I_{\omega 2} =$	10 ³ *TAB("steel/"Typ2; I ω ; Name=Profil2)	=	486900,00 cm ⁶
Cross-sectional area $A_2 =$	TAB("steel/"Typ2; A; Name=Profil2)	=	106,000 cm ²
$i_y =$	TAB("steel/"Typ2; iy; Name=Profil2)	=	10,30 cm
$i_z =$	TAB("steel/"Typ2; iz; Name=Profil2)	=	6,08 cm
Moment of resistance $W_{ely2} =$	TAB("steel/"Typ2; Wy; Name=Profil2)	=	938,00 cm ³
Moment of resistance $W_{ply2} =$	1,25 * W_{ely2}	=	1172,50 cm ³

Loads:

$H_d =$	9,00 kN
$q_d =$	9,00 kN/m

Materials and stresses:

steel =	SEL("steel/EC"; Name;)	=	Fe 360
$E_s =$	TAB("steel/EC"; E; Name=steel)	=	210000,00 N/mm ²
$G =$	TAB("steel/EC"; G; Name=steel)	=	81000,00 N/mm ²
$f_y =$	TAB("steel/EC"; fy; Name=steel)	=	235,00 N/mm ²
$\epsilon =$	$\sqrt{(235 / f_y)}$	=	1,00
$\gamma_M =$		=	1,10
$\lambda_1 =$	$93,90 * \epsilon$	=	93,90

Frame classification as in 5.2.5.2.:

Frame sways

$$k = I_{y1} / I_{y2} * h / l = 0,259$$

Deflection at top of frame due to horizontal load:

$$H = 1,00 \text{ kN}$$

$$\delta = (100 * h)^3 / (1,2 * E_s * I_{y2}) * (2 * k + 1) / k * H = 0,446 \text{ cm}$$

Sumtotal of vertical loads:

$$V = q_d * l = 72,00 \text{ kN}$$

Bracing is restrained out of plane of frame

$$\delta / (h * 100) * V / H = \underline{0,054 < 0,1}$$

⇒ Sway frame, plastic theory, restrained from moving out of plane.

Design with plastic theory

Imperfection:

$$\varphi_0 = 1 / 200 = 0,005$$

$$k_C = \text{MIN}(\sqrt{(0,5 + 1 / n_C)}; 1) = 1,00$$

$$k_S = \text{MIN}(\sqrt{(0,2 + 1 / n_S)}; 1) = 1,00$$

$$\varphi = \varphi_0 * k_C * k_S = 0,0050$$

$$\Delta H_d = \varphi * V = 0,36 \text{ kN}$$

$$H_{sd} = H_d + \Delta H_d = 9,36 \text{ kN}$$

Design calculations:

Reactions at column bases:

$$H_1 = q_d * l^2 / (4 * h * (2 * k + 3)) = 6,82 \text{ kN}$$

$$V_1 = q_d * l / 2 = 36,00 \text{ kN}$$

$$M_{B1} = -H_1 * h = -40,92 \text{ kNm}$$

$$H_2 = H_{sd} / 2 = 4,68 \text{ kN}$$

$$V_2 = H_{sd} * h / l = 7,02 \text{ kN}$$

$$M_{B2} = H_2 * h = 28,08 \text{ kNm}$$

Analysis of column

$$N_{sd} = V_1 + V_2 = 43,02 \text{ kN}$$

$$V_{sd} = H_1 + H_2 = 11,50 \text{ kN}$$

$$M_D = M_{B1} - M_{B2} = -69,00 \text{ kNm}$$

$$M_C = 0,00 \text{ kNm}$$

Buckling in the plane of frame as in section E:

$$\begin{aligned}
 k_c &= I_{y2} / h / 100 &= & 18,77 \text{ cm}^3 \\
 k_1 &= 1,5 * I_{y1} / I / 100 &= & 7,29 \text{ cm}^3 \\
 k_2 &= &= & 0,0 \\
 \eta_2 &= &= & 1 \text{ (Hinge)} \\
 \eta_1 &= k_c / (k_c + k_1 + k_2) &= & 0,72 \\
 \text{Slenderness ratio as in Fig. E.2.1.:} & & & \\
 l &= 3,2 * h &= & 19,20 \text{ m} \\
 \lambda_y &= 100 * l / i_y &= & 186,41 \\
 \lambda_{\text{trans,y}} &= \lambda_y / (\lambda_1 * \epsilon) &= & 1,99 \\
 h_2 / b_2 &= &= & 1,00 < 1,2 \\
 \text{Apply strut curve b:} & & & \\
 \alpha &= &= & 0,34 \\
 \beta_A &= &= & 1,000 \\
 \varphi &= 0,5 * (1 + \alpha * (\lambda_{\text{trans,y}} - 0,2) + \lambda_{\text{trans,y}}^2) &= & 2,784 \\
 \chi_y &= 1 / (\varphi + (\varphi^2 - \lambda_{\text{trans,y}}^2)^{0,5}) &= & 0,2114
 \end{aligned}$$

Buckling outside the plane of frame

$$\begin{aligned}
 \lambda_z &= 100 * h / i_z &= & 98,68 \\
 \lambda_{\text{trans,z}} &= \lambda_z / (\lambda_1 * \epsilon) &= & 1,05 \\
 \text{Apply strut curve c:} & & & \\
 \alpha &= &= & 0,49 \\
 \beta_A &= &= & 1,000 \\
 \varphi &= 0,5 * (1 + \alpha * (\lambda_{\text{trans,z}} - 0,2) + \lambda_{\text{trans,z}}^2) &= & 1,260 \\
 \chi_z &= 1 / (\varphi + (\varphi^2 - \lambda_{\text{trans,z}}^2)^{0,5}) &= & 0,5111 \\
 \chi_{\text{min}} &= \text{MIN}(\chi_y, \chi_z) &= & 0,2114
 \end{aligned}$$

Check bending and buckling:

$$\begin{aligned}
 \psi &= &= & 0,00 \\
 \beta_{My} &= 1,8 - 0,7 * \psi &= & 1,80 \\
 \mu_y &= \lambda_{\text{trans,y}} * (2 * \beta_{My} - 4) + (W_{\text{ply2}} - W_{\text{ely2}}) / W_{\text{ely2}} &= & -0,546 < 0,9 \\
 k_y &= 1 - (\mu_y * N_{\text{sd}}) / (\chi_y * A_2 * f_y) &= & 1,004 < 1,5
 \end{aligned}$$

$$N_{\text{sd}} / (\chi_{\text{min}} * A_2 * f_y / 10 / \gamma_M) + 10^3 * k_y * \text{ABS}(M_D) / (W_{\text{ply2}} * f_y / \gamma_M) = \underline{0,37 < 1}$$

Check torsional-flexural buckling:

$$\begin{aligned}
 C_1 &= &= & 1,879 \\
 M_{\text{cr}} &= (C_1 * \pi^2 * E_s * I_{z2} / (h * 100)^2 / 10 * (I_{\omega 2} / I_{z2} + ((h * 100)^2 * G * I_{t2}) / (\pi^2 * E_s * I_{z2})))^{0,5} &= & 94241,31 \text{ kNcm} \\
 \text{As in Table: F.1.1} & & & \\
 \psi &= &= & 0,00 \\
 \beta_w &= &= & 1,00 \\
 k &= &= & 1,00 \\
 \lambda_{\text{LT}} &= \sqrt{(\pi^2 * E_s / 10 * W_{\text{ply2}} / M_{\text{cr}})} &= & 50,78 \\
 \lambda_{\text{trans,LT}} &= \lambda_{\text{LT}} / \lambda_1 * \sqrt{\beta_w} &= & 0,541
 \end{aligned}$$

Apply strut curve a

$$\alpha = 0,21$$

$$\varphi = 0,5 * (1 + \alpha * (\lambda_{trans,LT} - 0,2) + \lambda_{trans,LT}^2) = 0,682$$

$$\chi_{LT} = 1 / (\varphi + (\varphi^2 - \lambda_{trans,LT}^2)^{0,5}) = 0,9114$$

$$\beta_{M,LT} = 1,8 - 0,7 * \psi = 1,80$$

$$\mu_{LT} = 0,15 * \lambda_{trans,z} * \beta_{M,LT} - 0,15 = 0,134 < 0,9$$

$$k_{LT} = 1 - (\mu_{LT} * N_{sd}) / (\chi_{LT} * A_2 * f_y) = 1,000 < 1,5$$

$$N_{sd} / (\chi_z * A_2 * f_y / 10 / \gamma_M) + 10^3 * k_{LT} * ABS(M_D) / (\chi_{LT} * W_{ply2} * f_y / \gamma_M) = \underline{0,339 < 1}$$

Section analysis at D:**Column:**

$$A_V = 1,04 * h_2 * s_2 / 10^2 = 24,96 \text{ cm}^2$$

$$V_{pl,Rd} = A_V * f_y / 10 / \sqrt{3} / \gamma_M = 307,86 \text{ kN}$$

$$V_{sd} / V_{pl,Rd} = \underline{0,037 < 0,5}$$

No interaction

$$N_{pl,Rd} = A_2 * f_y / 10 / \gamma_M = 2264,55 \text{ kN}$$

$$n = N_{sd} / N_{pl,Rd} = 0,02$$

$$M_{pl,y,Rd} = W_{ply2} * f_y / (\gamma_M * 10^3) = 250,49 \text{ kNm}$$

$$M_{Ny,Rd} = 1,11 * M_{pl,y,Rd} * (1 - n) = 272,48 \text{ kNm}$$

$$ABS(M_D) / \text{MIN}(M_{pl,y,Rd}; M_{Ny,Rd}) = \underline{0,28 < 1}$$

Beam:

$$A_V = 1,04 * h_1 * s_1 / 10^2 = 15,48 \text{ cm}^2$$

$$V_{pl,Rd} = A_V * f_y / 10 / \sqrt{3} / \gamma_M = 190,93 \text{ kN}$$

$$N_{sd} / V_{pl,Rd} = \underline{0,225 < 0,5}$$

No interaction

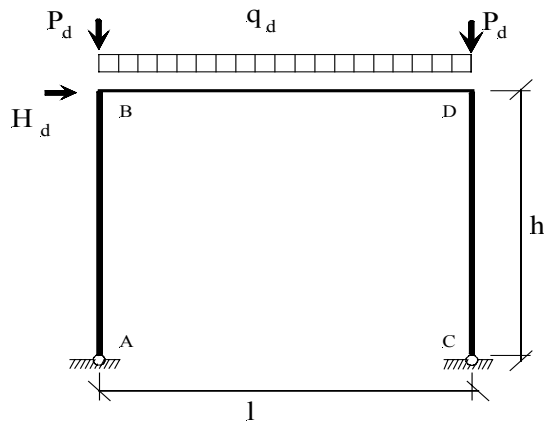
$$N_{pl,Rd} = A_1 * f_y / 10 / \gamma_M = 835,32 \text{ kN}$$

$$n = V_{sd} / N_{pl,Rd} = 0,014$$

$$M_{pl,y,Rd} = W_{ply1} * f_y / (\gamma_M * 10^3) = 78,91 \text{ kNm}$$

$$M_{Ny,Rd} = 1,11 * M_{pl,y,Rd} * (1 - n) = 86,36 \text{ kNm}$$

$$ABS(M_D) / \text{MIN}(M_{pl,y,Rd}; M_{Ny,Rd}) = \underline{0,87 < 1}$$

Frame, plastic with magnifying factor**Plan and elevation values:**

Frame width l =	8,00 m
Frame depth h =	6,00 m
Number of column n_c =	2
Number of storeys n_s =	1

Beam:

Profil Typ1 =	SEL("steel/Profils"; Name;)	=	IPE
Selected Profil1=	SEL("steel/"Typ1; Name;)	=	IPE 240
Column height h_1 =	TAB("steel/"Typ1; h; Name=Profil1)	=	240,00 mm
Flange thickness s_1 =	TAB("steel/"Typ1; s; Name=Profil1)	=	6,20 mm
Moment of inertia I_{y1} =	TAB("steel/"Typ1; Iy; Name=Profil1)	=	3890,00 cm ⁴
Cross-sectional area A_1 =	TAB("steel/"Typ1; A; Name=Profil1)	=	39,10 cm ²
Moment of resistance W_{y1} =	TAB("steel/"Typ1; Wy; Name=Profil1)	=	324,00 cm ³
Moment of resistance $W_{pl,y1}$ =	1,14 * W_{y1}	=	369,36 cm ³

Column section:

Profil Typ2 =	SEL("steel/Profils"; Name;)	=	HEB
Selected Profil2 =	SEL("steel/"Typ2; Name;)	=	HEB 240
Flange width b_2 =	TAB("steel/"Typ2; b; Name=Profil2)	=	240,00 mm
Column height h_2 =	TAB("steel/"Typ2; h; Name=Profil2)	=	240,00 mm
Flange thickness s_2 =	TAB("steel/"Typ2; s; Name=Profil2)	=	10,00 mm
Moment of inertia I_{y2} =	TAB("steel/"Typ2; Iy; Name=Profil2)	=	11260,00 cm ⁴
Moment of inertia I_{z2} =	TAB("steel/"Typ2; Iz; Name=Profil2)	=	3920,00 cm ⁴
Moment of inertia I_{t2} =	TAB("steel/"Typ2; IT; Name=Profil2)	=	103,00 cm ⁴
Moment of inertia $I_{\omega 2}$ =	10 ³ *TAB("steel/"Typ2; I ω ; Name=Profil2)	=	486900,00 cm ⁶
Cross-sectional area A_2 =	TAB("steel/"Typ2; A; Name=Profil2)	=	106,000 cm ²
i_y =	TAB("steel/"Typ2; iy; Name=Profil2)	=	10,30 cm
i_z =	TAB("steel/"Typ2; iz; Name=Profil2)	=	6,08 cm
Moment of resistance W_{ely2} =	TAB("steel/"Typ2; Wy; Name=Profil2)	=	938,00 cm ³
Moment of resistance W_{ply2} =	1,25 * W_{ely2}	=	1172,50 cm ³

Loads:

H_d =	9,00 kN
q_d =	8,00 kN/m
P_d =	100,00 kN

Materials and stresses:

steel =	SEL("steel/EC"; Name;)	=	Fe 360
$E_s =$	TAB("steel/EC"; E; Name=steel)	=	210000,00 N/mm ²
G =	TAB("steel/EC"; G; Name=steel)	=	81000,00 N/mm ²
$f_y =$	TAB("steel/EC"; fy; Name=steel)	=	235,00 N/mm ²
$\epsilon =$	$\sqrt{(235 / f_y)}$	=	1,00
$\gamma_M =$			1,10
$\lambda_1 =$	$93,90 * \epsilon$	=	93,90

Frame classification as in 5.2.5.2.:

Frame sways

Classification of stiffness:

$$k = \frac{l_{y1}}{l_{y2}} * h / l = 0,259$$

Deflection at top of frame due to horizontal load:

$$H = 1,00 \text{ kN}$$

$$\delta = \frac{(100 * h)^3}{(1,2 * E_s * I_{y2}) * (2 * k + 1)} / k * H = 0,446 \text{ cm}$$

Sumtotal of vertical loads:

$$V = P_d * 2 + q_d * l = 264,00 \text{ kN}$$

$$\delta / (h * 100) * V / H = 0,196 > 0,1$$

⇒ Frame, laterally unrestrained!;restrained from moving out of plane. mit Vergrößerungsfaktor!

Design with plastic theory and magnifying factor

Imperfection:

$\phi_0 =$	$1 / 200$	=	0,005
$k_c =$	$\text{MIN}(\sqrt{(0,5 + 1 / n_c)}; 1)$	=	1,00
$k_s =$	$\text{MIN}(\sqrt{(0,2 + 1 / n_s)}; 1)$	=	1,00
$\phi =$	$\phi_0 * k_c * k_s$	=	0,0050
$\Delta H_d =$	$\phi * V$	=	1,32 kN
$H_{sd} =$	$H_d + \Delta H_d$	=	10,32 kN

Design calculations:

Reactions at column bases:

$H_1 =$	$q_d * l^2 / (4 * h * (2 * k + 3))$	=	6,06 kN
$V_1 =$	$q_d * l / 2$	=	32,00 kN
$M_{B1} =$	$-H_1 * h$	=	-36,36 kNm
$H_2 =$	$H_{sd} / 2$	=	5,16 kN
$V_2 =$	$H_{sd} * h / l$	=	7,74 kN
$M_{B2} =$	$H_2 * h$	=	30,96 kNm

Analysis of column

Dischinger factor:

D =	$1 / (1 - (\delta / (h * 100) * V / H))$	=	1,244
$M_D =$	$M_{B1} - D * M_{B2}$	=	-74,87 kNm
$N_{sd} =$	$V_1 + D * V_2 + P_d$	=	141,63 kN
$V_{sd} =$	$H_1 + D * H_2$	=	12,48 kN

Buckling in the plane of frame:

$k_c =$	$l_{y2} / h / 100$	=	18,77 cm ³
$k_1 =$	$l_{y1} / l / 100$	=	4,86 cm ³
$k_2 =$		=	0,0
$\eta_2 =$		=	1 (Hinge)
$\eta_1 =$	$k_c / (k_c + k_1 + k_2)$	=	0,79

Slenderness ratio as in Fig. E.2.1.:

$$\begin{aligned}
 l &= 0,92 * h &= 5,52 \text{ m} \\
 \lambda_y &= 100 * l / i_y &= 53,59 \\
 \lambda_{\text{trans},y} &= \lambda_y / (\lambda_1 * \epsilon) &= 0,57 \\
 h_2 / b_2 & &= 1,00 < 1,2
 \end{aligned}$$

Apply strut curve b:

$$\begin{aligned}
 \alpha &= 0,34 \\
 \beta_A &= 1,000 \\
 \varphi &= 0,5 * (1 + \alpha * (\lambda_{\text{trans},y} - 0,2) + \lambda_{\text{trans},y}^2) &= 0,725 \\
 \chi_y &= 1 / (\varphi + (\varphi^2 - \lambda_{\text{trans},y}^2)^{0,5}) &= 0,8525
 \end{aligned}$$

Buckling outside the plane of frame

$$\begin{aligned}
 \lambda_z &= 100 * h / i_z &= 98,68 \\
 \lambda_{\text{trans},z} &= \lambda_z / (\lambda_1 * \epsilon) &= 1,05
 \end{aligned}$$

Apply strut curve c:

$$\begin{aligned}
 \alpha &= 0,49 \\
 \beta_A &= 1,000 \\
 \varphi &= 0,5 * (1 + \alpha * (\lambda_{\text{trans},z} - 0,2) + \lambda_{\text{trans},z}^2) &= 1,260 \\
 \chi_z &= 1 / (\varphi + (\varphi^2 - \lambda_{\text{trans},z}^2)^{0,5}) &= 0,5111 \\
 \chi_{\text{min}} &= \text{MIN}(\chi_y; \chi_z) &= 0,5111
 \end{aligned}$$

Check bending and buckling:

$$\begin{aligned}
 \psi &= 0,00 \\
 \beta_{My} &= 1,8 - 0,7 * \psi &= 1,80 \\
 \mu_y &= \lambda_{\text{trans},y} * (2 * \beta_{My} - 4) + (W_{\text{ply}2} - W_{\text{ely}2}) / W_{\text{ely}2} &= 0,022 < 0,9 \\
 k_y &= 1 - (\mu_y * N_{\text{sd}}) / (\chi_y * A_2 * f_y) &= 1,000 < 1,5
 \end{aligned}$$

$$N_{\text{sd}} / (\chi_{\text{min}} * A_2 * f_y / 10 / \gamma_M) + 10^{3 * k_y} * \text{ABS}(M_D) / (W_{\text{ply}2} * f_y / \gamma_M) = \underline{\underline{0,42 < 1}}$$

Check torsional-flexural buckling:

$$\begin{aligned}
 C_1 &= 1,879 \\
 M_{\text{cr}} &= (C_1 * \pi^2 * E_s * I_{z2} / (h * 100)^2 / 10 * (I_{\omega 2} / I_{z2} + ((h * 100)^2 * G * I_{t2} / (\pi^2 * E_s * I_{z2})))^{0,5}) = 94241,31 \text{ kNcm}
 \end{aligned}$$

As in Table: F.1.1

$$\begin{aligned}
 \psi &= 0,00 \\
 \beta_w &= 1,00 \\
 k &= 1,00 \\
 \lambda_{\text{LT}} &= \sqrt{(\pi^2 * E_s / 10 * W_{\text{ply}2} / M_{\text{cr}})} &= 50,78 \\
 \lambda_{\text{trans,LT}} &= \lambda_{\text{LT}} / \lambda_1 * \sqrt{\beta_w} &= 0,541
 \end{aligned}$$

Apply strut curve a

$$\begin{aligned}
 \alpha &= 0,21 \\
 \varphi &= 0,5 * (1 + \alpha * (\lambda_{\text{trans,LT}} - 0,2) + \lambda_{\text{trans,LT}}^2) &= 0,682 \\
 \chi_{\text{LT}} &= 1 / (\varphi + (\varphi^2 - \lambda_{\text{trans,LT}}^2)^{0,5}) &= 0,9114 \\
 \beta_{\text{M,LT}} &= 1,8 - 0,7 * \psi &= 1,80 \\
 \mu_{\text{LT}} &= 0,15 * \lambda_{\text{trans},z} * \beta_{\text{M,LT}} - 0,15 &= 0,134 < 0,9 \\
 k_{\text{LT}} &= 1 - (\mu_{\text{LT}} * N_{\text{sd}}) / (\chi_{\text{LT}} * A_2 * f_y) &= 0,999 < 1,5
 \end{aligned}$$

$$N_{\text{sd}} / (\chi_z * A_2 * f_y / 10 / \gamma_M) + 10^{3 * k_{\text{LT}}} * \text{ABS}(M_D) / (\chi_{\text{LT}} * W_{\text{ply}2} * f_y / \gamma_M) = \underline{\underline{0,450 < 1}}$$

Section analysis at D:**Column:**

$$A_v = 1,04 * h_2 * s_2 / 10^2 = 24,96 \text{ cm}^2$$

$$V_{pl,Rd} = A_v * f_y / 10 / \sqrt{3} / \gamma_M = 307,86 \text{ kN}$$

$$V_{sd} / V_{pl,Rd} = \underline{\underline{0,041 < 0,5}}$$

No interaction

$$N_{pl,Rd} = A_2 * f_y / 10 / \gamma_M = 2264,55 \text{ kN}$$

$$n = N_{sd} / N_{pl,Rd} = 0,063$$

$$M_{pl,y,Rd} = W_{ply2} * f_y / (\gamma_M * 10^3) = 250,49 \text{ kNm}$$

$$M_{Ny,Rd} = 1,11 * M_{pl,y,Rd} * (1 - n) = 260,53 \text{ kNm}$$

$$ABS(M_D) / \text{MIN}(M_{pl,y,Rd}; M_{Ny,Rd}) = \underline{\underline{0,30 < 1}}$$

Beam:

$$A_v = 1,04 * h_1 * s_1 / 10^2 = 15,48 \text{ cm}^2$$

$$V_{pl,Rd} = A_v * f_y / 10 / \sqrt{3} / \gamma_M = 190,93 \text{ kN}$$

$$N_{sd} / V_{pl,Rd} = \underline{\underline{0,742 < 0,5}}$$

No interaction

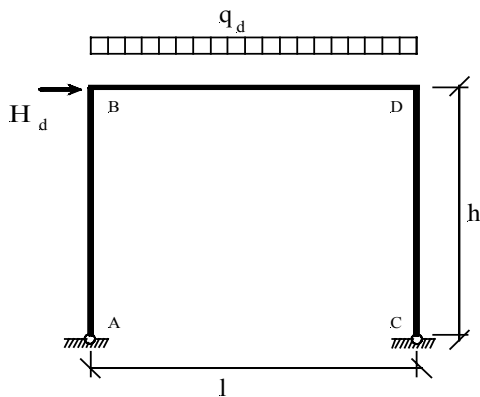
$$N_{pl,Rd} = A_1 * f_y / 10 / \gamma_M = 835,32 \text{ kN}$$

$$n = V_{sd} / N_{pl,Rd} = 0,015$$

$$M_{pl,y,Rd} = W_{ply1} * f_y / (\gamma_M * 10^3) = 78,91 \text{ kNm}$$

$$M_{Ny,Rd} = 1,11 * M_{pl,y,Rd} * (1 - n) = 86,28 \text{ kNm}$$

$$ABS(M_D) / \text{MIN}(M_{pl,y,Rd}; M_{Ny,Rd}) = \underline{\underline{0,95 < 1}}$$

Sway frame with bracing out of plane of frame, plastic theory:**Plan and elevation values:**

Frame width $l =$	8,00 m
Frame depth $h =$	6,00 m
Number of column $n_c =$	2
Number of storeys $n_s =$	1

Beam:

Profil Typ1 =	SEL("steel/Profils"; Name;)	=	IPE
Selected Profil1 =	SEL("steel/"Typ1; Name;)	=	IPE 240
Column height $h_1 =$	TAB("steel/"Typ1; h; Name=Profil1)	=	240,00 mm
Web thickness $s_1 =$	TAB("steel/"Typ1; s; Name=Profil1)	=	6,20 mm
Moment of inertia $I_{y1} =$	TAB("steel/"Typ1; Iy; Name=Profil1)	=	3890,00 cm ⁴
Cross-sectional area $A_1 =$	TAB("steel/"Typ1; A; Name=Profil1)	=	39,10 cm ²
Moment of resistance $W_{y1} =$	TAB("steel/"Typ1; Wy; Name=Profil1)	=	324,00 cm ³
Moment of resistance $W_{pl,y1} =$	1,14 * W_{y1}	=	369,36 cm ³

Column section:

Profil Typ2 =	SEL("steel/Profils"; Name;)	=	HEB
Selected Profil2 =	SEL("steel/"Typ2; Name;)	=	HEB 240
Flange width $b_2 =$	TAB("steel/"Typ2; b; Name=Profil2)	=	240,00 mm
Column height $h_2 =$	TAB("steel/"Typ2; h; Name=Profil2)	=	240,00 mm
Web thickness $s_2 =$	TAB("steel/"Typ2; s; Name=Profil2)	=	10,00 mm
Moment of inertia $I_{y2} =$	TAB("steel/"Typ2; Iy; Name=Profil2)	=	11260,00 cm ⁴
Moment of inertia $I_{z2} =$	TAB("steel/"Typ2; Iz; Name=Profil2)	=	3920,00 cm ⁴
Moment of inertia $I_{t2} =$	TAB("steel/"Typ2; IT; Name=Profil2)	=	103,00 cm ⁴
Moment of inertia $I_{\omega 2} =$	10 ³ *TAB("steel/"Typ2; I ω ; Name=Profil2)	=	486900,00 cm ⁶
Cross-sectional area $A_2 =$	TAB("steel/"Typ2; A; Name=Profil2)	=	106,000 cm ²
$i_y =$	TAB("steel/"Typ2; iy; Name=Profil2)	=	10,30 cm
$i_z =$	TAB("steel/"Typ2; iz; Name=Profil2)	=	6,08 cm
Moment of resistance $W_{ely2} =$	TAB("steel/"Typ2; Wy; Name=Profil2)	=	938,00 cm ³
Moment of resistance $W_{ply2} =$	1,25 * W_{ely2}	=	1172,50 cm ³

Loads:

$H_d =$	9,00 kN
$q_d =$	9,00 kN/m

Materials and stresses:

steel =	SEL("steel/EC"; Name;)	=	Fe 360
E_s =	TAB("steel/EC"; E; Name=steel)	=	210000,00 N/mm ²
G =	TAB("steel/EC"; G; Name=steel)	=	81000,00 N/mm ²
f_y =	TAB("steel/EC"; fy; Name=steel)	=	235,00 N/mm ²
ϵ =	$\sqrt{(235 / f_y)}$	=	1,00
γ_M =		=	1,10
λ_1 =	$93,90 * \epsilon$	=	93,90

Frame classification as in 5.2.5.2.:

Frame sways

$$k = \frac{l_{y1}}{l_{y2}} * h / l = 0,259$$

Deflection at top of frame due to horizontal load:

$$H = 1,00 \text{ kN}$$

$$\delta = \frac{(100 * h)^3 * 10}{(12 * E_s * I_{y2}) * (2 * k + 1)} / k * H = 0,446 \text{ cm}$$

Sumtotal of vertical loads:

$$V = q_d * l = 72,00 \text{ kN}$$

Bracing is restrained out of plane of frame

$$\delta / (h * 100) * V / H = 0,0535 < 0,1$$

⇒ Sway frame, plastic theory;restrained from moving out of plane.

Design with plastic theory and magnifying factor

Imperfection:

ϕ_0 =	$1 / 200$	=	0,005
k_c =	$\text{MIN}(\sqrt{(0,5 + 1 / n_c)}; 1)$	=	1,00
k_s =	$\text{MIN}(\sqrt{(0,2 + 1 / n_s)}; 1)$	=	1,00
ϕ =	$\phi_0 * k_c * k_s$	=	0,0050
ΔH_d =	$\phi * V$	=	0,36 kN
H_{sd} =	$H_d + \Delta H_d$	=	9,36 kN

Design calculations:

Reactions at column bases:

H_1 =	$q_d * l^2 / (4 * h * (2 * k + 3))$	=	6,82 kN
V_1 =	$q_d * l / 2$	=	36,00 kN
M_{B1} =	$-H_1 * h$	=	-40,92 kNm
H_2 =	$H_{sd} / 2$	=	4,68 kN
V_2 =	$H_{sd} * h / l$	=	7,02 kN
M_{B2} =	$H_2 * h$	=	28,08 kNm

Analysis of column

N_{sd} =	$V_1 + V_2$	=	43,02 kN
V_{sd} =	$H_1 + H_2$	=	11,50 kN

Dischinger factor:

D =	$1 / (1 - (\delta / (h * 100)) * V / H)$	=	1,057
M_D =	$M_{B1} - D * M_{B2}$	=	-70,60 kNm

Buckling in the plane of frame:

k_c =	$l_{y2} / h / 100$	=	18,77 cm ³
k_1 =	$l_{y1} / l / 100$	=	4,86 cm ³
k_2 =		=	0,0
η_2 =		=	1 (Hinge)
η_1 =	$k_c / (k_c + k_1 + k_2)$	=	0,79

Slenderness ratio as in Fig. E.2.1.:

$$\begin{aligned}
 l &= 0,92 * h &= & 5,52 \text{ m} \\
 \lambda_y &= 100 * l / i_y &= & 53,59 \\
 \lambda_{\text{trans},y} &= \lambda_y / (\lambda_1 * \epsilon) &= & 0,57 \\
 h_2 / b_2 & &= & 1,00 < 1,2
 \end{aligned}$$

Apply strut curve b:

$$\begin{aligned}
 \alpha &= 0,34 \\
 \beta_A &= 1,000 \\
 \varphi &= 0,5 * (1 + \alpha * (\lambda_{\text{trans},y} - 0,2) + \lambda_{\text{trans},y}^2) &= & 0,725 \\
 \chi_y &= 1 / (\varphi + (\varphi^2 - \lambda_{\text{trans},y}^2)^{0,5}) &= & 0,8525
 \end{aligned}$$

Buckling outside the plane of frame

$$\begin{aligned}
 \lambda_z &= 100 * h / i_z &= & 98,68 \\
 \lambda_{\text{trans},z} &= \lambda_z / (\lambda_1 * \epsilon) &= & 1,05
 \end{aligned}$$

Apply strut curve c:

$$\begin{aligned}
 \alpha &= 0,49 \\
 \beta_A &= 1,000 \\
 \varphi &= 0,5 * (1 + \alpha * (\lambda_{\text{trans},z} - 0,2) + \lambda_{\text{trans},z}^2) &= & 1,260 \\
 \chi_z &= 1 / (\varphi + (\varphi^2 - \lambda_{\text{trans},z}^2)^{0,5}) &= & 0,5111 \\
 \chi_{\text{min}} &= \text{MIN}(\chi_y, \chi_z) &= & 0,5111
 \end{aligned}$$

Check bending and buckling:

$$\begin{aligned}
 \psi &= 0,00 \\
 \beta_{My} &= 1,8 - 0,7 * \psi &= & 1,80 \\
 \mu_y &= \lambda_{\text{trans},y} * (2 * \beta_{My} - 4) + (W_{\text{ply}2} - W_{\text{ely}2}) / W_{\text{ely}2} &= & 0,022 < 0,9 \\
 k_y &= 1 - (\mu_y * N_{\text{sd}}) / (\chi_y * A_2 * f_y) &= & 1,000 < 1,5
 \end{aligned}$$

$$N_{\text{sd}} / (\chi_{\text{min}} * A_2 * f_y / 10 / \gamma_M) + 100 * k_y * \text{ABS}(M_D) / (W_{\text{ply}2} * f_y / 10 / \gamma_M) = \underline{\underline{0,32 < 1}}$$

Check torsional-flexural buckling:

$$\begin{aligned}
 C_1 &= 1,879 \\
 M_{\text{cr}} &= (C_1 * \pi^2 * E_s * I_{z2} / (h * 100)^2 / 10 * (I_{\omega 2} / I_{z2} + ((h * 100)^2 * G * I_{t2} / (\pi^2 * E_s * I_{z2})))^{0,5}) = 94241,31 \text{ kNcm}
 \end{aligned}$$

As in Table: F.1.1

$$\begin{aligned}
 \psi &= 0,00 \\
 \beta_w &= 1,00 \\
 k &= 1,00 \\
 \lambda_{\text{LT}} &= \sqrt{(\pi^2 * E_s / 10 * W_{\text{ply}2} / M_{\text{cr}})} &= & 50,78 \\
 \lambda_{\text{trans,LT}} &= \lambda_{\text{LT}} / \lambda_1 * \sqrt{\beta_w} &= & 0,541
 \end{aligned}$$

Apply strut curve a

$$\begin{aligned}
 \alpha &= 0,21 \\
 \varphi &= 0,5 * (1 + \alpha * (\lambda_{\text{trans,LT}} - 0,2) + \lambda_{\text{trans,LT}}^2) &= & 0,682 \\
 \chi_{\text{LT}} &= 1 / (\varphi + (\varphi^2 - \lambda_{\text{trans,LT}}^2)^{0,5}) &= & 0,9114 \\
 \beta_{\text{M,LT}} &= 1,8 - 0,7 * \psi &= & 1,80 \\
 \mu_{\text{LT}} &= 0,15 * \lambda_{\text{trans},z} * \beta_{\text{M,LT}} - 0,15 &= & 0,134 < 0,9 \\
 k_{\text{LT}} &= 1 - (\mu_{\text{LT}} * N_{\text{sd}}) / (\chi_{\text{LT}} * A_2 * f_y) &= & 1,000 < 1,5
 \end{aligned}$$

$$N_{\text{sd}} / (\chi_z * A_2 * f_y / 10 / \gamma_M) + 100 * k_{\text{LT}} * \text{ABS}(M_D) / (\chi_{\text{LT}} * W_{\text{ply}2} * f_y / 10 / \gamma_M) = \underline{\underline{0,346 < 1}}$$

Section analysis at D:**Column:**

$$A_v = 1,04 * h_2 * s_2 / 10^2 = 24,96 \text{ cm}^2$$

$$V_{pl,Rd} = A_v * f_y / 10 / \sqrt{3} / \gamma_M = 307,86 \text{ kN}$$

$$V_{sd} / V_{pl,Rd} = \underline{0,037 < 0,5}$$

No interaction

$$N_{pl,Rd} = A_2 * f_y / 10 / \gamma_M = 2264,55 \text{ kN}$$

$$n = N_{sd} / N_{pl,Rd} = 0,02$$

$$M_{pl,y,Rd} = W_{ply2} * f_y / (\gamma_M * 10^3) = 250,49 \text{ kNm}$$

$$M_{Ny,Rd} = 1,11 * M_{pl,y,Rd} * (1 - n) = 272,48 \text{ kNm}$$

$$ABS(M_D) / \text{MIN}(M_{pl,y,Rd}; M_{Ny,Rd}) = \underline{0,28 < 1}$$

Beam:

$$A_v = 1,04 * h_1 * s_1 / 10^2 = 15,48 \text{ cm}^2$$

$$V_{pl,Rd} = A_v * f_y / 10 / \sqrt{3} / \gamma_M = 190,93 \text{ kN}$$

$$N_{sd} / V_{pl,Rd} = \underline{0,225 < 0,5}$$

No interaction

$$N_{pl,Rd} = A_1 * f_y / 10 / \gamma_M = 835,32 \text{ kN}$$

$$n = V_{sd} / N_{pl,Rd} = 0,014$$

$$M_{pl,y,Rd} = W_{ply1} * f_y / (\gamma_M * 10^3) = 78,91 \text{ kNm}$$

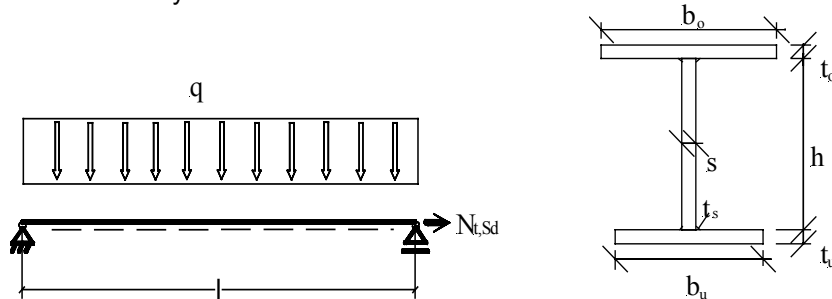
$$M_{Ny,Rd} = 1,11 * M_{pl,y,Rd} * (1 - n) = 86,36 \text{ kNm}$$

$$ABS(M_D) / \text{MIN}(M_{pl,y,Rd}; M_{Ny,Rd}) = \underline{0,89 < 1}$$

Single-span beam

Pos.: Flexural-torsional buckling of a single-span beam:

End supports are laterally fixed.



Load diagram:

Span length $l =$	24,00 m
top width $b_o =$	40,00 cm
bottom width $b_u =$	50,00 cm
Depth of web $h =$	100,00 cm
top Flange thickness $t_o =$	3,50 cm
bottom Flange thickness $t_u =$	3,50 cm
Web thickness $s =$	2,00 cm
Weld thickness $t_s =$	1,00 cm

Loads:

$q =$	4,04 kN/m
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Materials and stresses:

steel =	SEL("steel/EC"; Name;)	=	Fe 510
$E_s =$	TAB("steel/EC"; E; Name=steel)	=	210000,00 N/mm ²
$G =$	TAB("steel/EC"; G; Name=steel)	=	81000,00 N/mm ²
$f_y =$	TAB("steel/EC"; f_y ; Name=steel)	=	355,00 N/mm ²
$\epsilon =$	$\sqrt{(235/f_y)}$	=	0,81
Partial safety factors:			
$\gamma_M =$	1,10		
$\gamma_G =$	1,35		

Section classification as in Table 5.3.1:

$A =$	$(b_o * t_o + b_u * t_u + h * s)$	=	515,00 cm ²
Plastic neutral axis:			
$x =$	$(A / 2 - (b_o * t_o)) / s$	=	58,75 cm
$x_s =$	$h - x$	=	41,25 cm
Flange:			
$c =$	$((b_o - s) / 2 - t_s * \sqrt{2}) / t_o$	=	5,02 cm
$c / (9 * \epsilon)$		=	0,69 < 1
⇒ Section class 1			
Web:			
$\alpha =$	x / h	=	0,59 cm
$h / s / (456 * \epsilon / (13 * \alpha - 1))$		=	0,90 < 1
$h / s / (396 * \epsilon / (13 * \alpha - 1))$		=	1,04 > 1
⇒ Section class 2			

Check bending moment strength:

$$M_{sd} = \gamma_g \cdot q \cdot l^2 / 8 = 392,69 \text{ kNm}$$

Critical torsional-buckling moment:

$$I_z = t_o \cdot b_o^3 / 12 + t_u \cdot b_u^3 / 12 = 55125,00 \text{ cm}^4$$

As in Table: F.1.2(2)

$$k = 1,00$$

As in Table: F.1.1(4)

$$k_w = 1,00$$

As in Table: F.1.2

$$C_1 = 1,132$$

$$C_2 = 0,459$$

$$C_3 = 0,525$$

Location of center of gravity:

$$e = (b_u \cdot t_u \cdot (h + t_o) + h \cdot s \cdot (h + t_o) / 2) / A = 55,27 \text{ cm}$$

Location of shear centre:

$$s_s = (h + (t_o + t_u) / 2) \cdot (b_u^3 / (b_o^3 + b_u^3)) = 68,45 \text{ cm}$$

$$z_s = -(s_s - e) = -13,18 \text{ cm}$$

$$I_t = 1/3 \cdot (b_u \cdot t_u^3 + b_o \cdot t_o^3 + h \cdot s^3) = 1552,92 \text{ cm}^4$$

$$z_a = 0,00 \text{ cm}$$

$$z_g = z_a - z_s = 13,18 \text{ cm}$$

as in F 1.4:

$$\beta_f = b_o^3 / (b_o^3 + b_u^3) = 0,339 < 0,5$$

$$z_j = (2 \cdot \beta_f - 1) \cdot (h + (t_o + t_u) / 2) / 2 = -16,66 \text{ cm}$$

$$I_w = \beta_f \cdot (1 - \beta_f) \cdot I_z \cdot (h + (t_o + t_u) / 2)^2 = 132,32 \cdot 10^6 \text{ cm}^6$$

$$P_1 = C_1 \cdot (\pi^2 \cdot E_s \cdot I_z / (k \cdot l \cdot 100)^2) = 22453,85$$

$$P_2 = (k/k_w)^{2*} \cdot (I_w/I_z + ((k \cdot 100)^{2*} \cdot G \cdot I_t) / (\pi^2 \cdot E_s \cdot I_z) + (C_2 \cdot z_g - C_3 \cdot z_j)^2)^{0,5} = 94,66$$

$$P_3 = C_2 \cdot z_g - C_3 \cdot z_j = 14,80$$

$$M_{cr} = P_1 \cdot (P_2 - P_3) / 10^3 = 1793,16 \text{ kNm}$$

$$W_{pl} = b_u \cdot t_u \cdot (x_s + t_u/2) + x_s^2 \cdot s/2 + b_o \cdot t_o \cdot (x + t_o/2) + x^2 \cdot s/2 = 21148,13 \text{ cm}^3$$

$$\text{Section class 2 } \beta_w = 1,00$$

$$\lambda_{trans,LT} = (\beta_w \cdot W_{pl} \cdot f_y / (10^3 \cdot M_{cr}))^{0,5} = 2,046$$

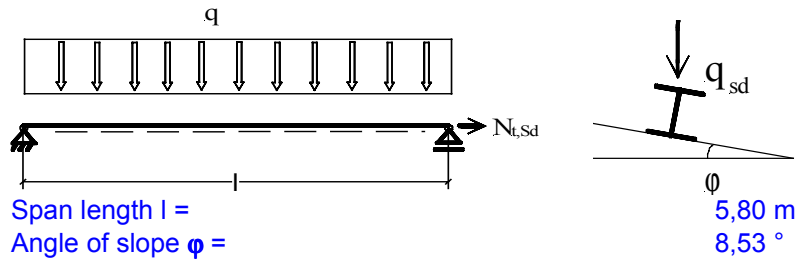
$$\text{As in Table 5.5.1 } \alpha = 0,49$$

$$\varphi = 0,5 \cdot (1 + \alpha \cdot (\lambda_{trans,LT} - 0,2) + \lambda_{trans,LT}^2) = 3,05$$

$$\chi_{LT} = 1 / (\varphi + (\varphi^2 - \lambda_{trans,LT}^2)^{0,5}) = 0,1883$$

$$M_{b,Rd} = \beta_w \cdot \chi_{LT} \cdot W_{pl} \cdot f_y / 10 / (\gamma_M \cdot 10)^2 = 1168,33 \text{ kNm}$$

$$M_{sd} / M_{b,Rd} = \underline{\underline{0,34 < 1}}$$

Pos.: Single-span beam with biaxial bending:**Loads:**

$$q_{sd} = 7,00 \text{ kN/m}$$

$$N_{t,sd} = 100,00 \text{ kN}$$

Materials and stresses:

$$\text{steel} = \text{SEL}(\text{"steel/EC"; Name; }) = \text{Fe 360}$$

$$E_s = \text{TAB}(\text{"steel/EC"; E; Name=steel}) = 210000,00 \text{ N/mm}^2$$

$$f_y = \text{TAB}(\text{"steel/EC"; f_y; Name=steel}) = 235,00 \text{ N/mm}^2$$

$$\varepsilon = \sqrt{(235/f_y)} = 1,00$$

$$\text{platischer Formbeiwert } \alpha_{ply} = 1,14$$

$$\text{platischer Formbeiwert } \alpha_{plz} = 1,25$$

$$\gamma_M = 1,10$$

$$\text{Profil Typ} = \text{SEL}(\text{"steel/Profils"; Name; }) = \text{HEA}$$

$$\text{Selected Profil} = \text{SEL}(\text{"steel/"Typ; Name; }) = \text{HEA 140}$$

Section classification:

$$\text{Column height } h = \text{TAB}(\text{"steel/"Typ; h; Name=Profil}) = 133,00 \text{ mm}$$

$$\text{Depth of web } h_1 = \text{TAB}(\text{"steel/"Typ; h1; Name=Profil}) = 92,00 \text{ mm}$$

$$\text{Web thickness } s = \text{TAB}(\text{"steel/"Typ; s; Name=Profil}) = 5,50 \text{ mm}$$

$$\text{Flange width } b = \text{TAB}(\text{"steel/"Typ; b; Name=Profil}) = 140,00 \text{ mm}$$

$$\text{Flange thickness } t = \text{TAB}(\text{"steel/"Typ; t; Name=Profil}) = 8,50 \text{ mm}$$

$$\text{Moment of inertia } I = \text{TAB}(\text{"steel/"Typ; I_y; Name=Profil}) = 1030,00 \text{ cm}^4$$

$$\text{Cross-sectional area } A = \text{TAB}(\text{"steel/"Typ; A; Name=Profil}) = 31,40 \text{ cm}^2$$

$$W_{ely} = \text{TAB}(\text{"steel/"Typ; W_y; Name=Profil}) = 155,00 \text{ cm}^3$$

$$W_{ply} = \alpha_{ply} * W_{ely} = 176,70 \text{ cm}^3$$

$$W_{elz} = \text{TAB}(\text{"steel/"Typ; W_z; Name=Profil}) = 55,60 \text{ cm}^3$$

$$W_{plz} = \alpha_{plz} * W_{elz} = 69,50 \text{ cm}^3$$

Design loads:**Plastic limit force:**

$$N_{pl,Rd} = A * f_y / \gamma_M / 10 = 670,82 \text{ kN}$$

Limit force that plasticizes the web

$$N_{pl,w,Rd} = (h - 2 * t) * s * f_y / \gamma_M / 10^3 = 136,30 \text{ kN}$$

$$N_{t,sd} / \text{MIN}(0,5 * N_{pl,w,Rd}; N_{pl,Rd} / 4) = \underline{\underline{1,47 > 1}}$$

⇒ Reduce plastic limit force as in 5.4.8.1:

$$\alpha = (A - 2 * b * t / 100) / A = 0,242 < 0,5$$

$$\eta = N_{t,sd} / N_{pl,Rd} = 0,149$$

$$M_{Ny,Rd} = ((W_{ply} * f_y) / \gamma_M * (1 - \eta) / (1 - 0,5 * \alpha)) / 10^3 = 36,55 \text{ kNm}$$

$$\eta / \alpha = 0,62 < 1$$

$$\Rightarrow M_{Nz,Rd} = W_{plz} * f_y / (\gamma_M * 10^3) = 14,85 \text{ kNm}$$

Design moments:

$$\begin{aligned}
 q_{sdy} &= q_{sd} * \cos(\varphi) &= & 6,92 \text{ kN/m} \\
 q_{sdz} &= q_{sd} * \sin(\varphi) &= & 1,04 \text{ kN/m} \\
 M_{y,sd} &= q_{sdy} * l^2 / 8 &= & 29,10 \text{ kNm} \\
 M_{z,sd} &= q_{sdz} * l^2 / 8 &= & 4,37 \text{ kNm}
 \end{aligned}$$

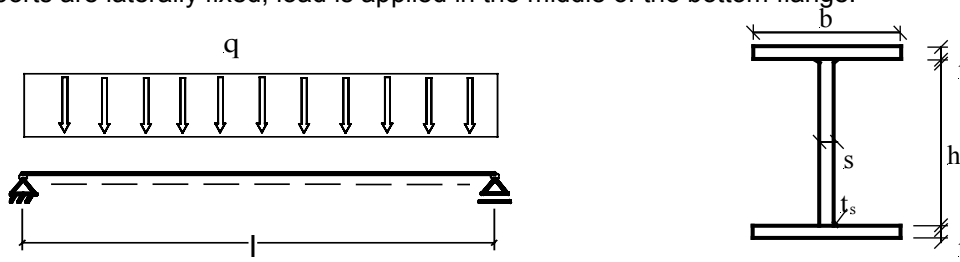
Check section strength:

$$\begin{aligned}
 &\text{for I-Profile gilt } \alpha = 2,00 \\
 \beta_1 &= 5 * \eta &= & 0,75 < 1 \\
 \beta_2 &= &= & 1,00 \\
 \beta &= \text{MAX}(\beta_1; \beta_2) &= & 1,00
 \end{aligned}$$

$$(M_{y,sd} / M_{Ny,Rd})^{(\alpha)} + (M_{z,sd} / M_{Nz,Rd})^{\beta} = \underline{\underline{0,93 < 1}}$$

Pos.: flexural-torsional buckling:

End supports are laterally fixed, load is applied in the middle of the bottom flange.

**Load diagram:**

Span length $l =$	8,00 m
Beam width $b =$	20,00 cm
Column height $h =$	50,00 cm
Flange thickness $t =$	2,50 cm
Web thickness $s =$	1,20 cm
Weld thickness $t_s =$	0,50 cm

Loads:

$q_{sd} =$	50,00 kN/m
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Materials and stresses:

steel =	SEL("steel/EC"; Name;)	=	Fe 510
$E_s =$	TAB("steel/EC"; E; Name=steel)	=	210000,00 N/mm ²
$G =$	TAB("steel/EC"; G; Name=steel)	=	81000,00 N/mm ²
$f_y =$	TAB("steel/EC"; fy; Name=steel)	=	355,00 N/mm ²
$\varepsilon =$	$\sqrt{(235/f_y)}$	=	0,81
Partial safety factors:			
$\gamma_M =$			1,10

Section classification:**Flange:**

$$c = (b/2 - t_s \cdot \sqrt{2})/t = 3,72 \text{ cm}$$

$$c/(9 \cdot \varepsilon) = 0,51 < 1$$

⇒ Section class 1

Web:

$$d = h - 2 \cdot t_s \cdot \sqrt{2} = 48,59 \text{ cm}$$

$$d/s/(72 \cdot \varepsilon) = 0,69 < 1$$

⇒ Section class 1

Check bending moment strength:

$$W_{pl} = (b \cdot t \cdot (h + t) / 2 + (h / 2) \cdot s \cdot (h / 4)) \cdot 2 = 3375,00 \text{ cm}^3$$

$$M_{c,Rd} = (W_{pl} \cdot f_y / \gamma_M) / 10^3 = 1089,20 \text{ kNm}$$

$$M_{sd} = q_{sd} \cdot l^2 / 8 = 400,00 \text{ kNm}$$

$$M_{sd} / M_{c,Rd} = \underline{\underline{0,37 < 1}}$$

Check shear strength:

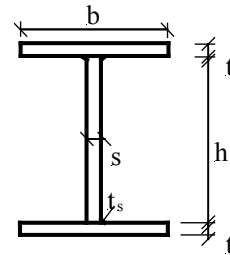
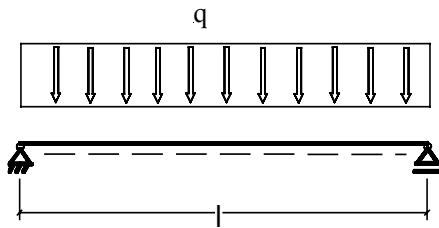
$$\begin{aligned}
 A_V &= h * s & = & 60,00 \text{ cm}^2 \\
 V_{pl,Rd} &= A_V * (f_y / \sqrt{3}) / \gamma_M / 10 & = & 1117,96 \text{ kN} \\
 V_{sd} &= q_{sd} * l / 2 & = & 200,00 \text{ kN} \\
 V_{sd} / V_{pl,Rd} & & = & \underline{0,18 < 1}
 \end{aligned}$$

Check torsional buckling strength:

$$\begin{aligned}
 I_Z &= 2 * t * b^3 / 12 & = & 3333,33 \text{ cm}^4 \\
 I_W &= I_Z * (h + t)^2 / 4 & = & 2,297 * 10^6 \text{ cm}^6 \\
 I_t &= 1/3 * (2 * b * t^3 + h * s^3) & = & 237,13 \text{ cm}^4 \\
 \text{As in Table F.1.2(2) } k &= & 1,00 \\
 \text{As in Table F.1.1(4) } k_W &= & 1,00 \\
 \text{As in Table F.1.2 } C_1 &= & 1,13 \\
 \text{As in Table F.1.2 } C_2 &= & 0,46 \\
 \text{As in Table F.1.2 } C_3 &= & 0,53 \\
 \text{Load is applied in centroid of section } z_a &= & -27,50 \text{ cm} \\
 \text{Centroid of section and shear centre are identical } z_s &= & 0,00 \text{ cm} \\
 \text{Section is symmetrical } z_j &= & 0,00 \text{ cm} \\
 z_g &= z_a - z_s & = & -27,50 \text{ cm} \\
 \text{Critical torsional-buckling moment} \\
 P_1 &= C_1 * (\pi^2 * E_s * I_Z / (k * l^2)) / 10 & = & 12,20 \\
 P_2 &= (k/k_W)^2 * (I_W / I_Z + ((k * l^2 / 100)^2 * G * I_t) / (\pi^2 * E_s * I_Z) + (C_2 * z_g - C_3 * z_j)^2)^{0,5} & = & 51,27 \\
 P_3 &= C_2 * z_g - C_3 * z_j & = & -12,65 \\
 M_{cr} &= P_1 * (P_2 - P_3) & = & 779,82 \text{ kNm} \\
 \text{Cross-section class 1 } \beta_W &= & 1,00 \\
 \lambda_{trans,LT} &= (\beta_W * W_{pl} * f_y / M_{cr} / 10^3)^{0,5} & = & 1,240 \\
 \text{Apply strut curve c:} \\
 \alpha_{LT} &= & 0,49 \\
 \phi_{LT} &= 0,5 * (1 + \alpha_{LT} * (\lambda_{trans,LT}^{-0,2} + \lambda_{trans,LT}^2)) & = & 1,524 \\
 \chi_{LT} &= 1 / (\phi_{LT} + (\phi_{LT}^2 - \lambda_{trans,LT}^2)^{0,5}) & = & 0,415 \\
 M_{b,Rd} &= \beta_W * \chi_{LT} * W_{pl} * f_y / \gamma_M / 10 & = & 45201,99 \text{ kNcm} \\
 M_{sd} * 100 / M_{b,Rd} & & = & \underline{0,88 < 1}
 \end{aligned}$$

Pos.: Flexural-torsional buckling of a single-span beam:

End supports are laterally fixed, Load is applied in centroid of section.

**Load diagram:**

Span length $l =$	8,00 m
Beam width $b =$	20,00 cm
Column height $h =$	50,00 cm
Flange thickness $t =$	2,50 cm
Web thickness $s =$	1,20 cm
Weld thickness $t_s =$	0,50 cm

Loads:

$q_{sd} =$	45,00 kN/m
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Materials and stresses:

steel =	SEL("steel/EC"; Name;)	=	Fe 510
$E_s =$	TAB("steel/EC"; E; Name=steel)	=	210000,00 N/mm ²
$G =$	TAB("steel/EC"; G; Name=steel)	=	81000,00 N/mm ²
$f_y =$	TAB("steel/EC"; f_y ; Name=steel)	=	355,00 N/mm ²
$\epsilon =$	$\sqrt{(235/f_y)}$	=	0,81
Partial safety factors:			
$\gamma_M =$		=	1,10

Section classification As in Table 5.3.1:**Flange:**

$c =$	$(b/2 - t_s \cdot \sqrt{2})/t$	=	3,72 cm
$c/(9 \cdot \epsilon)$		=	0,51 < 1

Section class 1

Web:

$d =$	$h - 2 \cdot t_s \cdot \sqrt{2}$	=	48,59 cm
$d/s/(72 \cdot \epsilon)$		=	0,69 < 1

Section class 1

Check bending moment strength:

$W_{pl} =$	$(b \cdot t \cdot (h+t)/2 + (h/2) \cdot s \cdot (h/4)) \cdot 2$	=	3375,00 cm ³
$M_{c,Rd} =$	$(W_{pl} \cdot f_y / \gamma_M) / 10^3$	=	1089,20 kNm
$M_{sd} =$	$q_{sd} \cdot l^2 / 8$	=	360,00 kNm

$$M_{sd} / M_{c,Rd} = \underline{0,33 < 1}$$

Check shear strength:

$$\begin{aligned}
 A_v &= h \cdot s & = & 60,00 \text{ cm}^2 \\
 V_{pl,Rd} &= A_v \cdot (f_y / \sqrt{3}) / \gamma_M / 10 & = & 1117,96 \text{ kN} \\
 V_{sd} &= q_{sd} \cdot l / 2 & = & 180,00 \text{ kN} \\
 V_{sd} / V_{pl,Rd} & & = & \underline{0,16 < 1}
 \end{aligned}$$

Check torsional buckling strength:

$$\begin{aligned}
 I_z &= 2 \cdot t \cdot b^3 / 12 & = & 3333,33 \text{ cm}^4 \\
 I_w &= I_z \cdot (h + t)^2 / 4 & = & 2,297 \cdot 10^6 \text{ cm}^6 \\
 I_t &= 1/3 \cdot (2 \cdot b \cdot t^3 + h \cdot s^3) & = & 237,13 \text{ cm}^4 \\
 \text{As in Table F.1.2(2) } k &= & & 1,00 \\
 \text{As in Table F.1.1(4) } k_w &= & & 1,00 \\
 \text{As in Table F.1.2 } C_1 &= & & 1,13 \\
 \text{As in Table F.1.2 } C_2 &= & & 0,46 \\
 \text{As in Table F.1.2 } C_3 &= & & 0,53 \\
 \text{Load in centroid } z_a &= & & 0,00 \text{ cm} \\
 \text{Centroid of section and shear centre are identical } z_s &= & & 0,00 \text{ cm} \\
 \text{Section is symmetrical } z_j &= & & 0,00 \text{ cm}
 \end{aligned}$$

Critical torsional-buckling moment

$$M_{cr} = C_1 \cdot (\pi^2 \cdot E_s \cdot I_z / (k \cdot l \cdot 10^2)^2) \cdot ((k/k_w)^2 \cdot I_w / I_z + ((k \cdot l \cdot 10^2)^2 \cdot G \cdot I_t) / (\pi^2 \cdot E_s \cdot I_z))^{0,5} / 10^3 = 606,05 \text{ kNm}$$

$$\text{Cross-section class 1 } \beta_w = 1,00$$

$$\lambda_{trans,LT} = (\beta_w \cdot W_{pl} \cdot f_y / M_{cr} / 10^3)^{0,5} = 1,406$$

Apply strut curve c:

$$\alpha_{LT} = 0,49$$

$$\phi_{LT} = 0,5 \cdot (1 + \alpha_{LT} \cdot (\lambda_{trans,LT}^{0,2} + \lambda_{trans,LT}^2)) = 1,784$$

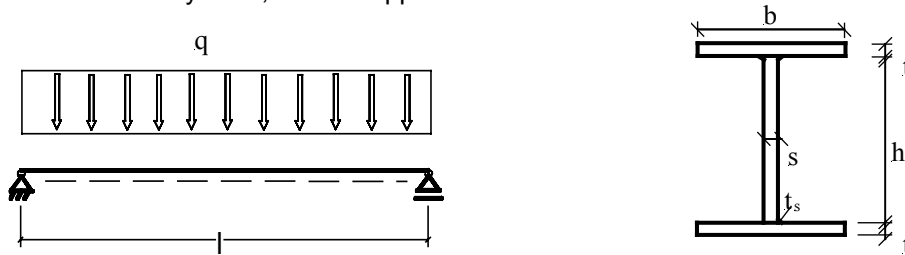
$$\chi_{LT} = 1 / (\phi_{LT} + (\phi_{LT}^2 - \lambda_{trans,LT}^2)^{0,5}) = 0,347$$

$$M_{b,Rd} = \beta_w \cdot \chi_{LT} \cdot W_{pl} \cdot f_y / \gamma_M / 10^3 = 377,95 \text{ kNm}$$

$$M_{sd} / M_{b,Rd} = \underline{0,95 < 1}$$

Pos.: Flexural-torsional buckling of a single-span beam:

End supports are laterally fixed, Load is applied in centroid of section.

**Load diagram:**

Span length $l =$	8,00 m
Beam width $b =$	20,00 cm
Column height $h =$	50,00 cm
Flange thickness $t =$	2,50 cm
Web thickness $s =$	1,20 cm
Weld thickness $t_s =$	0,50 cm

Loads:

$q_{sd} =$	36,00 kN/m
------------	------------

Materials and stresses:

steel =	SEL("steel/EC"; Name;)	=	Fe 510
$E_s =$	TAB("steel/EC"; E; Name=steel)	=	210000,00 N/mm ²
$G =$	TAB("steel/EC"; G; Name=steel)	=	81000,00 N/mm ²
$f_y =$	TAB("steel/EC"; f_y ; Name=steel)	=	355,00 N/mm ²
$\epsilon =$	$\sqrt{(235/f_y)}$	=	0,81
Partial safety factors:			
$\gamma_M =$			1,10

Section classification As in Table 5.3.1:**Flange:**

$c =$	$(b/2 - t_s \cdot \sqrt{2})/t$	=	3,72 cm
$c/(9 \cdot \epsilon)$		=	0,51 < 1

Section class 1

Web:

$d =$	$h - 2 \cdot t_s \cdot \sqrt{2}$	=	48,59 cm
$d/s/(72 \cdot \epsilon)$		=	0,69 < 1

Section class 1

Check bending moment strength:

$W_{pl} =$	$(b \cdot t \cdot (h+t)/2 + (h/2) \cdot s \cdot (h/4)) \cdot 2$	=	3375,00 cm ³
$M_{c,Rd} =$	$(W_{pl} \cdot f_y / \gamma_M) / 10^3$	=	1089,20 kNm
$M_{sd} =$	$q_{sd} \cdot l^2 / 8$	=	288,00 kNm
$M_{sd}/M_{c,Rd}$		=	<u>0,26 < 1</u>

Check shear strength:

$$\begin{aligned}
 A_V &= h \cdot s & = & 60,00 \text{ cm}^2 \\
 V_{pl,Rd} &= A_V \cdot (f_y / \sqrt{3}) / \gamma_M / 10 & = & 1117,96 \text{ kN} \\
 V_{sd} &= q_{sd} \cdot l / 2 & = & 144,00 \text{ kN} \\
 V_{sd} / V_{pl,Rd} & & = & \underline{0,13} < 1
 \end{aligned}$$

Check torsional buckling strength:

$$\begin{aligned}
 I_z &= 2 \cdot t \cdot b^3 / 12 & = & 3333,33 \text{ cm}^4 \\
 I_w &= I_z \cdot (h + t)^2 / 4 & = & 2,297 \cdot 10^6 \text{ cm}^6 \\
 I_t &= 1/3 \cdot (2 \cdot b \cdot t^3 + h \cdot s^3) & = & 237,13 \text{ cm}^4 \\
 \text{As in Table F.1.2(2) } k &= & & 1,00 \\
 \text{As in Table F.1.1(4) } k_w &= & & 1,00 \\
 \text{As in Table F.1.2 } C_1 &= & & 1,13 \\
 \text{As in Table F.1.2 } C_2 &= & & 0,46 \\
 \text{As in Table F.1.2 } C_3 &= & & 0,53 \\
 \text{Load in centroid } z_a &= & & 27,50 \text{ cm} \\
 \text{Centroid of section and shear centre are identical } z_s &= & & 0,00 \\
 \text{cm} & & & \\
 \text{Section is symmetrical } z_j &= & & 0,00 \text{ cm} \\
 z_g &= z_a - z_s & = & 27,50 \text{ cm}
 \end{aligned}$$

Critical torsional-buckling moment

$$\begin{aligned}
 P_1 &= C_1 \cdot (\pi^2 \cdot E_s \cdot I_z / (k \cdot l \cdot 100)^2) & = & 12198,18 < 1 \\
 P_2 &= (k/k_w)^2 \cdot (I_w / I_z + ((k \cdot l \cdot 100)^2 \cdot G \cdot I_t) / (\pi^2 \cdot E_s \cdot I_z) + (C_2 \cdot z_g - C_3 \cdot z_j)^2)^{0,5} & = & 51,27 < 1 \\
 P_3 &= C_2 \cdot z_g - C_3 \cdot z_j & = & 12,65 \\
 M_{cr} &= P_1 \cdot (P_2 - P_3) / 10^3 & = & 471,09 \text{ kNm} \\
 \text{Cross-section class 1 } \beta_w &= & & 1,00
 \end{aligned}$$

$$\lambda_{trans,LT} = (\beta_w \cdot W_{pl} \cdot f_y / M_{cr} / 10^3)^{0,5} = 1,595 < 1$$

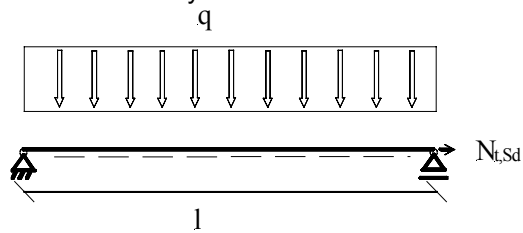
Apply strut curve c:

$$\begin{aligned}
 \alpha_{LT} &= & & 0,49 \\
 \phi_{LT} &= 0,5 \cdot (1 + \alpha_{LT} \cdot (\lambda_{trans,LT} - 0,2) + \lambda_{trans,LT}^2) & = & 2,114 \\
 \chi_{LT} &= 1 / (\phi_{LT} + (\phi_{LT}^2 - \lambda_{trans,LT}^2)^{0,5}) & = & 0,286 \\
 M_{b,Rd} &= \beta_w \cdot \chi_{LT} \cdot W_{pl} \cdot f_y / \gamma_M / 10^3 & = & 311,51 \text{ kNm}
 \end{aligned}$$

$$M_{sd} / M_{b,Rd} = \underline{0,92} < 1$$

Pos.: Single-span beam subject to flexural-torsional buckling with uniform load and compression:

End supports are laterally fixed.



Load diagram:

Span length $l =$	24,00 m
top Flange width $b_o =$	40,00 cm
bottom Flange width $b_u =$	50,00 cm
Depth of web $h =$	100,00 cm
top Flange thickness $t_o =$	3,50 cm
bottom Flange thickness $t_u =$	3,50 cm
Web thickness $s =$	2,00 cm
Weld thickness $t_s =$	1,00 cm

Loads:

$q_{sd} =$	18,00 kN/m
$N_{t,sd} =$	500,00 kN

Materials and stresses:

steel =	SEL("steel/EC"; Name;)	=	Fe 510
$E_s =$	TAB("steel/EC"; E; Name=steel)	=	210000,00 N/mm ²
$G =$	TAB("steel/EC"; G; Name=steel)	=	81000,00 N/mm ²
$f_y =$	TAB("steel/EC"; fy; Name=steel)	=	355,00 N/mm ²

$$\epsilon = \sqrt{(235/f_y)} = 0,81$$

Partial safety factors:

$\gamma_M =$	1,10
$\gamma_G =$	1,35

$$A = (b_o * t_o + b_u * t_u + h * s) = 515,00 \text{ cm}^2$$

Location of center of gravity:

$$e = (b_u * t_u * (h + t_o) + h * s * (h + t_o) / 2) / A = 55,27 \text{ cm}$$

Location of shear centre:

$$s_s = (h + (t_o + t_u) / 2) * (b_u^3 / (b_o^3 + b_u^3)) = 68,45 \text{ cm}$$

Plastic neutral axis:

$$x = (A / 2 - (b_o * t_o)) / s = 58,75 \text{ cm}$$

Section classification As in Table 5.3.1:

Flange:

$$c = ((b_o - s) / 2 - t_s * \sqrt{2}) / t_o = 5,02 \text{ cm}$$

$$c / (9 * \epsilon) = 0,69 < 1$$

Section class 1

Web:

$$\alpha = x / h = 0,59 \text{ cm}$$

$$h / s / (456 * \epsilon / (13 * \alpha - 1)) = 0,90 < 1$$

$$h / s / (396 * \epsilon / (13 * \alpha - 1)) = 1,04 > 1$$

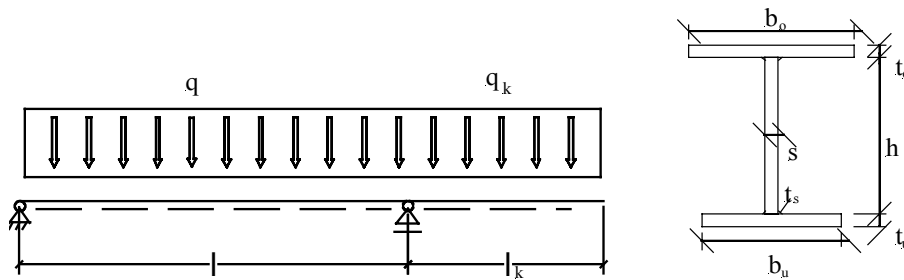
Section class 2

Check bending moment strength:

$$\begin{aligned}
 M_{sd} &= q_{sd} * l^2 / 8 &= & 1296,00 \text{ kNm} \\
 I_z &= t_o * b_o^3 / 12 + t_u * b_u^3 / 12 &= & 55125,00 \text{ cm}^4 \\
 I_y &= b_o * t_o * e^2 + b_u * t_u * (h + t_u - e)^2 + s * h^3 / 12 + h * s * (e - (h/2 + t_u/2))^2 &= & 1003886,210 \text{ cm}^4 \\
 W_{com} &= I_y / (e + t_o / 2) &= & 17605,86 \text{ cm}^3
 \end{aligned}$$

Effective bending moment:

$$\begin{aligned}
 M_{sd} &= q_{sd} * l^2 / 8 &= & 1296,00 \text{ kNm} \\
 \text{Assumption as in 5.5.3 } \psi_{vec} &= & & 0,80 \\
 \sigma_{com,Ed} &= M_{sd} * 100 / W_{com} - \psi_{vec} * N_{t,sd} / A &= & 6,58 \text{ kN/cm}^2 \\
 M_{eff,sd} &= W_{com} * \sigma_{com,Ed} / 100 &= & 1158,47 \text{ kNm} \\
 \text{As in Table F.1.2(2) } k &= & & 1,00 \\
 \text{As in Table F.1.1(4) } k_w &= & & 1,00 \\
 \text{As in Table: F.1.2} & & & \\
 C_1 &= & & 1,132 \\
 C_2 &= & & 0,459 \\
 C_3 &= & & 0,525 \\
 z_s &= -(s_s - e) &= & -13,18 \text{ cm} \\
 I_t &= 1/3 * (b_u * t_u^3 + b_o * t_o^3 + h * s^3) &= & 1552,92 \text{ cm}^4 \\
 z_a &= & & 0,00 \text{ cm} \\
 z_g &= z_a - z_s &= & 13,18 \text{ cm} \\
 \beta_f &= b_o^3 / (b_o^3 + b_u^3) &= & 0,339 < 0,5 \\
 z_j &= (2 * \beta_f - 1) * (h + (t_o + t_u) / 2) / 2 &= & -16,66 \text{ cm} \\
 I_w &= \beta_f * (1 - \beta_f) * I_z * (h + (t_o + t_u) / 2)^2 &= & 0,1323 * 10^9 \text{ cm}^6 \\
 P_1 &= C_1 * (\pi^2 * E_s * I_z / (k * l^2 * 10^3)^2) / 10 &= & 22,45 \text{ kNm} \\
 P_2 &= (k / k_w)^{2*} * (I_w / I_z + ((k * l^2 * 100)^{2*} * G * I_t) / (\pi^2 * E_s * I_z) + (C_2 * z_g - C_3 * z_j)^2)^{0,5} &= & 94,66 \\
 P_3 &= C_2 * z_g - C_3 * z_j &= & 14,80 \\
 M_{cr} &= P_1 * (P_2 - P_3) &= & 1792,86 \text{ kNm} \\
 W_{pl} &= b_u * t_u * (x + t_u / 2) + x^2 * s / 2 + b_o * t_o * (h - x + t_o / 2) + (h - x)^2 * s / 2 &= & 21760,63 \text{ cm}^3 \\
 \text{Section class 2 } \beta_w &= & & 1,00 \\
 \lambda_{trans,LT} &= (\beta_w * W_{pl} * f_y / (M_{cr} * 10^3))^{0,5} &= & 2,076 \\
 \text{As in Table 5.5.1 } \alpha &= & & 0,49 \\
 \varphi &= 0,5 * (1 + \alpha * (\lambda_{trans,LT}^{0,2} + \lambda_{trans,LT}^2)) &= & 3,11 \\
 \chi_{LT} &= 1 / (\varphi + (\varphi^2 - \lambda_{trans,LT}^2)^{0,5}) &= & 0,1843 \\
 M_{b,Rd} &= \beta_w * \chi_{LT} * W_{pl} * f_y / (\gamma_M * 10)^2 / 10 &= & 1176,63 \text{ kNm} \\
 M_{eff,sd} / M_{b,Rd} &= & & \underline{0,98 < 1}
 \end{aligned}$$

Pos.: Single-span beam with cantilever, asymmetric section:

Span length $l =$	10,50 m
Cantilever length $l_k =$	5,00 m
top Flange width $b_o =$	50,00 cm
bottom Flange width $b_u =$	30,00 cm
top Flange thickness $t_o =$	2,00 cm
bottom Flange thickness $t_u =$	2,00 cm
Depth of web $h =$	60,00 cm
Web thickness $s =$	1,50 cm
Weld thickness $t_s =$	0,80 cm

Loads:

Dead weight $g =$	26,00 kN/m
Live load $q =$	37,70 kN/m
Snow load $s_0 =$	7,00 kN/m

Materials and stresses:

steel =	SEL("steel/EC"; Name;)	=	Fe 360
$E_s =$	TAB("steel/EC"; E; Name=steel)	=	210000,00 N/mm ²
$f_y =$	TAB("steel/EC"; f_y ; Name=steel)	=	235,00 N/mm ²

$$\varepsilon = \sqrt{(235/f_y)} = 1,00$$

Partial safety factors:

$\gamma_{fg} =$	1,35
$\gamma_{fq} =$	1,50
$\psi =$	0,90
$\gamma_M =$	1,10

Design loads:

$q_{d1} =$	$\gamma_{fg} * g + \gamma_{fq} * q$	=	91,65 kN/m
$q_{d2} =$	$\gamma_{fg} * g + \psi * \gamma_{fq} * (q + s_0)$	=	95,44 kN/m
$q_d =$	MAX(q_{d1} ; q_{d2})	=	95,44 kN/m
$M_{sdek} =$	$-q_d * l_k^2 / 2$	=	-1193,00 kNm
$B_v =$	$(l + l_k)^2 / 2 * q_d / l$	=	1091,88 kN
$B_r =$	$q_d * l_k$	=	477,20 kN
$B_l =$	$B_v - B_r$	=	614,68 kN
$A_v =$	$(l + l_k) * q_d - B_v$	=	387,44 kN
$M_{sdfeld} =$	$A_v * (A_v / q_d / 2)$	=	786,41 kNm

Plastic neutral axis:

$$\begin{aligned}
 A &= (b_o * t_o + b_u * t_u + h * s) &= & 250,00 \text{ cm}^2 \\
 x &= (A / 2 - (b_o * t_o)) / s &= & 16,67 \text{ cm} \\
 W_{pl} &= (b_o * t_o * (x + t_o / 2) + 0,5 * s * x^2 + b_u * t_u * (t_u / 2 + (h - x)) + 0,5 * s * (h - x)^2) &= & 6043,33 \text{ cm}^3 \\
 M_{pl} &= W_{pl} * f_y / 10^3 &= & 1420,18 \text{ kNm}
 \end{aligned}$$

Section classification Kragarm As in Table 5.3.1:**Bottom Flange:**

$$c = 0,5 * (b_u - s) - t_s * \sqrt{2} = 13,12 \text{ cm}$$

$$c / t_u / (9 * \epsilon) = 0,73 < 1$$

Web:

$$\alpha = (h - x) / h = 0,72$$

$$((h - 2 * t_s * \sqrt{2}) / s) / (396 * \epsilon / (13 * \alpha - 1)) = 0,81 < 1$$

⇒ Section class 1.

Check shear strength:

$$A_V = h * s = 90,00 \text{ cm}^2$$

$$V_{pl,Rd} = (A_V * f_y) / (10 * \sqrt{3} * \gamma_M) = 1110,09 \text{ kN}$$

$$V_{sd} = \text{MAX}(B_i; B_r; A_V) = 614,68 \text{ kN}$$

$$V_{sd} / (V_{pl,Rd} * 0,5) = \underline{1,11 > 1}$$

⇒ M_{pl}, reduced.

Check bending moment strength:

$$\rho = (2 * V_{sd} / V_{pl,Rd} - 1)^2 = 0,012$$

$$M_{V,Rd} = (1 - \rho) * M_{pl} / \gamma_M = 1275,58 \text{ kNm}$$

$$\text{ABS}(M_{sdk}) / M_{V,Rd} = \underline{0,94 < 1}$$

Section classification Feld As in Table 5.3.1:**topr Flange:**

$$c = 0,5 * (b_o - s) - t_s * \sqrt{2} = 23,12 \text{ cm}$$

$$c / t_o / (10 * \epsilon) = 1,16 > 1$$

$$c / t_o / (14 * \epsilon) = 0,83 < 1$$

⇒ Section class 3.

Web:

$$\alpha = x / h = 0,28 < 1$$

$$((h - 2 * t_s * \sqrt{2}) / s) / (396 * \epsilon / (13 * \alpha - 1)) = 0,26 < 1$$

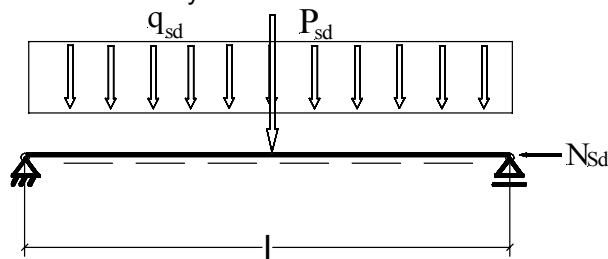
⇒ Section class 1.

Check section strength:

$$\text{ABS}(M_{sdfeld}) / (M_{pl} / \gamma_M) = \underline{0,61 < 1}$$

Pos.: Analysis single-span beam:

End supports are laterally fixed.

**Load diagram:**Span length $l =$ 6,00 m**Loads:**

$q_{sd} =$ 10,00 kN/m
 $N_{sd} =$ 273,00 kN
 $P_{sd} =$ 15,00 kN

Materials and stresses:

$steel =$ SEL("steel/EC"; Name;) = Fe 360
 $E_s =$ TAB("steel/EC"; E; Name=steel) = 210000,00 N/mm²
 $f_y =$ TAB("steel/EC"; fy; Name=steel) = 235,00 N/mm²
 $\epsilon =$ $\sqrt{(235/f_y)}$ = 1,00
 Partial safety factors:
 $\gamma_M =$ 1,10
 Plastic shape factor $\alpha_{pl} =$ 1,14

Section classification:

Profil Typ = SEL("steel/Profils"; Name;) = IPE
 Selected Profil = SEL("steel/"Typ; Name;) = IPE 300
 Column height $h =$ TAB("steel/"Typ; h; Name=Profil) = 300,00 mm
 Depth of web $h_1 =$ TAB("steel/"Typ; h1; Name=Profil) = 248,00 mm
 Web thickness $s =$ TAB("steel/"Typ; s; Name=Profil) = 7,10 mm
 Flange width $b =$ TAB("steel/"Typ; b; Name=Profil) = 150,00 mm
 Flange thickness $t =$ TAB("steel/"Typ; t; Name=Profil) = 10,70 mm
 Moment of inertia $I =$ TAB("steel/"Typ; Iy; Name=Profil) = 8360,00 cm⁴
 Cross-sectional area $A =$ TAB("steel/"Typ; A; Name=Profil) = 53,800 cm²
 $i_y =$ TAB("steel/"Typ; iy; Name=Profil) = 12,50 cm
 $i_z =$ TAB("steel/"Typ; iz; Name=Profil) = 3,35 cm
 $W_{el} =$ TAB("steel/"Typ; Wy; Name=Profil) = 557,00 cm³
 $W_{pl} =$ $\alpha_{pl} * W_{el}$ = 634,98 cm³

Section classification As in Table 5.3.1:

Web:
 $(h_1 / s) / (33 * \epsilon) =$ 1,06 ~ 1
 ⇒ Section class 1.
Flange:
 $(b / 2 / t) / (10 * \epsilon) =$ 0,70 < 1
 ⇒ Section class 1.

Check bending moment strength:

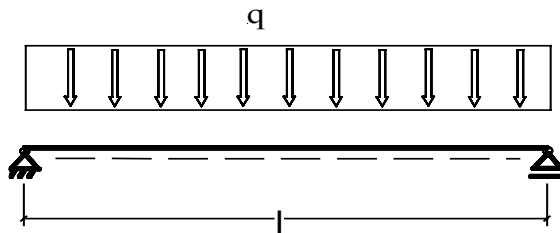
$$\begin{aligned}
 M_{sd} &= q_{sd} * l^2 / 8 + P_{sd} * l / 4 &= & 67,50 \text{ kNm} \\
 M_{pl,y,Rd} &= W_{pl} * f_y / \gamma_M / 10^3 &= & 135,65 \text{ kNm} \\
 N_{pl,Rd} &= A * f_y / \gamma_M / 10 &= & 1149,36 \text{ kN} \\
 n &= N_{sd} / N_{pl,Rd} &= & 0,238 \\
 \alpha &= (A - 2 * b * t / 10^2) / A &= & 0,403 < 0,5 \\
 \text{Reduced limit moment due to tension force:} & & & \\
 M_{N,y,Rd} &= M_{pl,y,Rd} * (1 - n) / (1 - 0,5 * \alpha) &= & 129,45 \text{ kNm} \\
 \\
 M_{sd} / M_{N,y,Rd} & &= & \underline{0,52 \leq 1}
 \end{aligned}$$

Check shear strength:

$$\begin{aligned}
 V_{sd} &= (P_{sd} + q_{sd} * l) / 2 &= & 37,50 \text{ kN} \\
 A_v &= 1,04 * h * s / 10^2 &= & 22,15 \text{ cm}^2 \\
 V_{pl,Rd} &= A_v * (f_y / \sqrt{3}) / \gamma_M / 10 &= & 273,20 \text{ kN} \\
 V_{sd} / V_{pl,Rd} & &= & \underline{0,14 \leq 1} \\
 \text{Where max M occurs:} & & & \\
 V_s &= P_{sd} / 2 &= & 7,50 \text{ kN} \\
 V_s / (0,5 * V_{pl,Rd}) & &= & \underline{0,05 \leq 1} \\
 \Rightarrow \text{No interaction!} & & &
 \end{aligned}$$

Check buckling strength:

$$\begin{aligned}
 \lambda_y &= 100 * l / i_y &= & 48,00 < 1 \\
 \lambda_{trans,y} &= \lambda_y / (\pi * \sqrt{E_s / f_y}) &= & 0,511 \\
 \lambda_z &= 100 * l / i_z &= & 179,10 \\
 \lambda_{trans,z} &= \lambda_z / (\pi * \sqrt{E_s / f_y}) &= & 1,91 \\
 h/b & &= & 2,00 > 1,2 \\
 t/10 & &= & 1,07 < 4 \\
 \text{Apply strut curve:} & & & \\
 \text{line} &= \text{SEL("steel/buck"; line;)} &= & a \\
 \alpha &= \text{TAB("steel/buck"; \alpha; line=line)} &= & 0,210 \\
 \chi_y &= \text{TAB("steel/buck"; \chi; \alpha=\alpha; \lambda q=\lambda_{trans,y})} &= & 0,9205 \\
 \\
 \text{Auxilliary values:} & & & \\
 \beta_M &= 1,30 \text{ Bild 5,5,3} & & \\
 \mu_y &= \lambda_{trans,y} * (2 * \beta_M - 4) + (W_{pl} - W_{el}) / W_{el} &= & -0,575 < 0,9 \\
 k_y &= 1 - (\mu_y * N_{sd}) / (\chi_y * A * f_y) &= & 1,013 < 1,5 \\
 \\
 N_{sd} / (\chi_y * A * f_y / \gamma_M) + 100 * k_y * M_{sd} / (W_{pl} * f_y / \gamma_M) & &= & \underline{0,076 < 1}
 \end{aligned}$$

Pos.: Single-span beam:

Span length $l = 7,50 \text{ m}$

Loads:

Dead weight $g = 3,00 \text{ kN/m}$
 Live load $q = 5,00 \text{ kN/m}$
 Snow load $s_0 = 2,00 \text{ kN/m}$

Materials and stresses:

steel = SEL("steel/EC"; Name;) = Fe 360
 $E_s = \text{TAB}(\text{"steel/EC"; E; Name=steel}) = 210000,00 \text{ N/mm}^2$
 $f_y = \text{TAB}(\text{"steel/EC"; } f_y; \text{ Name=steel}) = 235,00 \text{ N/mm}^2$

$\varepsilon = \sqrt{(235/f_y)} = 1,00$

Partial safety factors:

$\gamma_{fg} = 1,35$
 $\gamma_{fq} = 1,50$
 $\psi = 0,90$
 $\gamma_{Mo} = 1,10$

Design loads:

$q_{d1} = \gamma_{fg} \cdot g + \gamma_{fq} \cdot q = 11,55 \text{ kN/m}$
 $q_{d2} = \gamma_{fg} \cdot g + \psi \cdot \gamma_{fq} \cdot (q + s_0) = 13,50 \text{ kN/m}$
 $q_d = \text{MAX}(q_{d1}; q_{d2}) = 13,50 \text{ kN/m}$

Design moment:

$M_{sd} = q_d \cdot l^2 / 8 = 94,92 \text{ kNm}$
 Profil Typ = SEL("steel/Profils"; Name;) = IPE
 Selected Profil = SEL("steel/"Typ; Name; Mplyd $\geq M_{sd}$) = IPE 270

with $M_{pl,yd} = \text{TAB}(\text{"steel/"Typ; Mplyd; Name=Profil}) = 107,00 \text{ kNm}$

$M_{sd} / M_{pl,yd} = \underline{\underline{0,89 < 1}}$

Section classification:

Column height $h = \text{TAB}(\text{"steel/"Typ; } h; \text{ Name=Profil}) = 270,00 \text{ mm}$
 Depth of web $h_1 = \text{TAB}(\text{"steel/"Typ; } h_1; \text{ Name=Profil}) = 219,00 \text{ mm}$
 Web thickness $s = \text{TAB}(\text{"steel/"Typ; } s; \text{ Name=Profil}) = 6,60 \text{ mm}$
 Flange width $b = \text{TAB}(\text{"steel/"Typ; } b; \text{ Name=Profil}) = 135,00 \text{ mm}$
 Flange thickness $t = \text{TAB}(\text{"steel/"Typ; } t; \text{ Name=Profil}) = 10,20 \text{ mm}$
 Moment of inertia $I = \text{TAB}(\text{"steel/"Typ; } I_y; \text{ Name=Profil}) = 5790,00 \text{ cm}^4$

Section classification as in Table 5.3.1:**Web:**

$$(h_1 / s) / (72 * \epsilon) = 0,46 < 1$$

Flange:

$$(b / 2 / t) / (10 * \epsilon) = 0,66 < 1$$

⇒ Section class 1.

Check shear strength:

$$V_{sd} = 0,5 * q_d * l = 50,63 \text{ kN}$$

$$A_v = 1,04 * h * s / 100 = 18,53 \text{ cm}^2$$

$$V_{pl,Rd} = (A_v * f_y / 10) / (\sqrt{3} * \gamma_{Mo}) = 228,55 \text{ kN}$$

$$V_{sd} / V_{pl,Rd} = \underline{0,22 \leq 1}$$

Analysis working / servicing capacity as in Table 4.1:

$$q_{ser} = g + \psi * (q + s_0) = 9,30 \text{ kN/m}$$

$$\delta_{max} = 5/384 * (q_{ser} * (l * 100)^4) / (E_s * I * 10) = 3,15 \text{ cm}$$

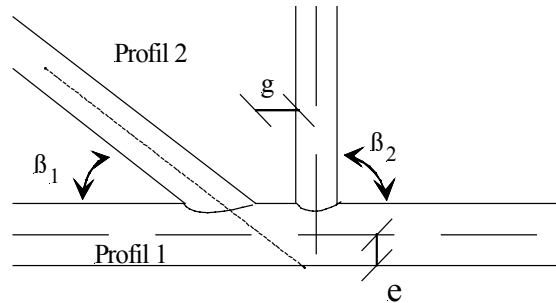
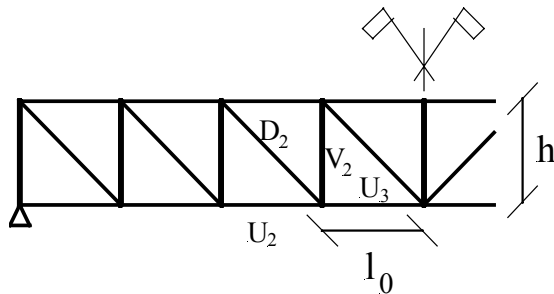
$$\delta_{max} / (l * 100 / 250) = \underline{1,05 \leq 1}$$

$$\delta_2 = 5/384 * ((q + s_0) * (l * 100)^4) / (E_s * I * 10) = 2,37 \text{ cm}$$

$$\delta_2 / (l * 100 / 300) = \underline{0,95 \leq 1}$$

Trusses and lattice girders

Lattice girder with circular hollow sectionsn:



Plan and elevation values:

Span length $l_0 =$	250,00 cm
$\beta_1 =$	30,96 °
$\beta_2 =$	90,00 °
$h =$	150,00 cm
$g =$	2,00 cm
$e =$	0,81 cm
Weld thickness $a =$	3,00 mm

Profil1: SEL("steel/R"; Name;)	=	R 114.3x5
$d_U =$ TAB("steel/R"; d; Name=Profil1)	=	114,30 mm
$t_U =$ TAB("steel/R"; t; Name=Profil1)	=	5,00 mm
$A_U =$ TAB("steel/R"; A; Name=Profil1)	=	17,20 cm ²
Profil2: SEL("steel/R"; Name;)	=	R 60.3x2.9
$d_2 =$ TAB("steel/R"; d; Name=Profil2)	=	60,30 mm
$t_2 =$ TAB("steel/R"; t; Name=Profil2)	=	2,90 mm
$A_2 =$ TAB("steel/R"; A; Name=Profil2)	=	5,23 cm ²
$i_2 =$ TAB("steel/R"; i; Name=Profil2)	=	2,03 cm

Materials and stresses:

steel = SEL("steel/EC"; Name;)	=	Fe 360
$E_s =$ TAB("steel/EC"; E; Name=steel)	=	210000,00 N/mm ²
$f_y =$ TAB("steel/EC"; f_y ; Name=steel)	=	235,00 N/mm ²
$\epsilon = \sqrt{(235 / f_y)}$	=	1,00
$\gamma_M =$	=	1,10
$\lambda_1 = 93,90 * \epsilon$	=	93,90

Member forces:

$U_2 =$	116,67 kN
$U_3 =$	200,00 kN
$D_2 =$	97,18 kN
$V_2 =$	50,00 kN Druck
$l_0 / (d_U / 10)$	= 21,87 > 6
$h / (d_2 / 10)$	= 24,88 > 6

Section classification:**Member V2:**

$$d_2 / t_2 / (50 * \epsilon^2) = \underline{0,42 < 1}$$

Section class 1

Analysis of the members:Member V₂:

$$\text{Section class 1 } \beta_A = 1,00$$

$$\lambda = 0,75 * h / i_2 = 55,42$$

$$\lambda_{trans} = \lambda / \lambda_1 * \sqrt{\beta_A} = 0,590$$

Apply strut curve a

$$\alpha = 0,21$$

$$\phi = 0,5 * (1 + \alpha * (\lambda_{trans} - 0,2) + \lambda_{trans}^2) = 0,715$$

$$\chi = 1 / (\phi + (\phi^2 - \lambda_{trans}^2)^{0,5}) = 0,8937$$

$$N_{b,Rd} = \chi * \beta_A * A_2 * f_y / 10 / \gamma_M = 99,85 \text{ kN}$$

$$V_2 / N_{b,Rd} = \underline{0,501 < 1}$$

Member D2:

$$N_{Rd} = A_2 * f_y / 10 / \gamma_M = 111,73 \text{ kN}$$

$$D_2 / N_{Rd} = \underline{0,870 < 1}$$

Member U2;U3

$$N_{Rd} = A_U * f_y / 10 / \gamma_M = 367,45 \text{ kN}$$

$$U_3 / N_{Rd} = \underline{0,544 < 1}$$

Analysis of joint:**Check permissible stress As in Table: K.5**

$$d_2 / d_U = 0,528 < 1$$

$$d_2 / d_U = 0,528 > 1$$

$$d_U / t_U = 22,860 > 10$$

$$d_U / t_U = 22,860 < 50$$

$$d_2 / t_2 = 20,793 > 10$$

$$d_2 / t_2 = 20,793 < 50$$

$$(t_U + t_2) / g = 3,950 < 1$$

Analysis as given in Table. K.6:

$$t_2 / 2,5 = 1,160 > 1$$

$$t_U / 25 = 0,200 < 1$$

$$\beta = \text{MIN}(\beta_1; \beta_2) = 30,960^\circ$$

$$30 / \beta = 0,969 < 1$$

$$e / (d_U / 4) = 0,028 < 1$$

⇒ Eccentricities can be neglected.

$$a / (\text{MIN}(t_U; t_2)) = 1,034 > 0,84$$

Calculate maximum stress As in Table K.6

Collapse of top chord:

$$\begin{aligned} \gamma &= d_U / (2 * t_U) &= & 11,43 \\ 10 * g / t_U & &= & 4,00 \\ c &= (0,5 * 10 * g / t_U - 1,33) &= & 0,670 \\ k_g &= \gamma^{0,2} * (1 + 0,024 * \gamma^{1,2} / (1 + 2,7183^c)) &= & 1,874 \\ k_p & &= & 1,00 \text{ (Zug)} \\ \beta &= d_2 / d_U &= & 0,528 \\ N_{1,Rd} &= k_g * k_p * f_y * t_U^2 / ((1 - \beta) * \sin(\beta_1)) * (1,8 + 10,2 * d_2 / d_U) * (1,1 / 10^3 / \gamma_M) &= & 325,61 \text{ kN} \\ N_{2,Rd} &= \sin(\beta_1) / \sin(\beta_2) * N_{1,Rd} &= & 167,51 \text{ kN} \end{aligned}$$

$$V_2 / N_{2,Rd} = \underline{\underline{0,30 < 1}}$$

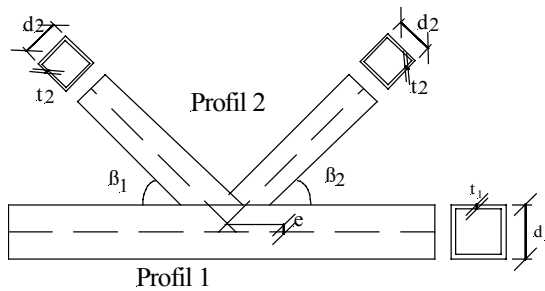
Collapse due to punching shear:

$$\begin{aligned} d_2 / (d_U - 2 * t_U) & &= & 0,58 < 1 \\ N_{i1,Rd} &= f_y / \sqrt{3} * t_2 * \pi * d_2 * (1 + \sin(\beta_1)) / (2 * (\sin(\beta_1))^2) * (1,1 / 10^3 / \gamma_M) &= & 213,27 \text{ kN} \end{aligned}$$

$$D_2 / N_{i1,Rd} = \underline{\underline{0,46 < 1}}$$

$$N_{i1,Rd} = f_y / \sqrt{3} * t_2 * \pi * d_2 * (1 + \sin(\beta_2)) / (2 * (\sin(\beta_2))^2) * (1,1 / 10^3 / \gamma_M) = 74,54 \text{ kN}$$

$$V_2 / N_{i1,Rd} = \underline{\underline{0,67 < 1}}$$

Truss joint with rectangular hollow sections:**Plan and elevation values:**

Span length $l_2 =$	200,00 cm
Projection length $\lambda_{ov} =$	40,00 %
$\beta_1 =$	50,00 °
$\beta_2 =$	50,00 °
$e =$	-2,00 cm
Weld thickness $a =$	3,50 mm

Profil1:	SEL("steel/QR"; Name;)	=	QR 100x4.0
$d_1 =$	TAB("steel/QR"; a; Name=Profil1)	=	100,00 mm
$t_1 =$	TAB("steel/QR"; t; Name=Profil1)	=	4,00 mm
$A_1 =$	TAB("steel/QR"; A; Name=Profil1)	=	15,20 cm ²

Profil2:	SEL("steel/QR"; Name;)	=	QR 60x4.0
$d_2 =$	TAB("steel/QR"; a; Name=Profil2)	=	60,00 mm
$t_2 =$	TAB("steel/QR"; t; Name=Profil2)	=	4,00 mm
$A_2 =$	TAB("steel/QR"; A; Name=Profil2)	=	8,82 cm ²
$i_2 =$	TAB("steel/QR"; i; Name=Profil2)	=	2,28 cm

Materials and stresses:

steel =	SEL("steel/EC"; Name;)	=	Fe 360
$E_s =$	TAB("steel/EC"; E; Name=steel)	=	210000,00 N/mm ²
$f_y =$	TAB("steel/EC"; f _y ; Name=steel)	=	235,00 N/mm ²

$$\epsilon = \sqrt{(235 / f_y)} = 1,00$$

$$\gamma_M = 1,10$$

$$\lambda_1 = 93,90 * \epsilon = 93,90$$

Member forces:

$U_l =$	250,00 kN
$U_r =$	150,00 kN
$D_l =$	77,80 kN (Druck)
$D_r =$	77,80 kN

Section classification:

Member DI:	
$d_2 / t_2 / (33 * \epsilon^2)$	= <u>0,45 < 1</u>
Section class 1	

Analysis of the members:**Member V2:**

$$\lambda = 0,75 \cdot l_2 / i_2 = 65,79$$

$$\text{Section class 1 } \beta_A = 1,00$$

$$\lambda_{\text{trans}} = \lambda / \lambda_1 \cdot \sqrt{\beta_A} = 0,70$$

Apply strut curve a

$$\alpha = 0,21$$

$$\varphi = 0,5 \cdot (1 + \alpha \cdot (\lambda_{\text{trans}} - 0,2) + \lambda_{\text{trans}}^2) = 0,797$$

$$\chi = 1 / (\varphi + (\varphi^2 - \lambda_{\text{trans}}^2)^{0,5}) = 0,8489$$

$$N_{b,Rd} = \chi \cdot \beta_A \cdot A_2 \cdot f_y / 10 / \gamma_M = 159,956 \text{ kN}$$

$$D_1 / N_{b,Rd} = \underline{0,486 < 1}$$

Member Dr:

$$N_{Rd} = A_2 \cdot f_y / 10 / \gamma_M = 188,427 \text{ kN}$$

$$D_r / N_{Rd} = \underline{0,413 < 1}$$

Member U2;U3

$$N_{Rd} = A_1 \cdot f_y / 10 / \gamma_M = 324,727 \text{ kN}$$

$$U_1 / N_{Rd} = \underline{0,770 < 1}$$

Analysis of joint:**Check permissible stress as in Table: K.14**

$$d_2 / d_1 = 0,60 > 0,25$$

$$d_2 / t_2 / (1,1 \cdot \sqrt{E_s / f_y}) = 0,456 < 1 \text{ (Druck)}$$

$$d_2 / t_2 = 15,000 < 35 \text{ (Zug)}$$

$$d_1 / t_1 = 25,000 < 35 \text{ (Zug)}$$

$$\lambda_{ov} / 100 = 0,400 < 1$$

$$25 / \lambda_{ov} = 0,625 < 1$$

Analysis as given in Table. K.12:

$$t_2 / 2,5 = 1,600 > 1$$

$$t_2 / 25 = 0,160 < 1$$

$$\beta = \text{MIN}(\beta_1; \beta_2) = 50,000^\circ$$

$$30 / \beta = 0,600 < 1$$

$$e / (-d_1 \cdot 0,55) = 0,036 < 1$$

⇒ Eccentricities can be neglected.

$$a / \text{MIN}(t_1; t_2) = 0,875 > 0,84$$

Calculate maximum stress As in Table K.14

Only the overlapping diagonals will be analysed:

$$b_{\text{eff}} = 1 / (d_1 / t_1) \cdot t_2 / t_1 \cdot d_2 = 2,40 \text{ cm}$$

$$b_{\text{eff}} / (\text{MIN}(d_1; d_2)/10) = 0,40 < 1$$

$$b_{e,ov} = 1 / (d_2 / t_2) \cdot t_1 / t_2 \cdot d_2 = 4,00 \text{ cm}$$

$$b_{e,ov} / (\text{MIN}(d_1; d_2)/10) = 0,67 < 1$$

$$k_n = 1,00 \text{ (Zug)}$$

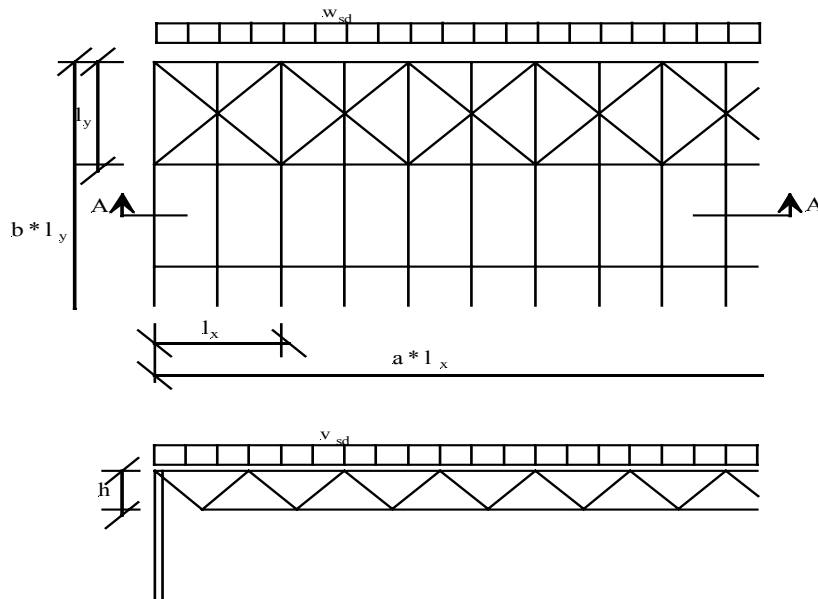
so that

$$\lambda_{ov} / 50 = 0,80 < 1$$

$$25 / \lambda_{ov} = 0,63 < 1$$

$$N_{2,Rd} = f_y / 10^2 \cdot t_2 \cdot (\lambda_{ov} / 50 \cdot (2 \cdot d_2 - 4 \cdot t_2) / 10 + b_{\text{eff}} + b_{e,ov}) = 138,368 \text{ kN}$$

$$D_r / N_{2,Rd} = \underline{0,562 < 1}$$

Roof truss:**Plan and elevation values:**

Span width l_x =	3,00 m
Span length l_y =	5,00 m
Number of spans in X a =	10
Number of spans in Y b =	10
Truss depth h =	2,00 m

section for chords:

Profil Typ =	SEL("steel/Profils"; Name;)	=	HEA
Selected Profil =	SEL("steel/"Typ; Name;)	=	HEA 140
Cross-sectional area A =	TAB("steel/"Typ; A; Name=Profil)	=	31,40 cm ²

steel =	SEL("steel/EC"; Name;)	=	Fe 360
E_s =	TAB("steel/EC"; E; Name=steel)	=	210000,00 N/mm ²

Loads:

w_{sd} =	2,00 kN/m
v_{sd} =	5,00 kN/m

Design loads:

$$M_{sd} = v_{sd} * (a * l_x)^2 / 8 = 562,50 \text{ kNm}$$

Compression force in the top chord:

$$N = M_{sd} / h = 281,25 \text{ kN}$$

Total compression force / Stabilising force:

$$N_{ges} = (a + 1) / 2 * N = 1546,88 \text{ kN}$$

Imperfection:

$$k_{r1} = \sqrt{0,2 + 1 / ((a + 1) / 2)} = 0,62$$

$$k_{r2} = 1,00$$

$$k_r = \text{MIN}(k_{r1}; k_{r2}) = 0,62 < 1$$

$$e_0 = k_r * a * l_x / 5 = 3,72 \text{ cm}$$

Equivalent load instead of buckling:

$$\delta_q = a * l_x / 25 = 1,20 \text{ cm}$$

$$q = N_{ges} / (60 * a * l_x) * (k_r + 0,2) = 0,70 \text{ kN/m}$$

$$h_{sd} = w_{sd} + q = 2,70 \text{ kN/m}$$

Check deformation δ_q :

$$E'_{\text{eff}} = 10^3 * E_s * 0,5 * A * I_y^2 = 8,24 * 10^{10} \text{ kNcm}^2$$

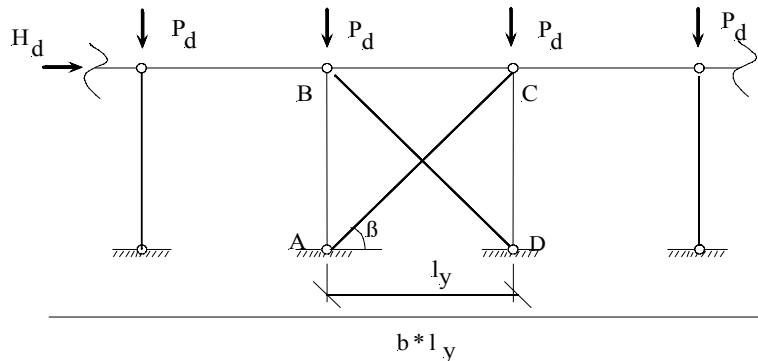
Deformation in the middle of truss:

$$\delta_{q1} = (5/384 * h_{sd} * (a * I_x)^4) / (E'_{\text{eff}}/10^6) = 0,35 \text{ cm}$$

$$\delta_{q1} / \delta_q = \underline{\underline{0,29 < 1}}$$

With it the acceptance, that $\delta_q \leq l / 2500$ properly.

It can be calculated with h_{sd} .

Vertical bracing Non sway frame:**Plan and elevation values:**

Frame width l_y =	6,00 m
Number of frames b =	5
Frame depth h =	5,00 m
Angle of bracing $\beta = \text{ATAN}(h/l_y) =$	39,81 °
Number of bracings n =	1
Number of storeys n_s =	1
Number of column $n_c =$	$b+1 = 6$
Diagonalen wirken auf Zug und auf Druck, Or else $s_d=1$	
$s_d =$	2

Profil Typ1 =	SEL("steel/Profils"; Name;)	=	IPE
Selected Profil1 =	SEL("steel/Typ1; Name;)	=	IPE 200
Moment of inertia $I_{y1} =$	TAB("steel/Typ1; l_y ; Name=Profil1)	=	1940,00 cm ⁴
Profil Typ2 =	SEL("steel/Profils"; Name;)	=	HEA
Selected Profil2 =	SEL("steel/Typ2; Name;)	=	HEA 180
Flange width $b_t =$	TAB("steel/Typ2; b ; Name=Profil2)	=	180,00 mm
Column height $h_t =$	TAB("steel/Typ2; h ; Name=Profil2)	=	171,00 mm
Flange thickness $t =$	TAB("steel/Typ2; t ; Name=Profil2)	=	9,50 mm
Moment of inertia $I_{y2} =$	TAB("steel/Typ2; l_y ; Name=Profil2)	=	2510,00 cm ⁴
Cross-sectional area $A_t =$	TAB("steel/Typ2; A ; Name=Profil2)	=	45,300 cm ²
$i_y =$	TAB("steel/Typ2; i_y ; Name=Profil2)	=	7,45 cm
$i_z =$	TAB("steel/Typ2; i_z ; Name=Profil2)	=	4,52 cm
ProfilR:	SEL("steel/R"; Name;)	=	R 177.8x5
$d =$	TAB("steel/R"; d ; Name=ProfilR)	=	177,80 mm
$t_r =$	TAB("steel/R"; t ; Name=ProfilR)	=	5,00 mm
$A_r =$	TAB("steel/R"; A ; Name=ProfilR)	=	27,10 cm ²
$i_r =$	TAB("steel/R"; i ; Name=ProfilR)	=	6,11 cm
Span length $l_r =$	$\sqrt{(h^2 + l_y^2)}$	=	7,81 m

Loads:

$H_d =$	80,00 kN
$P_d =$	300,00 kN

Materials and stresses:

steel =	SEL("steel/EC"; Name;)	=	Fe 360
E_s =	TAB("steel/EC"; E; Name=steel)	=	210000,00 N/mm ²
f_y =	TAB("steel/EC"; fy; Name=steel)	=	235,00 N/mm ²
ϵ =	$\sqrt{(235 / f_y)}$	=	1,00
γ_M =		=	1,10
λ_1 =	$93,90 * \epsilon$	=	93,90

Check swaying:

$k =$	$I_{y1} / I_{y2} * h / l_y$	=	0,644
Deflection at top of frame due to horizontal load:			
$H =$		=	1,00 kN
$\delta_F =$	$(100 * h)^3 * 10 / (12 * E_s * I_{y2}) * (2 * k + 1) / k * H$	=	0,702 cm
Shear strength:			
$S_V =$	$2 / 10 * n * E_s * A_r * h * I_y^2 / I_r^3$	=	430,1*10 ³ kN
$\delta_W =$	$H * h / S_V * 100$	=	1,16*10 ⁻³ cm
Deflection at top of frame:			
$H =$		=	1,00 kN
$\delta_{tot} =$	$1 / (1 / \delta_F + 1 / \delta_W)$	=	1,158*10 ⁻³ cm
Reduction due to bracing:			
$(1 - (\delta_{tot} / \delta_F)) * 100$		=	99,84 % > 80
⇒ Non sway frame.			

Analysis of vertical bracing

Imperfection to 5.2.4.3:

$\varphi_0 =$	$1 / 200$	=	0,005
$k_{C1} =$	$\sqrt{(0,5 + 1 / n_C)}$	=	0,82
$k_{C2} =$		=	1,00
$k_C =$	$\text{MIN}(k_{C1}; k_{C2})$	=	0,82
$k_{S1} =$	$\sqrt{(0,2 + 1 / n_S)}$	=	1,10
$k_{S2} =$		=	1,00
$k_S =$	$\text{MIN}(k_{S1}; k_{S2})$	=	1,00
$\varphi =$	$\varphi_0 * k_C * k_S$	=	0,0041
$\Delta H_d =$	$\varphi * P_d * (b + 1)$	=	7,38 kN
$H_{sd} =$	$H_d + \Delta H_d$	=	87,38 kN

Bracing is restrained out of plane of frame

$$\delta_W / (h * 100) * (b + 1) * P_d / H = 0,004 < 0,1$$

⇒ restrained from moving out of plane.

Analysis of lacing angles:

Design compression load:

$$N_{sd} = H_{sd} / (2 * \cos(\beta)) = 56,88 \text{ kN}$$

Slenderness:

$$\lambda = 100 * l_r / i_r = 127,82$$

Effective slenderness:

$$\lambda_{trans} = \lambda / (\lambda_1 * \epsilon) = 1,36$$

Apply strut curve a:

$$\alpha = 0,21$$

$$\beta_A = 1,000$$

$$\varphi = 0,5 * (1 + \alpha * (\lambda_{trans} - 0,2) + \lambda_{trans}^2) = 1,547$$

$$\chi = 1 / (\varphi + (\varphi^2 - \lambda_{trans}^2)^{0,5}) = 0,4378$$

$$N_{Rd} = \chi * \beta_A * A_r * f_y / 10 / \gamma_M = 253,47 \text{ kN}$$

$$N_{sd} / N_{Rd} = \underline{0,224 < 1}$$

Analysis of frame:

Column CD:

$$N_{sd} = P_d + H_{sd} / 2 * h / l_y = 336,41 \text{ kN}$$

Buckling in the plane of frame:

$$k_c = l_{y2} / h / 100 = 5,02 \text{ cm}^3$$

$$k_1 = 1,0 * l_{y1} / l_y / 100 = 3,23 \text{ cm}^3$$

$$k_2 = 0,0$$

$$\eta_2 = 1,0$$

$$\eta_1 = k_c / (k_c + k_1 + k_2) = 0,61$$

Slenderness ratio as in Fig. E.2.1.:

$$l = h * 0,85 = 4,25 \text{ m}$$

$$\lambda_y = 100 * l / i_y = 57,05$$

$$\lambda_{trans} = \lambda_y / (\lambda_1 * \epsilon) = 0,61$$

$$h_t / b_t = 0,95 < 1,2$$

Apply strut curve b:

$$\alpha = 0,34$$

$$\beta_A = 1,000$$

$$\varphi = 0,5 * (1 + \alpha * (\lambda_{trans} - 0,2) + \lambda_{trans}^2) = 0,756$$

$$\chi_y = 1 / (\varphi + (\varphi^2 - \lambda_{trans}^2)^{0,5}) = 0,8315$$

Buckling outside the plane of frame

$$\lambda_y = 100 * h / i_z = 110,62$$

$$\lambda_{trans} = \lambda_y / (\lambda_1 * \epsilon) = 1,18$$

Apply strut curve c:

$$\alpha = 0,49$$

$$\beta_A = 1,000$$

$$\varphi = 0,5 * (1 + \alpha * (\lambda_{trans} - 0,2) + \lambda_{trans}^2) = 1,436$$

$$\chi_z = 1 / (\varphi + (\varphi^2 - \lambda_{trans}^2)^{0,5}) = 0,4436$$

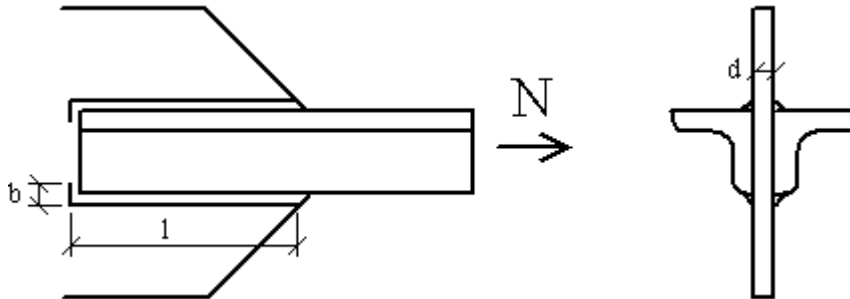
$$\chi_{min} = \text{MIN}(\chi_y, \chi_z) = 0,4436$$

$$N_{Rd} = \chi_{min} * \beta_A * A_t * f_y / 10 / \gamma_M = 429,30 \text{ kN}$$

$$N_{sd} / N_{Rd} = \underline{0,784 < 1}$$

Welded connections

Angle – gusset joint:



Dimensions of connection:

As demanded from EC3 6.6.2.2. $b =$	12,00 mm
Weld length $l =$	100,00 mm
Joint plate thickness $d =$	10,00 mm
Weld thickness $a_w =$	4,00 mm

Angle section $P =$	SEL("steel/WG"; Name;)	=	L 60x6
Area of angle $A =$	TAB("steel/WG"; A; Name=P)	=	6,91 cm ²
Width of angle $h =$	TAB("steel/WG"; a; Name=P)	=	60,00 mm

Materials and stresses:

steel =	SEL("steel/EC"; Name;)	=	Fe 360
$f_u =$	TAB("steel/EC"; fu; Name=steel)	=	360,00 N/mm ²
$f_y =$	TAB("steel/EC"; fy; Name=steel)	=	235,00 N/mm ²
$\beta_w =$	TAB("steel/EC"; β_w ; Name=steel)	=	0,80
$\gamma_{M0} =$	1,10		
$\gamma_{Mw} =$	1,25		

Plastic tension force:

$$N_{Rdp} = 2 * A * f_y / 10 / \gamma_{M0} = 295,25 \text{ kN}$$

Maximum strength of weld:

as in 6.6.5.2(2)

$$3 / a_w = 0,75 < 1$$

$$\text{MIN}(40; 6 * a_w) / l = 0,24 < 1$$

$$l / (150 * a_w) = 0,17 < 1$$

$$12 / b = 1,00 < 1$$

Reduction factor

$$\beta_{w1} = 1,2 - 0,2 * l / (150 * a_w) = 1,17$$

$$\beta_w = \text{MIN}(1; \beta_{w1}) = 1,00$$

$$l = \beta_w * l = 100,00 \text{ mm}$$

$$N_{w,Rd} = 4 * l * a_w * f_u / (\sqrt{3}) * \beta_w * \gamma_{Mw} / 10^3 = 266,04 \text{ kN}$$

Maximum strength of gusset:

Assumption: Stress spreads at 30° angle in gusset:

$$A = (2 * l * \text{TAN}(30) + h) * d / 100 = 17,55 \text{ cm}^2$$

$$N_{Rd} = A * f_y / 10 / \gamma_{M0} = 374,93 \text{ kN}$$

Limit design force for tension :

$$\text{MIN}(N_{Rd}; N_{w,Rd}; N_{Rdp}) = \underline{\underline{266,04 \text{ kN}}}$$

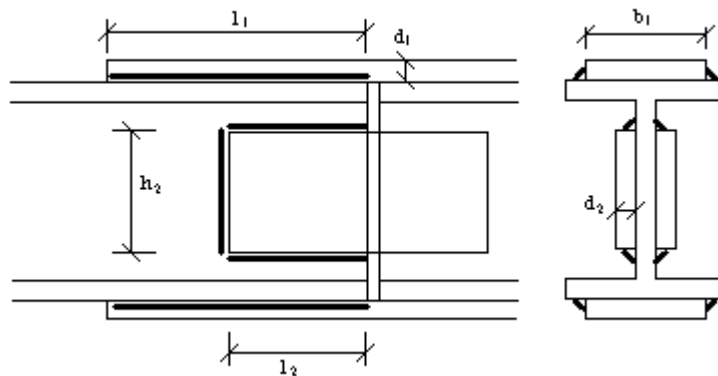
Welded beam splice**Dimensions of connection:**

Plate thickness d_1 =	20,00 mm
Plate thickness d_2 =	8,00 mm
Plate width b_1 =	160,00 mm
Plate thickness h_2 =	280,00 mm
Weld length l_1 =	240,00 mm
Weld length l_2 =	200,00 mm

Welds

Weld thickness Flange a_{wf} =	6,00 mm
Weld thickness Web a_{ws} =	4,00 mm
l_{wf} =	$2 * l_1$ = 480,00 mm
l_{ws} =	$2 * l_2 + h_2$ = 680,00 mm

Profil: IPE 400

Profil Typ =	SEL("steel/Profils"; Name;)	=	IPE
Selected Profil =	SEL("steel/"Typ; Name;)	=	IPE 400
Column height h =	TAB("steel/"Typ; h; Name=Profil)	=	400,00 mm
Web thickness s =	TAB("steel/"Typ; s; Name=Profil)	=	8,60 mm
Flange width b =	TAB("steel/"Typ; b; Name=Profil)	=	180,00 mm
Flange thickness t =	TAB("steel/"Typ; t; Name=Profil)	=	13,50 mm
Cross-sectional area A =	TAB("steel/"Typ; A; Name=Profil)	=	84,50 mm ²
W_{el} =	TAB("steel/"Typ; Wy; Name=Profil)	=	1160,00 cm ³
W_{pl} =	$1,14 * W_{el}$	=	1322,40 cm ³

Material and Partial safety factors:

steel =	SEL("steel/EC"; Name;)	=	Fe 360
f_u =	TAB("steel/EC"; fu; Name=steel)	=	360,00 N/mm ²
f_y =	TAB("steel/EC"; fy; Name=steel)	=	235,00 N/mm ²
β_w =	TAB("steel/EC"; β_w ; Name=steel)	=	0,80
γ_{M0} =	1,10		
γ_{M2} =	1,25		
γ_{Mw} =	1,25		

Loads :

M_{sd} =	157,95 kNm
V_{sd} =	60,75 kN

Check beam:

$$M_{c,Rd} = W_{pl} * f_y / \gamma_{M0} / 10^3 = 282,51 \text{ kNm}$$

$$M_{sd} / M_{c,Rd} = \underline{0,56 < 1}$$

$$A_v = 1,04 * h * s / 100 = 35,78 \text{ cm}^2$$

$$V_{pl,Rd} = A_v * f_y / 10 / \sqrt{3} / \gamma_{M0} = 441,32 \text{ kN}$$

$$V_{sd} / V_{pl,Rd} = \underline{0,14 < 1}$$

Check welds in flanges:

$$I_w = 2 / 12 * d_2 * h_2^3 / 10^4 = 2926,93 \text{ cm}^4$$

$$I_f = 2 * b_1 * d_1 * ((h + d_1) / 2)^2 / 10^4 = 28224,00 \text{ cm}^4$$

$$M_w = M_{sd} * I_w / (I_w + I_f) = 14,84 \text{ kNm}$$

$$M_f = M_{sd} * I_f / (I_w + I_f) = 143,11 \text{ kNm}$$

Effective tension force in flange

$$N_{sd} = M_f / (h + d_1) * 10^3 = 340,74 \text{ kN}$$

Limit shear stress of flange plates:

$$f_{v,wd} = f_u / 10 / (\sqrt{3}) * \beta_w * \gamma_{Mw} = 20,78 \text{ kN/cm}^2$$

Design stress:

$$f_{sd} = N_{sd} / (l_{wf} * a_{wf}) * 10^2 = 11,83 \text{ kN/cm}^2$$

$$f_{sd} / f_{v,wd} = \underline{0,57 < 1}$$

Change welds in web:

Centre of gravity

$$e = (2 * l_2 * l_2 / 2 * a_{ws}) / (l_{ws} * a_{ws}) = 58,82 \text{ mm}$$

$$I_x = (a_{ws} * h_2^3 / 12 + 2 * l_2 * (h_2 / 2)^2 * a_{ws}) / 10^4 = 3867,73 \text{ cm}^4$$

$$I_y = (h_2 * a_{ws} * e^2 + 2 / 12 * a_{ws} * l_2^3 + 2 * l_2 * a_{ws} * (l_2 / 2 - e)^2) / 10^4 = 1192,16 \text{ cm}^4$$

Design moment

$$M_{sw} = M_w + V_{sd} * (l_2 - e) / 10^3 = 23,42 \text{ kNm}$$

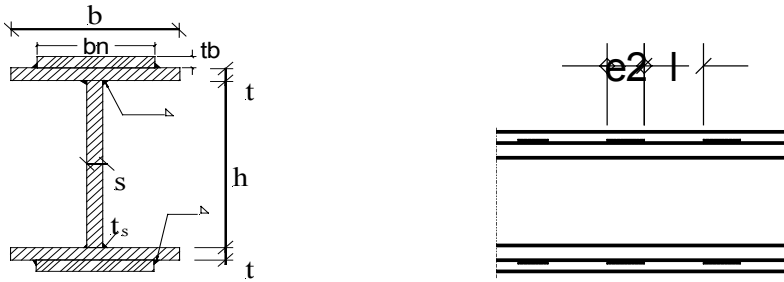
Maximum shear stress

$$f_{sx} = 10 * M_{sw} * h_2 / (4 * (I_x + I_y)) = 3,24 \text{ kN/cm}^2$$

$$f_{sy} = (V_{sd} / (l_{ws} * a_{ws} / 100) + (100 * M_{sw} * ((l_2 - e) / 10)) / (2 * (I_x + I_y))) = 5,50 \text{ kN/cm}^2$$

$$f_s = \sqrt{(f_{sx}^2 + f_{sy}^2)} = 6,38 \text{ kN/cm}^2$$

$$f_s / f_{v,wd} = \underline{0,31 < 1}$$

Beam with cover plates on flange:**Plan and elevation values:**

Flange width b =	16,00 cm
Flange thickness t =	1,20 cm
Depth of web h =	34,00 cm
Web thickness s =	0,80 cm
Plate thickness t_b =	0,80 cm
Weld thickness a =	0,30 cm
Weld distance l =	9,50 cm

Loads:

M_{Sd} =	241,90 kNm
V_{Sd} =	97,50 kN

Materials and stresses

steel =	SEL("steel/EC"; Name;)	=	Fe 360
f_y =	TAB("steel/EC"; f_y ; Name=steel)	=	235,00 N/mm ²
f_u =	TAB("steel/EC"; f_u ; Name=steel)	=	360,00 N/mm ²
β_w =	TAB("steel/EC"; β_w ; Name=steel)	=	0,80
ϵ =	$\sqrt{(235/f_y)}$	=	1,00

Partial safety factors:

γ_M =	1,10
γ_{Mw} =	1,25

Design:

W_{pl} =	$2 * (t * b * (h+t)/2 + s * h^2/8)$	=	907,04 cm ³
M_{pl} =	$0,001 * W_{pl} * f_y / \gamma_M$	=	193,78 kNm
$V_{pl,Rd}$ =	$h * s * f_y / 10 / (\sqrt{3}) * \gamma_M$	=	335,49 kN

Distance between cover plates:

b_n =	$(\gamma_M * 10 * M_{Sd} / f_y - W_{pl}) / (2 * t_b * (h/2 + t + t_b/2))$	=	-30,10 cm
sel b_n =		=	7,60 cm
W_{pl} =	$2 * (t * b * (h+t)/2 + s * h^2/8) + 2 * t_b * (h/2 + t + t_b/2) * b_n$	=	1133,22 cm ³
$M_{pl,Rd}$ =	$0,001 * W_{pl} * f_y / \gamma_M$	=	242,10 kNm

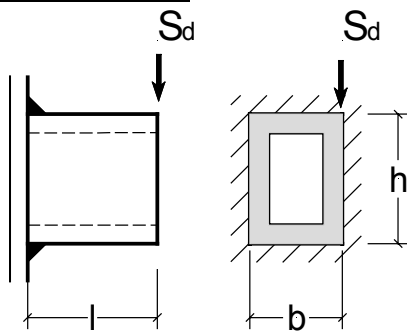
Analysis:

$M_{Sd} / M_{pl,Rd}$	=	<u>1,00 ≤ 1</u>
$V_{Sd} / (1/2 * V_{pl,Rd})$	=	<u>0,58 ≤ 1</u>

Length e2 of weld:

I_y =	$(b * (h + 2 * t)^3 - (b - s) * h^3) / 12 + 2 * t_b * b_n * (h/2 + t + t_b/2)^2$	=	18726,53 cm ⁴
T =	$V_{Sd} * (t_b * b_n * (h/2 + t + t_b/2)) / I_y$	=	0,59 kN/cm
$f_{v,wd}$ =	$f_u / 10 / (\sqrt{3}) * \beta_w * \gamma_{Mw}$	=	20,78 N/mm ²

$$\begin{aligned} F_{w,Rd} &= 0,2 * a * f_{v,wd} &= & 1,25 \text{ kN/cm} \\ e_2 &= T' / F_{w,Rd} &= & 0,47 \text{ cm} \\ \text{sel } e_2 &= & & \mathbf{40,00 \text{ mm (Minimum allowed length)}} \\ T &= T' * (e_2 + l) &= & 29,20 \text{ kN} \\ F_{w,Rd} &= 0,2 * a * e_2 * f_{v,wd} &= & 49,87 \text{ kN} \\ \text{Analysis:} & & & \\ T / F_{w,Rd} &= & & = \underline{\underline{0,59 \leq 1}} \end{aligned}$$

Welded connection**Plan and elevation values:**

Span length $l =$	200,00 mm
Width $b =$	80,00 mm
Web depth $h =$	140,00 mm
Weld thickness $a_w =$	6,00 mm

Loads:

$S_d =$	100,00 kN
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Materials and stresses:

steel =	SEL("steel/EC"; Name;)	=	Fe 360
$f_u =$	TAB("steel/EC"; f_u ; Name=steel)	=	360,00 N/mm ²
$\beta_w =$	TAB("steel/EC"; β_w ; Name=steel)	=	0,80

$$\gamma_{Mw} = 1,25$$

Design:

Weld properties:

$A =$	$0,02 * a_w * (b+h)$	=	26,40 cm ²
$I_y =$	$(2 * b * a_w * (h/2)^2 + 2 * a_w * h^3 / 12) / 10^4$	=	744,80 cm ⁴
$I_z =$	$(2 * h * a_w * (b/2)^2 + 2 * a_w * b^3 / 12) / 10^4$	=	320,00 cm ⁴
$I_p =$	$I_y + I_z$	=	1064,80 cm ⁴

Design load in relation to the centroid of weld:

$S_{dz} =$	S_d	=	100,00 kN
$M_{y,Sd} =$	$S_d * l/10$	=	2000,00 kNcm
$M_{t,Sd} =$	$S_d * b/20$	=	400,00 kNcm

Check stress at weakest point:

$\sigma_A =$	$M_{y,Sd} / I_y * h / 20$	=	18,80 kN/cm ²
$\tau_1 =$	$M_{t,Sd} / I_p * h / 20$	=	2,63 kN/cm ²
$\tau_2 =$	$M_{t,Sd} / I_p * b / 20 + S_{dz} / A$	=	5,29 kN/cm ²
$\Rightarrow \sigma_{res} =$	$\sqrt{(\sigma_A^2 + \tau_1^2 + \tau_2^2)}$	=	<u>19,71 kN/cm²</u>

Check weld strength:

Limit shear stress

$f_{w,Rd} =$	$f_u / 10 / (\sqrt{3}) * \beta_w * \gamma_{Mw}$	=	20,78 kN/cm ²
$\sigma_{res} / f_{w,Rd}$		=	<u>0,95 < 1</u>